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Outline



- Modeling agents exchanging arguments
 - Argumentation frameworks
 - Semantics
 - Algorithms

government.

- A: My government cannot negotiate with your government because your government does not even recognize my
- B: Your government does not recognize my government either.
- A: But your government is a terrorist government.
- Which arguments should be accepted?

Dispute II



- A: Ralph goes fishing, because it is sunday.
- B: Ralph does not go fishing, because it is Mother's day, so he visits his parents.
- C: Ralph cannot visit his parents, because it is a leap year, so they are on vacation.
- Which arguments should be accepted?

Core idea



A statement is accepted if it can be successfully defended against attacking arguments.

Definition (Argument)

An argument is a pair (S, φ) , such that S is a set of formulae and φ can be derived from S. S is also called the support for the claim φ .

Definition (Attack)

Two definitions of attack:

Undercut Argument $A_1 = (S_1, \varphi_1)$ undercuts argument $A_2 = (S_2, \varphi_2)$ iff $\neg \varphi_2$ can be derived from S_1 .

Rebuttal Argument $A_1 = (S_1, \varphi_1)$ rebuts argument $A_2 = (S_2, \varphi_2)$ iff $\varphi_1 \equiv \neg \varphi_2$.

- Disregarding internal structures of arguments
- Focus on the attack relation between arguments (a,b,c,d,...): a attacks b or $a \rightsquigarrow b$
- Not concerned with the origin of arguments or the attack relation

Abstract argumentation framework

An argumentation framework is a pair $\mathcal{AF} = (Arg, \leadsto)$ where Arg is a set of arguments and $\leadsto \subseteq Arg \times Arg$. We say that $a \in Arg$ attacks $b \in Arg$ iff $(a,b) \in \leadsto$.

- Remember:
 - A: Ralph goes fishing, because it is sunday.
 - B: Ralph does not go fishing, because it is Mother's day, so he visits his parents.
 - C: Ralph cannot visit his parents, because it is a leap year, so they are on vacation.
- Representation as an argumentation framework:

$$\mathcal{AF} = \langle \{a,b,c\}, \{(b,a),(c,b)\} \rangle,$$

$$(a) \longleftarrow (b) \longleftarrow (c)$$

$$\mathcal{AF} = \langle \{a,b,c\}, \{(b,a),(c,b)\} \rangle,$$

 \mathcal{AF} can also be understood as a logic program $\Pi_{\mathcal{AF}}$:

