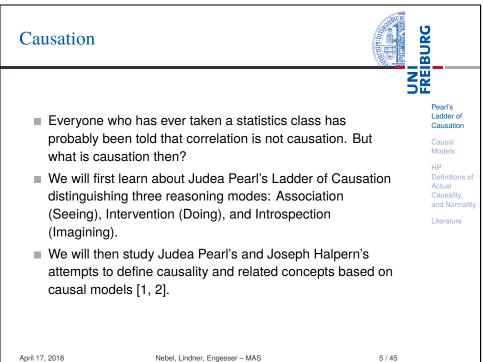
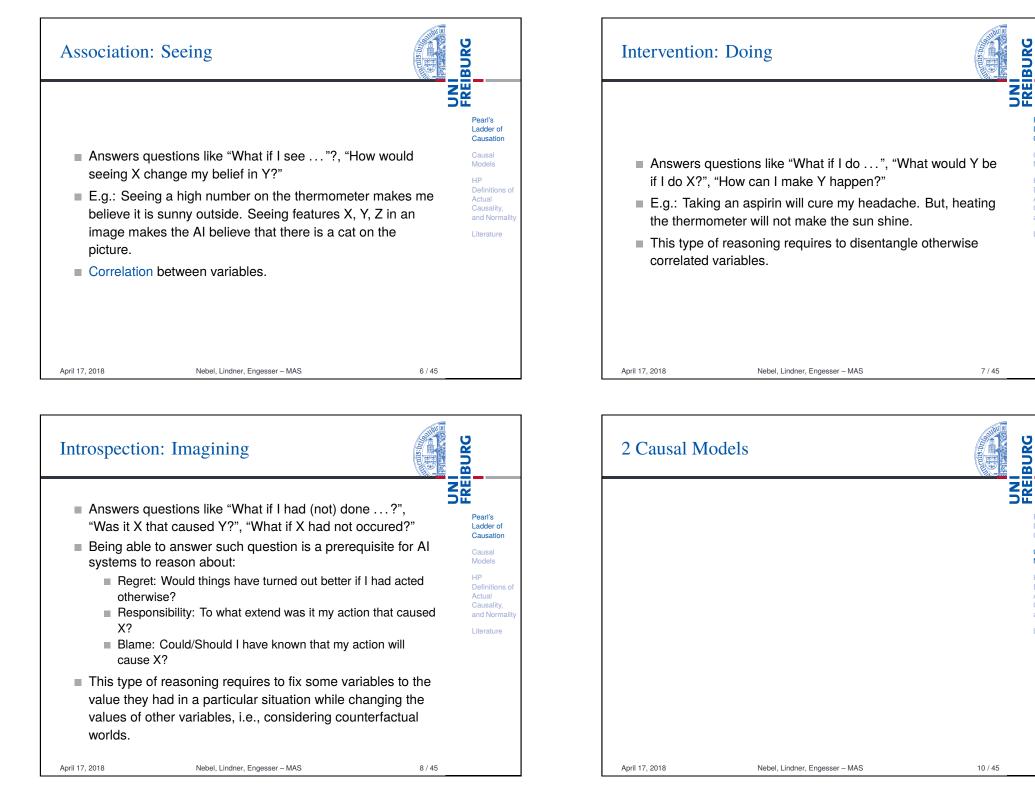


Motivation			BURG
•	are used or are about to be used Ily affect people's life significantly etc.		Pear Lado Cau:
Regulation, e	The European Union General Da everyone has the right to obtain a on reached [] and to challenge	an explanation	Mod HP Defii Actu Cau
Explainable	s currently a huge interest in so-c AI (XAI), i.e., the design and ana are able to explain their decision	lysis of	and Liter
clearify whicl	gent System, deriving causal exp h agents' actions resulted in som ue, i.e., assigning responsibility a	e proposition	
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Pearl's

