Principles of AI Planning

8. Planning as search: relaxation heuristics

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Towards better relaxed plans

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Why does the greedy algorithm compute low-quality plans?

■ It may apply many operators which are not goal-directed.

How can this problem be fixed?

- Reaching the goal of a relaxed planning task is most easily achieved with forward search.
- Analyzing relevance of an operator for achieving a goal (or subgoal) is most easily achieved with backward search.

Idea: Use a forward-backward algorithm that first finds a path to the goal greedily, then prunes it to a relevant subplan.

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Relaxed plan steps



How to decide which operators to apply in forward direction?

■ We avoid such a decision by applying all applicable operators simultaneously.

Definition (plan step)

A plan step is a set of operators $\omega = \{\langle \chi_1, e_1 \rangle, \dots, \langle \chi_n, e_n \rangle\}.$ In the special case of all operators of ω being relaxed, we further define:

- Plan step ω is applicable in state s iff $s \models \chi_i$ for all $i \in \{1, ..., n\}.$
- The result of applying ω to s, in symbols $app_{\omega}(s)$, is defined as the state s' with $on(s') = on(s) \cup \bigcup_{i=1}^{n} [e_i]_s$.

general semantics for plan steps → much later

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Applying relaxed plan steps: examples

In all cases, $s = \{a \mapsto 0, b \mapsto 0, c \mapsto 1, d \mapsto 0\}.$

 \blacksquare $\omega = \{\langle c, a \rangle, \langle \top, b \rangle\}$

 \blacksquare $\omega = \{\langle c, a \rangle, \langle c, a \rhd b \rangle\}$

 $\blacksquare \omega = \{\langle c, a \land b \rangle, \langle a, b \rhd d \rangle\}$



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Parallel plans



Definition (parallel plan)

A parallel plan for a relaxed planning task $\langle A, I, O^+, \gamma \rangle$ is a sequence of plan steps $\omega_1, \ldots, \omega_n$ of operators in O^+ with:

- \blacksquare $s_0 := I$
- For i = 1, ..., n, step ω_i is applicable in s_{i-1} and $s_i := app_{\alpha_i}(s_{i-1})$.
- $\blacksquare s_n \models \gamma$

Remark: By ordering the operators within each single step arbitrarily, we obtain a (regular, non-parallel) plan.

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Serializations



Applying a relaxed plan step to a state is related to applying the operators in the step to a state in sequence.

Definition (serialization)

A serialization of plan step $\omega = \{o_1^+, \dots, o_n^+\}$ is a sequence $o_{\pi(1)}^+,\ldots,o_{\pi(n)}^+$ where π is a permutation of $\{1,\ldots,n\}$.

Lemma (conservativeness of plan step semantics)

If ω is a plan step applicable in a state s of a relaxed planning task, then each serialization o_1, \ldots, o_n of ω is applicable in s and $app_{o_1,...o_n}(s)$ dominates $app_{\omega}(s)$.

- Does equality hold for all/some serialization(s)?
- What if there are no conditional effects?
- What if we allowed general (unrelaxed) planning tasks?

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Forward states, plan steps and sets



Idea: In the forward phase of the heuristic computation,

- apply plan step with all operators applicable initially,
- 2 apply plan step with all operators applicable then,
- and so on.

Definition (forward state/plan step/set)

Let $\Pi^+ = \langle A, I, O^+, \gamma \rangle$ be a relaxed planning task.

The *n*-th forward state, in symbols s_n^F $(n \in \mathbb{N}_0)$, the *n*-th forward plan step, in symbols ω_n^{F} $(n \in \mathbb{N}_1)$, and the *n*-th forward set, in symbols S_n^F $(n \in \mathbb{N}_0)$, are defined as:

- $\mathbf{s}_0^\mathsf{F} := I$
- lacksquare $\omega_n^{\mathsf{F}} := \{ o \in O^+ \mid o \text{ applicable in } s_{n-1}^{\mathsf{F}} \} \text{ for all } n \in \mathbb{N}_1$
- $\blacksquare s_n^{\mathsf{F}} := app_{\omega^{\mathsf{F}}}(s_{n-1}^{\mathsf{F}}) \text{ for all } n \in \mathbb{N}_1$
- $S_n^F := on(s_n^F)$ for all $n \in \mathbb{N}_0$

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The max heuristic h_{max}

Definition (parallel forward distance)

The parallel forward distance of a relaxed planning task $\langle A, I, O^+, \gamma \rangle$ is the lowest number $n \in \mathbb{N}_0$ such that $s_n^{\mathsf{F}} \models \gamma$, or ∞ if no forward state satisfies γ .