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a :- not -a.
b :- not -b.
c :- not -c.
-a :- b.
-b :- c.
```

The output of Π_{AF} is just its models. Those atoms that are true in the model correspond to the accepted arguments. Which ones?

Argument-based semantics get as input an argumentation framework and output zero or more sets of acceptable arguments.

Definition: Labelling

Let $\mathcal{AF} = (Arg, \leadsto)$ be an argumentation framework. A labelling of \mathcal{AF} is a total function $\mathcal{L}ab : Arg \rightarrow \{in, out, undec\}$. The set of all labellings will be denoted by $\mathcal{L}(\mathcal{AF})$.

- \blacksquare $in(\mathcal{L}ab) = \{a \mid \mathcal{L}ab(a) = \mathbf{in}\}$
- \blacksquare out($\mathcal{L}ab$) = $\{a \mid \mathcal{L}ab(a) = \mathbf{out}\}$
- $undec(\mathcal{L}ab) = \{a \mid \mathcal{L}ab(a) = undec\}$
- To refer to a labelling $\mathcal{L}ab$ we will also write $\langle in(\mathcal{L}ab), out(\mathcal{L}ab), undec(\mathcal{L}ab) \rangle$

Application to initial example



$$\mathcal{AF} = \langle \{a,b,c\}, \{(b,a),(c,b)\} \rangle,$$

$$(a) \longleftarrow (b) \longleftarrow (c)$$

$$\mathcal{L}(\mathcal{AF}) = \{ \langle \emptyset, \emptyset, \{a,b,c\} \rangle, \langle \emptyset, \{a\}, \{b,c\} \rangle \dots \}$$

- How to identify the appropriate labellings?
- E.g., we do not want to accept both a and b, thus if $\mathcal{L}ab(a) = \mathbf{in}$ then $\mathcal{L}ab(b) \neq \mathbf{in}$.

Definition

Let $\mathcal{L}ab$ be a labelling of argumentation framework \mathcal{AF} . An in-labelled argument is said to be legally in iff all its attackers are labelled **out**. An **out**-labelled argument is said to be legally out iff it has at least one attacker that is labelled in.

Definition

Let \mathcal{AF} be an argumentation framework. An admissible labelling is a labelling where each in-labelled argument is legally in and each out-labelled argument is legally out.

Application to initial example



$$\mathcal{AF} = \langle \{a,b,c\}, \{(b,a),(c,b)\} \rangle,$$

$$(a) \longleftarrow (b) \longleftarrow (c)$$

Admissible labellings

- $\blacksquare \langle \emptyset, \emptyset, \{a, b, c\} \rangle$
- $\blacksquare \langle \{a,c\},\{b\},\emptyset \rangle$

Definition

Given an argumentation framework $\mathcal{AF} = (Arg, \leadsto)$, a labelling semantics S associates with \mathcal{AF} a subset of $\mathcal{L}(\mathcal{AF})$, denoted as $\mathcal{L}_{S}(\mathcal{AF})$.

Complete semantics



Definition

Let $\mathcal{AF} = (Arg, \leadsto)$ be an argumentation framework and

 $\mathcal{L}ab: \textit{Arg} \rightarrow \{\textit{in}, \textit{out}, \textit{undec}\}$ be a total function. We say that

Lab is a complete labelling iff it satisfies the following:

$$\forall a \in Arg : (\mathcal{L}ab(a) = \mathbf{out} \leftrightarrow \exists b \in Arg : (b \leadsto a \land \mathcal{L}ab(b) = \mathbf{in}))$$

$$\forall a \in Arg : (\mathcal{L}ab(a) = \mathsf{in} \leftrightarrow \forall b \in Arg : (b \leadsto a \to \mathcal{L}ab(b) = \mathsf{out}))$$

$$\mathcal{AF} = \langle \{a,b,c\}, \{(b,a),(c,b)\} \rangle,$$



Complete labellings:

$$\langle \{a,c\},\{b\},\emptyset \rangle$$

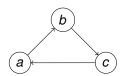
Why not
$$\langle \emptyset, \emptyset, \{a, b, c\} \rangle$$
?

Bert, Ernie, and Elmo



- A: Bert says that Ernie is unreliable, therefore everything that Ernie says cannot be relied on.
- B: Ernie says that Elmo is unreliable, therefore everything that Elmo says cannot be relied on.
- C: Elmo says that Bert is unreliable, therefore everything that Bert says cannot be relied on.

$$\mathcal{AF} = \langle \{a,b,c\}, \{(a,b),(b,c),(c,a)\} \rangle,$$



Complete labellings:

 \square $\mathcal{L}ab_1: \langle \emptyset, \emptyset, \{a,b,c\} \rangle$

