

Nondetermin	nistic planning	EBURG
changes tal and that we Other agen formalized Implications The fut We car sequen In some certain	istic planning we have assumed king place in the world are those e can exactly predict the results of ts and processes, beyond our co as (demonic) nondeterminism. S: ure state of the world cannot be pre- not reliably plan ahead: no single of the cases it is not possible to achieve ty no matter which outcomes the ac- ider certain fairness assumptions.	a caused by us of our actions. Transition systems and planning tasks pontrol, are Plans Plans the goals with
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# A note on the term *nondeterminism*

Nondeterminism occurs in three different kinds in computer science:

- demonic nondeterminism as in nondeterministic planning,
   i.e., on has to be prepared that the worst-case happens;
- angelic nondeterminism as in nondeterministic automata, where always the best choice is taken;
- don't care nondeterminism as in the variable choice in solving CSPs, where the choice does not influence the final outcome, but can make a difference in runtime.

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Motivation

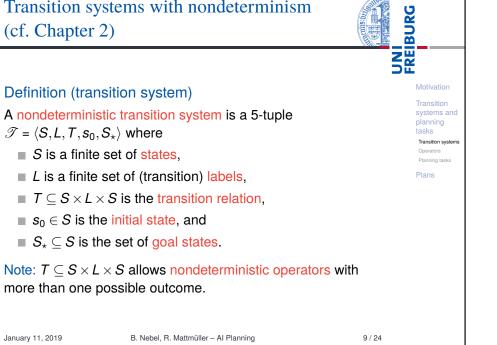
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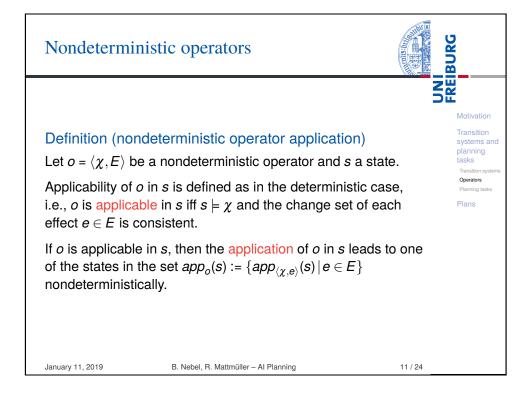
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Plans

## Transition systems with nondeterminism (cf. Chapter 2)

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## Nondeterministic planning task



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Plans

### Definition (nondeterministic planning task)

A (fully observable) nondeterministic planning task is a 4-tuple  $\Pi = \langle V, I, O, \gamma \rangle$  where

- *V* is a finite set of finite-domain state variables,
- I is an initial state over V,
- $\blacksquare$  *O* is a finite set of nondeterministic operators over *V*, and
- γ is a conjunctions of atoms over V describing the goal states.

Remark: In the following, we will always assume that our nondeterministic planning tasks are fully observable.

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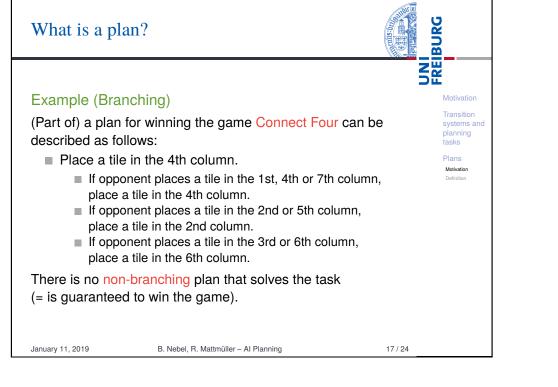
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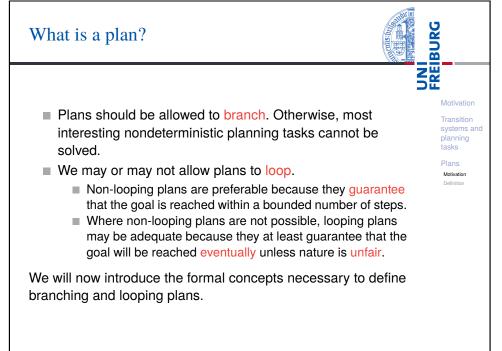
## Mapping planning tasks to transition systems