Remark: The parallel forward distance can be computed in polynomial time. (How?)

Definition (max heuristic h_{max})

Let $\Pi = \langle A, I, O, \gamma \rangle$ be a planning task in positive normal form, and let s be a state of Π .

The max heuristic estimate for s, $h_{max}(s)$, is the parallel forward distance of the relaxed planning task $\langle A, s, O^+, \gamma \rangle$.

Remark: h_{max} is safe, goal-aware, admissible and consistent. (Why?)

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So far, so good...



We have seen how systematic computation of forward states leads to an admissible heuristic estimate.

However, this estimate is very coarse.

■ To improve it, we need to include backward propagation of information.

For this purpose, we use so-called relaxed planning graphs.

Forward distance

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AND/OR dags

Definition (AND/OR dag)

An AND/OR dag $\langle V, A, type \rangle$ is a directed acyclic graph $\langle V, A \rangle$ with a label function *type* : $V \rightarrow \{\land, \lor\}$ partitioning nodes into AND nodes $(type(v) = \land)$ and OR nodes $(type(v) = \lor)$.

Note: AND nodes drawn as squares, OR nodes as circles.

Definition (truth values in AND/OR dags)

Let $G = \langle V, A, type \rangle$ be an AND/OR dag, and let $u \in V$ be a node with successor set $\{v_1, \ldots, v_k\} \subseteq V$.

The (truth) value of u, val(u), is inductively defined as:

- If $type(u) = \land$, then $val(u) = val(v_1) \land \cdots \land val(v_k)$.
- If $type(u) = \vee$, then $val(u) = val(v_1) \vee \cdots \vee val(v_k)$.

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Let Π^+ be a relaxed planning task, and let $k \in \mathbb{N}_0$.

The relaxed planning graph of Π^+ for depth k, in symbols $RPG_k(\Pi^+)$, is an AND/OR dag that encodes

- \blacksquare which propositions can be made true in k plan steps, and
- how they can be made true.

Its construction is a bit involved, so we present it in stages.

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Running example

 $\langle A, I, \{o_1, o_2, o_3, o_4\}, \gamma \rangle$ with



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 $e \mapsto 0, f \mapsto 0, g \mapsto 0, h \mapsto 0\}$ $o_1 = \langle b \lor (c \land d), b \land ((a \land b) \rhd e) \rangle$ $o_2 = \langle \top, f \rangle$ $o_3 = \langle f, g \rangle$ $o_4 = \langle f, h \rangle$ $\gamma = e \land (g \land h)$

 $I = \{a \mapsto 1, b \mapsto 0, c \mapsto 1, d \mapsto 1,$

As a running example, consider the relaxed planning task

 $A = \{a,b,c,d,e,f,g,h\}$

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Running example: forward sets and plan steps



$$\begin{split} I &= \{a \mapsto 1, b \mapsto 0, c \mapsto 1, d \mapsto 1, e \mapsto 0, f \mapsto 0, g \mapsto 0, h \mapsto 0\} \\ o_1 &= \langle b \lor (c \land d), b \land ((a \land b) \rhd e) \rangle \\ o_2 &= \langle \top, f \rangle, \quad o_3 &= \langle f, g \rangle, \quad o_4 &= \langle f, h \rangle \\ \\ S_0^F &= \{a, c, d\} \\ \omega_1^F &= \{o_1, o_2\} \\ S_1^F &= \{a, b, c, d, f\} \\ \omega_2^F &= \{o_1, o_2, o_3, o_4\} \\ S_2^F &= \{a, b, c, d, e, f, g, h\} \\ \omega_3^F &= \omega_2^F \\ S_3^F &= S_2^F \text{ etc.} \end{split}$$