Nixon Diamond



- A: Nixon is a pacifist, because he is a quaker.
- B: Nixon is not a pacifist, because he is a republican.

$$\mathcal{AF} = \langle \{a,b\}, \{(a,b), (b,a)\} \rangle,$$

Complete labellings:

 \blacksquare $\mathcal{L}ab_1: \langle \emptyset, \emptyset, \{a,b\} \rangle$

 \square $\mathcal{L}ab_3: \langle \{b\}, \{a\}, \emptyset \rangle$

⇒Three resonable positions a rational agent can take.

Definition

Let \mathcal{AF} be an argumentation framework. The grounded labelling of \mathcal{AF} is a complete labelling $\mathcal{L}ab$ where $in(\mathcal{L}ab)$ is minimal w.r.t. set inclusion.

- Grounded semantics picks the complete labelling with minimal in, minimal out, and maximal undec.
- Intuitively, the arguments in **in** are those that must be accepted by every rational agent.
- These arguments are in the in set of every complete labelling.
- The grounded labelling is unique.

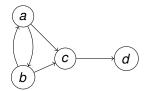
Definition

Let \mathcal{AF} be an argumentation framework. The preferred labelling of \mathcal{AF} is a complete labelling $\mathcal{L}ab$ where $in(\mathcal{L}ab)$ is maximal w.r.t. set inclusion.

- Preferred semantics picks the complete labelling with maximal in, maximal out, and minimal undec.
- For every argumentation framework one or more preferred labellings exists.

Preferred semantics: Example





- Ground labelling: $\langle \emptyset, \emptyset, \{a, b, c, d\} \rangle$
- Preferred labellings: $\langle \{a,d\}, \{b,c\}, \emptyset \rangle$, $\langle b,d\}, \{a,c\}, \emptyset \rangle$

Observe: Ground labelling is not among the preferred labellings and none of the preferred labellings is the ground labelling. Also, it is not the case that the ground labelling coincedes with the intersection of all preferred labellings.

Definition

Let $\mathcal{L}ab$ be a labelling of an argumentation framework \mathcal{AF} . $\mathcal{L}ab$ is a stable labelling of \mathcal{AF} iff it is a complete labelling with $\mathbf{undec}(\mathcal{L}ab) = \emptyset$.

- Stable semantics decides for every argument if it is in or out, no undec.
- As it minimizes undec it maximizes in and out. Thus, every stable labelling is a preferred labelling.
- But not vice versa: Whereas a preferred labelling always exists, the existence of a stable labelling is not guaranteed.

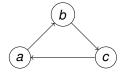
Applicability of stable semantics





Complete labellings:

 \blacksquare $\mathcal{L}ab_1:\langle\emptyset,\emptyset,\{a\}\rangle$



Complete labellings:

- \blacksquare $\mathcal{L}ab_2: \langle \emptyset, \emptyset, \{a,b,c\} \rangle$
- $\Rightarrow \mathcal{L}ab_1$, $\mathcal{L}ab_2$ are complete, ground, preferred, but not stable.



restriction on complete labelling	resulting semantics
no restrictions	complete semantics
empty undec	stable semantics
maximal in	preferred semantics
maximal out	preferred semantics
maximal undec	grounded semantics
minimal in	grounded semantics
minimal out	grounded semantics

- Every complete labelling is admissible.
- Every ground labelling is complete.
- Every preferred labelling is complete.
- Every stable labelling is preferred.

Definition (Credulous Acceptance)

Given $\mathcal{AF} = (Arg, \leadsto)$ and $a \in Arg$: is a labelled **in** in at least one ground/preferred/stable/...labelling?

- NP-complete for stable, admissible, complete, preferred
- P-complete for ground

Definition (Skeptical Acceptance)

Given $\mathcal{AF} = (Arg, \leadsto)$ and $a \in Arg$: is a labelled **in** in every ground/preferred/stable/...labelling?

stable: co-NP-complete

admissible: trivially false (empty in is admissible)

complete, ground: P-complete

■ preferred: Π_2^p -complete

- Other interesting decision problems:
 - Given some labelling, is it ground/preferred/stable/...?