HP Definitions of

Actual

and Normalit

Literature

Pearl's

Ladder of

Causation

Causal

Models

Actual

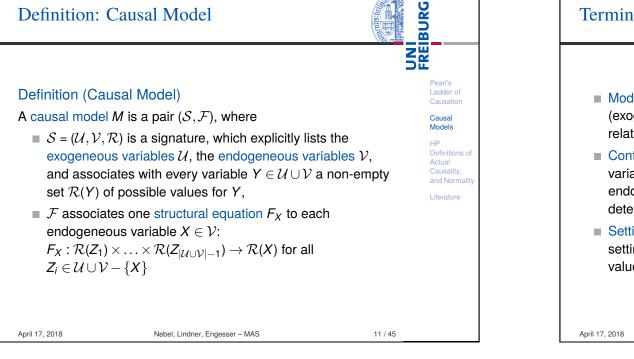
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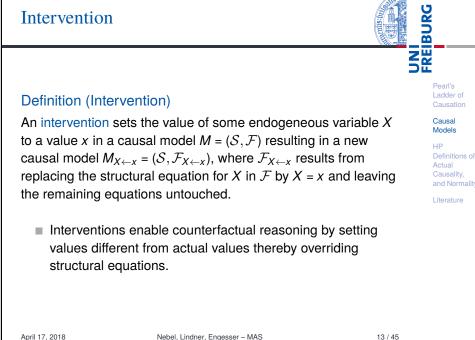
Literature

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Ladder of

Causation





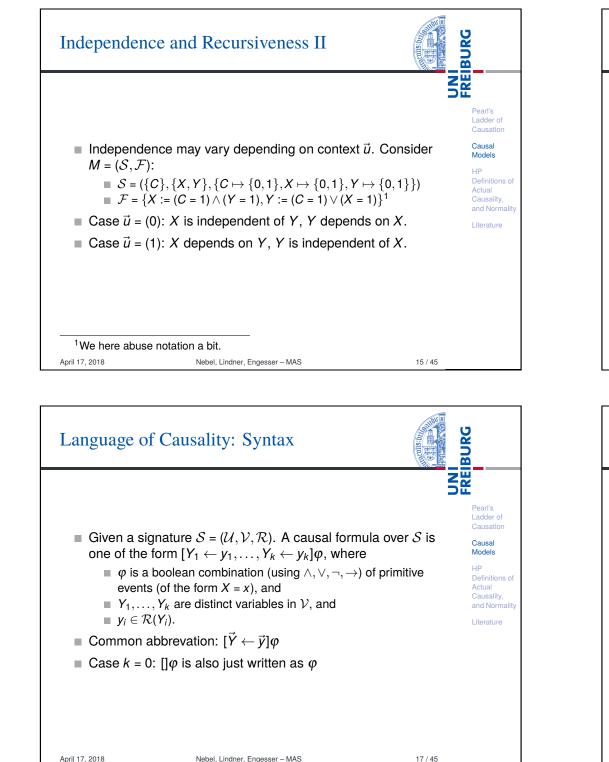
Terminology		BURG
		PRE
(exogeneou	pecification of the available variables is and endogeneous) and their structu s (via structural equations).	Pearl's Ladder of Causation Causal Models HP
variables. (	An assignment of values to the exoger From this assignment, the values of th us variables can be deterministically ).	neous Definitions Actual
	$\vec{u}$ ): A pair of a model and a context de a setting, every variable in the model h	
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Independenc	e and Recursiveness I	KEBURG
-	riable Y is independent of endogened	Gausai
endogeneous va	etting $(M, \vec{u})$ iff for all settings $\vec{z}$ of the riables other than X and Y, and all va = $F_Y(x', \vec{z}, \vec{u})$ holds.	Models Ilues x, x' HP Definitions Actual Causality

#### **Definition (Recursive Model)**

A model *M* is recursive iff for each context  $\vec{u}$ , there is a partial order  $\leq_{\vec{u}}$  (reflexive, anti-symmetric, transitive) of the endogeneous variables, such that unless  $X \leq_{\vec{u}} Y$ , Y is independent of X in  $(M, \vec{u})$ .