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Components of relaxed planning graphs



A relaxed planning graph consists of four kinds of components:

- Proposition nodes represent the truth value of propositions after applying a certain number of plan steps.
- Idle arcs represent the fact that state variables, once true, remain true.
- Operator subgraphs represent the possibility and effect of applying a given operator in a given plan step.
- The goal subgraph represents the truth value of the goal condition after *k* plan steps.

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Relaxed planning graph: proposition layers



Let $\Pi^+ = \langle A, I, O^+, \gamma \rangle$ be a relaxed planning task, let $k \in \mathbb{N}_0$.

For each $i \in \{0,...,k\}$, $RPG_k(\Pi^+)$ contains one proposition layer which consists of:

a proposition node a^i for each state variable $a \in A$.

Node a^i is an AND node if i = 0 and $I \models a$. Otherwise, it is an OR node.

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Relaxed planning graph: proposition layers

b⁴

 c^4

 d^4

 e^4

 f^4



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a⁰

 b^0

 c^0

 d^0

 e^0

 f^0

 g^2

b²

 d^2

 e^2

 f^2

(

9 -2 **g**⁴

g

 a^6

b⁶

 d^6

*f*⁶

 g^7

9

h

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Relaxed planning graph: idle arcs



For each proposition node a^i with $i \in \{1, ..., k\}$, $RPG_k(\Pi^+)$ contains an arc from a^i to a^{i-1} (idle arcs).

Intuition: If a state variable is true in step i, one of the possible reasons is that it was already previously true.

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Relaxed planning graph: idle arcs



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 b^0 b^1 b^2 b^3 b^4 b^5 b^6 b^7 b^8

e⁰ + e¹ + e² + e³ + e⁴ + e⁵ + e⁶ + e⁷ + e⁶

 $g^0 \leftarrow g^1 \leftarrow g^2 \leftarrow g^3 \leftarrow g^4 \leftarrow g^5 \leftarrow g^6 \leftarrow g^7 \leftarrow g^8$

 (h^0) (h^1) (h^2) (h^3) (h^4) (h^5) (h^6) (h^7) (h^7)

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Relaxed planning graph: operator subgraphs

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For each $i \in \{1, ..., k\}$ and each operator $o^+ = \langle \chi, e^+ \rangle \in O^+$, $RPG_k(\Pi^+)$ contains a subgraph called an operator subgraph with the following parts:

- one formula node n_{φ}^{i} for each formula φ which is a subformula of χ or of some effect condition in e^{+} :
 - If $\varphi = a$ for some atom a, n_{φ}^{i} is the proposition node a^{i-1} .
 - If $\varphi = \top$, n_{φ}^{i} is a new AND node without outgoing arcs.
 - If $\varphi = \bot$, n_{φ}^{i} is a new OR node without outgoing arcs.
 - If $\varphi = (\varphi' \wedge \varphi'')$, n_{φ}^i is a new AND node with outgoing arcs to $n_{\varphi'}^i$ and $n_{\varphi''}^i$.
 - If $\varphi = (\varphi' \lor \varphi'')$, n_{φ}^i is a new OR node with outgoing arcs to $n_{\varphi'}^i$ and $n_{\varphi''}^i$.