 - Does there some ground/preferred/stable/...labelling exist?
 - Does there some nonempty ground/preferred/stable/...labelling exist?

- Given an argument A and and argumentation framework \mathcal{AF} , is A in the **in** set of \mathcal{AF} 's ground labelling?
- Given an argument A and and argumentation framework \mathcal{AF} , is A in the **in** set of some of \mathcal{AF} 's preferred labellings?

Definition

A partial labelling is a partial function $\mathcal{L}ab$: $Args \rightarrow \{in, out\}$ such that

- if $\mathcal{L}ab(A) = \mathbf{in}$ then for each attacker B $\mathcal{L}ab(B) = \mathbf{out}$
- if $\mathcal{L}ab(A) = \mathbf{out}$ then for some attacker B $\mathcal{L}ab(B) = \mathbf{in}$
- Partial labellings are admissible labellings
- A partial labelling $\mathcal{L}ab$ can be extended to a complete labelling $\mathcal{L}ab' \supseteq \mathcal{L}ab$
- For each complete labelling $\mathcal{L}ab'$ there exists a partial labelling $\mathcal{L}ab \subseteq \mathcal{L}ab'$ (just remove the **undec** labels)

Grounded labelling: Algorithm

Definition

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 \begin{array}{l} \textit{extendin}(\mathcal{L}\textit{ab}) = \mathcal{L}\textit{ab} \cup \{(\textit{A}, \textbf{in}) \, | \, \forall \textit{B} \, [\textit{B} \leadsto \textit{A} \rightarrow \mathcal{L}\textit{ab}(\textit{B}) = \textbf{out}]\} \\ \textit{extendout}(\mathcal{L}\textit{ab}) = \mathcal{L}\textit{ab} \cup \{(\textit{A}, \textbf{out}) \, | \, \exists \textit{B} \, [\textit{B} \leadsto \textit{A} \land \mathcal{L}\textit{ab}(\textit{B}) = \textbf{in}]\} \\ \textit{extendinout}(\mathcal{L}\textit{ab}) = \textit{extendin}(\mathcal{L}\textit{ab}) \circ \textit{extendout}(\mathcal{L}\textit{ab}) \end{array}
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If $\mathcal{L}ab$ is a partial labelling, then $extendin(\mathcal{L}ab)$, $extendout(\mathcal{L}ab)$, $extendinout(\mathcal{L}ab)$ are partial labellings. **function** GROUNDLABELLING($A\mathcal{F}$)

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\begin{array}{l} \textbf{function} \; \texttt{GROUNDLABELLING}(\mathcal{AF}) \\ L \leftarrow \emptyset \\ \textbf{repeat} \\ L_{old} \leftarrow L \\ L \leftarrow \textit{extendin}(L) \\ L \leftarrow \textit{extendout}(L) \\ \textbf{until} \; L = L_{old} \\ \textbf{return} \; L \cup \big\{ (A, \textbf{undec}) \, | \, (A, \textbf{in}) \not\in L \; \text{and} \; (A, \textbf{out}) \not\in L \big\} \\ \textbf{end function} \end{array}
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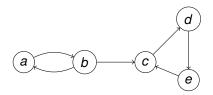
- Idea: Take the other's opinion and then derive a contradiction:
 - Proponent (M) makes a statement (A)
 - Opponent (S) derives from A more statements M will be committed to
 - S aims at letting M commit himself to a contradiction

Dialog game

- M starts and claims the existence of a reasonable position (admissible labelling) in which a particular argument is accepted (labelled in).
- S confronts M with the consequences of M's own position, and asks M to resolve these consequences.
- S wins if she leads M to a contradiction.
- If M wins then his argument is in the in set of an admissible labelling, and thus in the in of a preferred labelling.

Example Dialog





- M: in(D) I have an admissible labelling in which D is in
- S: out(C) But then in your labelling C is out. Why?
- M: in(B) Because B is in
- S: out(A) But then A must be out. Why?
- M: in(B) Because B is in.

Example Dialog





- M: in(C) I have an admissible labelling in which C is in
- S: out(A) But then in your labelling A is out. Why?
- M: in(B) Because B is in
- S: out(B) But B must be out!

Admissible discussion I



Definition