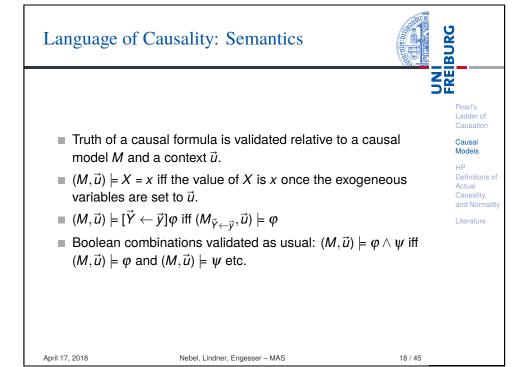
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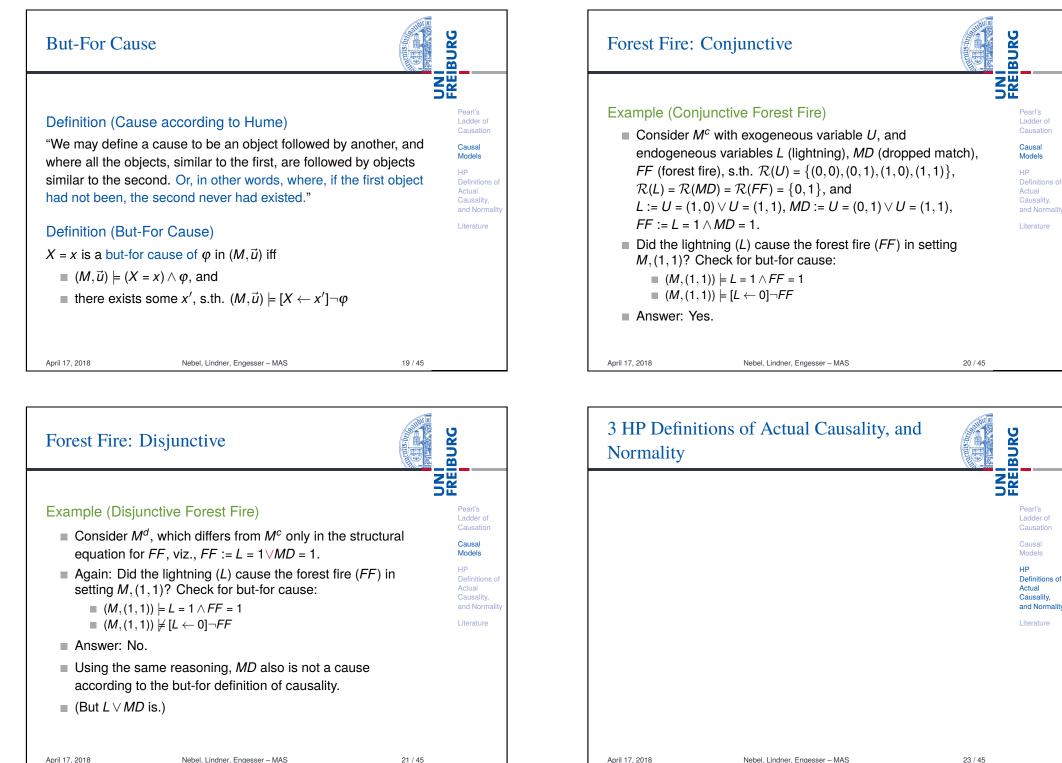
Independence and Recursiveness III	EBURG
<ul> <li>For a recursive model <i>M</i> and context <i>u</i>, the value of all endogeneous variables can be determined deterministically:</li> <li>First, determine values of variables that depend only on <i>u</i></li> </ul>	Pearl's Ladder of Causation Causal Models HP Definitions of Actual
<ul> <li>(first level).</li> <li>Second, determine values of variables that depend only on <i>u</i> and first-level variables (second level).</li> <li></li> <li>In everything that follows, "causal model" will always mean</li> </ul>	Causality, and Normality Literature
"recursive causal model".	