#### Motivation Definition (induced transition system) systems and Every nondeterministic planning task $\Pi = \langle V, I, O, \gamma \rangle$ induces a tasks corresponding nondeterministic transition system Transition syste Operators $\mathscr{T}(\Box) = \langle S, L, T, s_0, S_{\star} \rangle$ : Planning tasks Plans $\blacksquare$ S is the set of all states over V, $\blacksquare$ *L* is the set of operators *O*, $T = \{ \langle s, o, s' \rangle \mid s \in S, o \text{ applicable in } s, s' \in app_o(s) \},\$ $\blacksquare$ $s_0 = I$ , and $\blacksquare S_{\star} = \{ s \in S \mid s \models \gamma \}$ B. Nebel, R. Mattmüller - Al Planning 14/24 January 11, 2019







What is a pla	n?	BURG
<ol> <li>Build a wall If the structure</li> <li>Build a second If the structure</li> <li>Build a ceilin If the structure</li> <li>Build a wall If the structure</li> <li>There is no non-</li> </ol>	ing) Ig a card house can be described a with two cards. ure falls apart, redo from start. ond wall with two cards. ure falls apart, redo from start. Ing on top of the walls with a fifth ca ure falls apart, redo from start. on top of the ceiling with two cards ure falls apart, redo from start. Is apa	systems and planning tasks Plans Motivation Definition
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### Definition (strategy)

Let  $\Pi = \langle V, I, O, \gamma \rangle$  be a nondeterministic planning task with state set *S* and goal states *S*<sub>\*</sub>.

A strategy for  $\Pi$  is a function  $\pi : S_{\pi} \to O$  for some subset  $S_{\pi} \subseteq S$  such that for all states  $s \in S_{\pi}$  the action  $\pi(s)$  is applicable in s.

The set of states reachable in  $\mathcal{T}(\Pi)$  starting in state *s* and following  $\pi$  is denoted by  $S_{\pi}(s)$ .

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## Nondeterministic plans: formal definition



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### Definition (weak, closed, proper, and acyclic strategies)

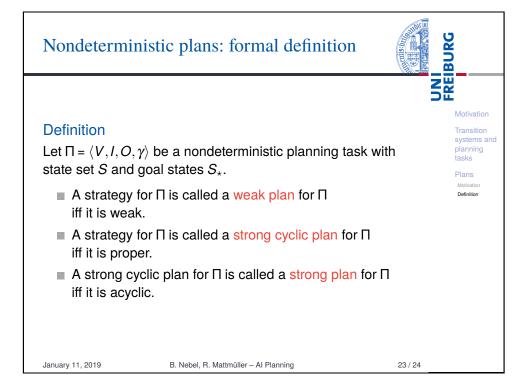
Let  $\Pi = \langle V, I, O, \gamma \rangle$  be a nondeterministic planning task with state set S and goal states  $S_*$ , and let  $\pi$  be a strategy for  $\Pi$ . Then  $\pi$  is called

- weak iff  $S_{\pi}(s_0) \cap S_{\star} \neq \emptyset$ ,
- closed iff  $S_{\pi}(s_0) \subseteq S_{\pi} \cup S_{\star}$ ,
- **proper** iff  $S_{\pi}(s') \cap S_{\star} \neq \emptyset$  for all  $s' \in S_{\pi}(s_0)$ , and
- **acyclic** iff there is no state  $s' \in S_{\pi}(s_0)$  such that s' is reachable from s' following  $\pi$  in a strictly positive number of steps.

Note: Proper implies closed and acyclic together with closed implies proper.

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# UNI FREIBURG Nondeterministic plans: formal definition Motivation systems and Strategies in nondeterministic planning correspond to applicable operator sequences in deterministic planning. Plans Motivation In deterministic planning, a plan is an applicable operator Definition sequence that results in a goal state. In nondeterministic planning, we define different notions of "resulting in a goal state". 22/24 January 11, 2019 B. Nebel, R. Mattmüller - Al Planning