Let $\mathcal{AF} = (Arg, \leadsto)$ be an argumentation framework. An admissible discussion is a sequence of moves $[\Delta_1, \ldots, \Delta_n] (n \geq 0)$ such that:

- each move Δ_i (1 ≤ i ≤ n) where i is odd is called M-move and is of the form in(A)
- each move Δ_i (1 ≤ i ≤ n) where i is even is called S-move and is of the form out(A)
- for each S-move $\Delta_i = out(A)(2 \le i \le n)$ there exists an M-move $\Delta_i = in(B)(j < i)$ such that A attacks B
- for each M-move $\Delta_i = in(A)(3 \le i \le n)$ it holds that Δ_{i-1} is of the form out(B), where A attacks B
- there exist no two S-moves $\Delta_i = \Delta_j$ with $i \neq j$

Definition

An admissible discussion $[\Delta_1, ..., \Delta_n]$ is said to be finished iff

- There exists no Δ_{n+1} such that $[\Delta 1, \dots, \Delta_n, \Delta_{n+1}]$ is an admissible discussion, or there exists a M-move and a S-move containing the same argument
- 2 No subsequence of the discussion is finished.

Definition

A finished admissible discussion is won by player S if there exist a M-move and a S-move containing the same argument. Otherwise, it is won by the player making the last move.

Theorem

Let g be an admissible discussion won by M and let $\mathcal{L}ab: Ar \to \{\mathbf{in}, \mathbf{out}, \mathbf{undec}\}$ be a function defined as follows. For every argument $B \in Ar$:

- **Lab**(B) = **in** if B was labeled in during g
- $\mathcal{L}ab(B) = \mathbf{out}$ if B was labeled out during g
- \blacksquare $\mathcal{L}ab(B) =$ **undec** otherwise

Then $\mathcal{L}ab$ is an admissible labelling.

Thus, if there is a winning game for M defending A then A is in the in set of some preferred labelling (add undec arguments to in as long as possible).

SAT-Based Procedure [5]



Proposition 6 Let (A, R) be an argument system. A set $S \subseteq A$ is admissible iff S is a model of the formula

$$\bigwedge_{a \in A} ((a \to \bigwedge_{b:(b,a) \in R} \neg b) \land (a \to \bigwedge_{b:(b,a) \in R} (\bigvee_{c:(c,b) \in R} c))).$$

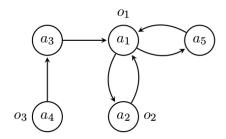
Example

- $AF = (\{a,b\}, \{(a,b), (b,a)\})$
- Is a credulously accepted: Is $a \land \varphi_{AF}$ satisfiable?

- Can be used to decide what to do next.
- Can be used to find perfect matchings [3]
 - Arg: The couples
 - \blacksquare $(m_1, w_1) \rightsquigarrow (m_2, w_2)$ iff
 - $m_1 = m_2$ and m_1 prefers w_1 to w_2 , or
 - $w_1 = w_2$ and w_1 prefers m_1 to m_2
- Ressource allocation
 - Arg: Pairs (agent, task)
 - $(agent_i, task_i) \rightsquigarrow (agent_j, task_j)$ iff one of:
 - (agent_i, task_i) is preferred to (agent_i, task_i)
 - (agent_i, task_i) excludes (agent_i, task_i)
 - Agent is unable to do $task_i$ (then self attack of $(agent_i, task_i)$)
- Can be used to compute the set of arguments an agent should utter / keep for itself (Persuation).

Argument-Based Decisions

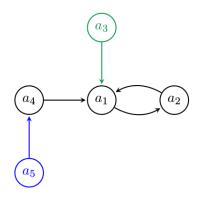




Source: [4]

Argument-Based Debates

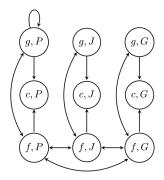




Source: [4]

Argument-Based Allocation





Souce: [4]

- In abstract argumentation systems all arguments are equally strong—relaxation
 - → Preference-based argumentation systems (e.g., Amgoud et al. 1998f) model preference (weights) of arguments.
- Arguments in abstract argumentation systems do not have an internal (logical) structure
 - → Deductive argumentation systems

Some projects available for BA/MA:

- SAT reductions of argumentation-framework semantics. Complexity preserving?
- Dialogue-based algorithms for the other semantics
- More types of semantics: semi-stable, stage, ideal, eager, cf2, ...
- Building argumentation frameworks from utterances
- Planning utterances based on argumentation frameworks
- Verbalization of argumentation frameworks

Literature





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