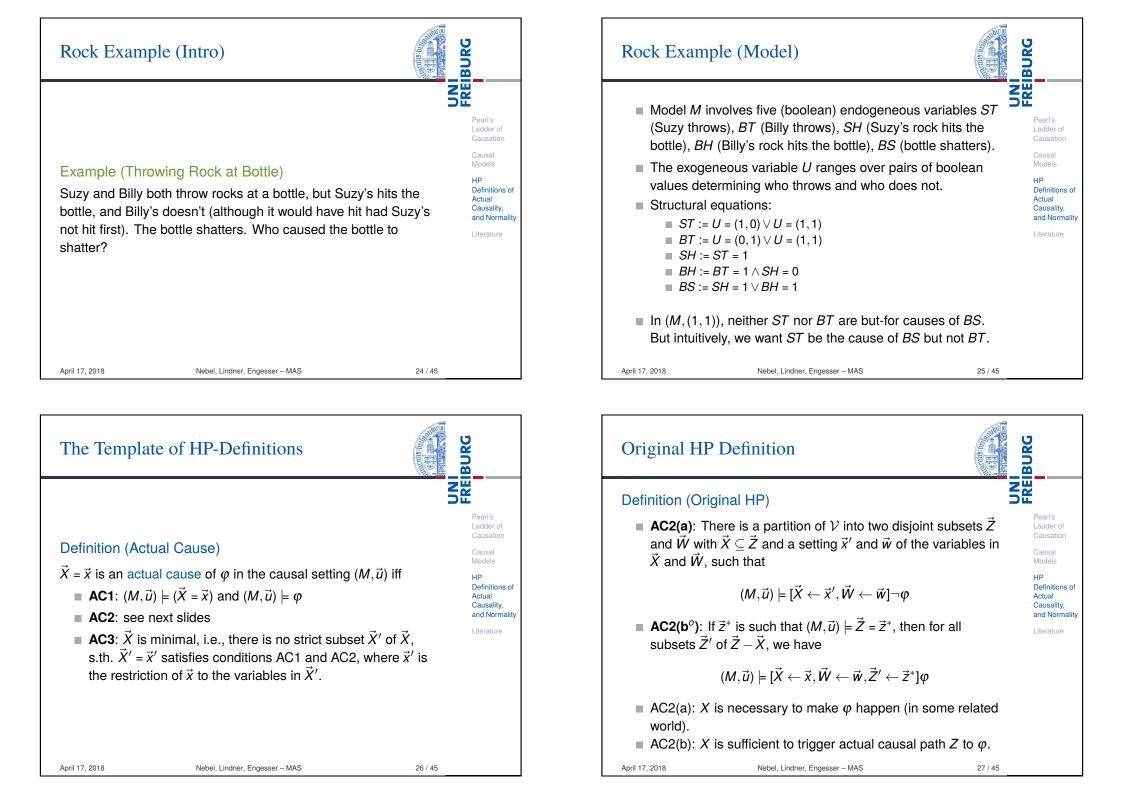
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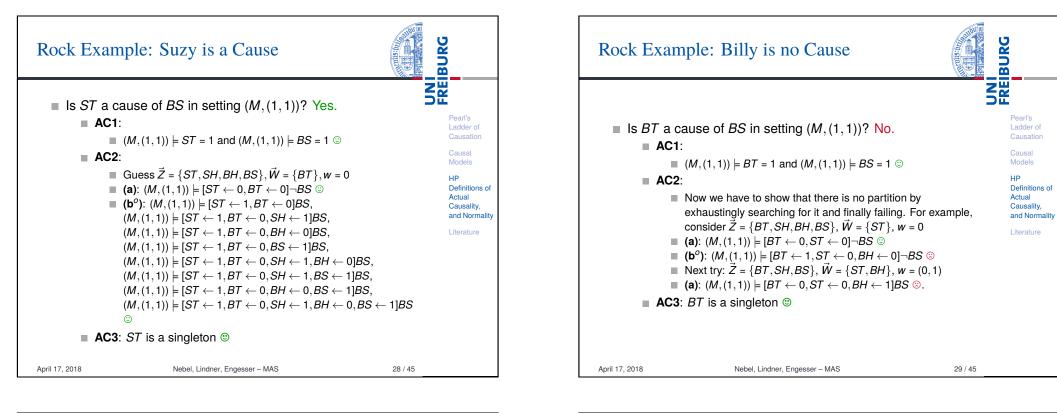


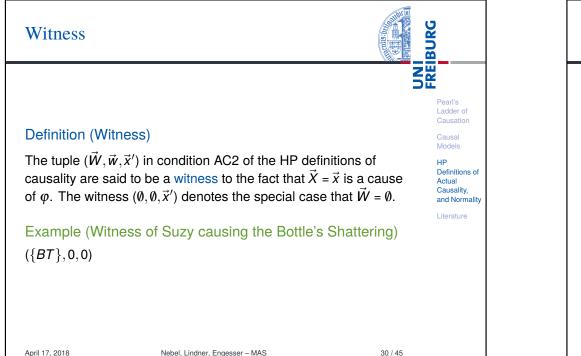
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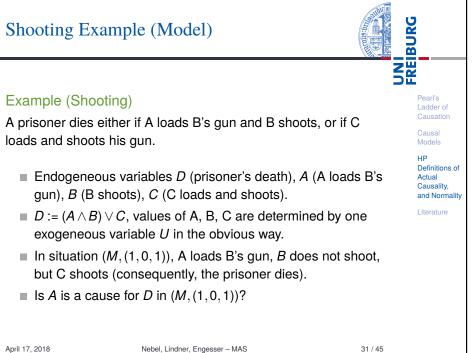
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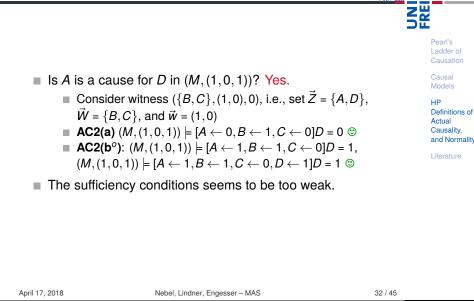


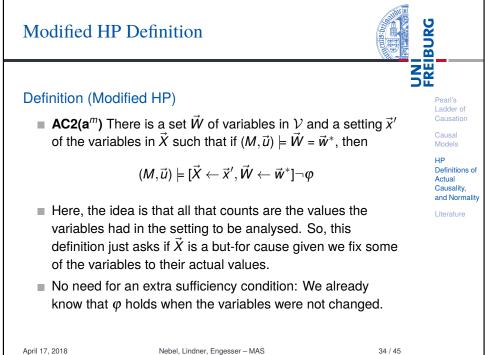




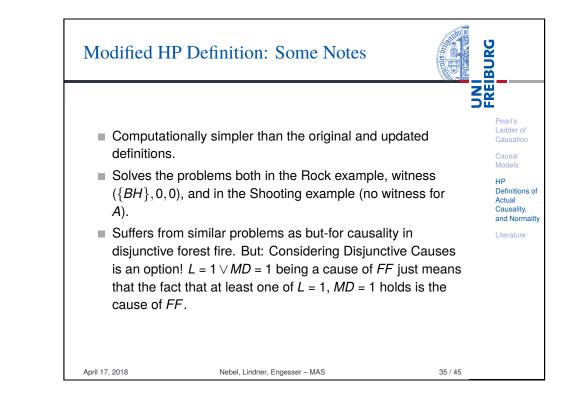


# BURG Shooting Example: A is a Cause of D





#### BURG Updated HP-Definition **FREI** Definition (Updated HP) Pearl's Ladder of AC2(a) same as original HP definition Causation **AC2(b**<sup>*u*</sup>) If $\vec{z}^*$ is such that $(M, \vec{u}) \models \vec{Z} = \vec{z}^*$ , then for all subsets $\vec{W}'$ of $\vec{W}$ and subsets $\vec{Z}'$ of $\vec{Z} - \vec{X}$ , we have HP Definitions of $(M,\vec{u}) \models [\vec{X} \leftarrow \vec{x}, \vec{W}' \leftarrow \vec{w}, \vec{Z}' \leftarrow \vec{z}^*] \varphi$ Actual Causality and Normalit Literature According to updated HP definition, $\varphi$ must hold even if only some of the values in $\vec{W}$ are set to w. In the shooting example and under the chosen $\vec{Z}$ , $\vec{W}$ , w, we get $(M, \vec{u}) \not\models [A \leftarrow 1, C \leftarrow 0] \neg (D = 1)$ , so A's loading the gun was not sufficient for D's death, and hence, A did not cause D according to the updated HP definition. 33 / 45 April 17, 2018 Nebel, Lindner, Engesser - MAS



## Relationships (without proofs)



Ladder of

Causation

Models

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Causality

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and Normality

HP

#### Theorem (see Halpern, Proposition 2.2.2)

If X = x is a but-for cause of Y = y in  $(M, \vec{u})$ , then X = x is a cause of Y = y according to all three variants of the HP definition.

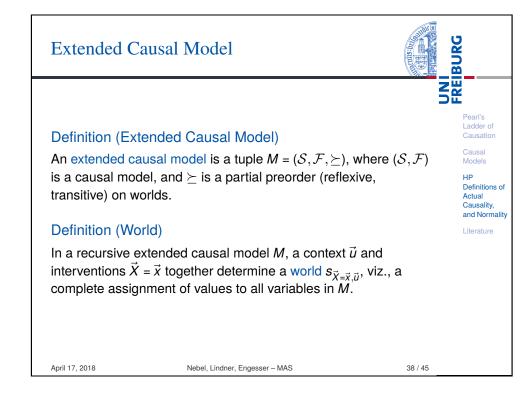
#### Theorem (see Halpern, Proposition 2.2.3)

- If X = x is part of a cause of φ in (M, u) according to the modified HP definition, then X = x is a cause of φ in (M, u) according to the original and the updated HP definition.
- If X = x is part of a cause of  $\varphi$  in  $(M, \vec{u})$  according to the updated HP definition, then X = x is a cause of  $\varphi$  in  $(M, \vec{u})$  according to the original HP definition.

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## Normality



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### Example (Normality, Knobe & Fraser)

The receptionist in the philosophy department keeps her desk stocked with pens. The administrative assistants are allowed to take the pens, but faculty members are supposed to buy their own. On Monday morning, one of the administrative assistants encounters Professor Smith walking past the receptionist's desk. Both take pens. Later that day, the receptionist needs to take an important message, but she has a problem: There are no pens left on her desk. Pearl's Ladder of Causation Causal Models HP Definitions of Actual Causality, and Normality Literature

- Who is the cause of there not being pens?
- Kahnemann and Miller:"an event is more likely to be undone by altering exceptional than route aspects of the causal chain that led to it".

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