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Relaxed planning graph: operator subgraphs



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For each $i \in \{1,...,k\}$ and each operator $o^+ = \langle \chi, e^+ \rangle \in O^+$, $RPG_k(\Pi^+)$ contains a subgraph called an operator subgraph with the following parts:

- for each conditional effect $(\chi' \triangleright a)$ in e^+ , an effect node $o_{\chi'}^i$ (an AND node) with outgoing arcs to the precondition formula node n_{χ}^i and effect condition formula node $n_{\chi'}^i$, and incoming arc from proposition node a^i
 - unconditional effects *a* (effects which are not part of a conditional effect) are treated the same, except that there is no arc to an effect condition formula node
 - effects with identical condition (including groups of unconditional effects) share the same effect node
 - \blacksquare the effect node for unconditional effects is denoted by o^i

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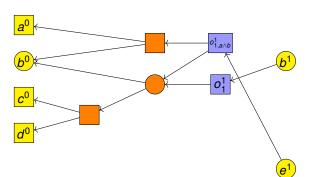
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Relaxed planning graph: operator subgraphs



Operator subgraph for $o_1 = \langle b \lor (c \land d), b \land ((a \land b) \rhd e) \rangle$ for layer i = 1.



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Relaxed planning graph: goal subgraph



 $RPG_k(\Pi^+)$ contains a subgraph called a goal subgraph with the following parts:

- one formula node n_{φ}^{k} for each formula φ which is a subformula of γ :
 - If $\varphi = a$ for some atom a, n_{φ}^{k} is the proposition node a^{i} .
 - If $\varphi = \top$, n_{φ}^{k} is a new AND node without outgoing arcs.
 - If $\varphi = \bot$, n_{φ}^{k} is a new OR node without outgoing arcs.
 - If $\varphi = (\varphi' \wedge \varphi'')$, n_{φ}^k is a new AND node with outgoing arcs to $n_{\varphi'}^k$ and $n_{\varphi''}^k$.
 - If $\varphi = (\varphi' \lor \varphi'')$, n_{φ}^k is a new OR node with outgoing arcs to $n_{\varphi'}^k$ and $n_{\varphi''}^k$.

The node n_{γ}^{k} is called the goal node.

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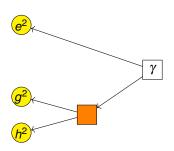
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Relaxed planning graph: goal subgraphs



Goal subgraph for $\gamma = e \wedge (g \wedge h)$ and depth k = 2:



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Connection to forward sets and plan steps

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Theorem (relaxed planning graph truth values)

Let $\Pi^+ = \langle A, I, O^+, \gamma \rangle$ be a relaxed planning task. Then the truth values of the nodes of its depth-k relaxed planning graph $RPG_k(\Pi^+)$ relate to the forward sets and forward plan steps of Π^+ as follows:

- Proposition nodes: For all $a \in A$ and $i \in \{0, ..., k\}$, $val(a^i) = 1$ iff $a \in S_i^F$.
- (Unconditional) effect nodes: For all $o \in O^+$ and $i \in \{1, ..., k\}$, $val(o^i) = 1$ iff $o \in \omega_i^F$.
- Goal nodes: $val(n_{\nu}^{k}) = 1$ iff the parallel forward distance of Π^{+} is at most k.

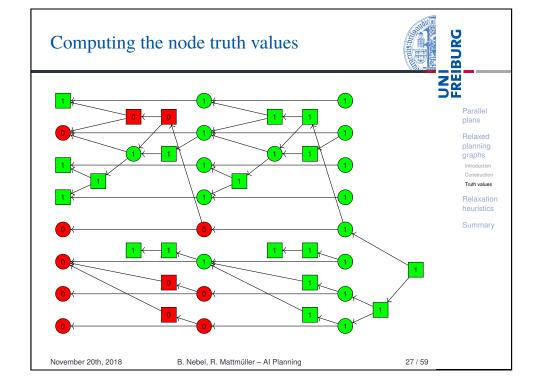
(We omit the straight-forward proof.)

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Relaxed planning graphs for STRIPS



Remark: Relaxed planning graphs have historically been defined for STRIPS tasks only. In this case, we can simplify:

- Only one effect node per operator: STRIPS does not have conditional effects.
 - Because each operator has only one effect node, effect nodes are called operator nodes in relaxed planning graphs for STRIPS.
- No goal nodes: The test whether all goals are reached is done by the algorithm that evaluates the AND/OR dag.
- No formula nodes: Operator nodes are directly connected to their preconditions.
- → Relaxed planning graphs for STRIPS are layered digraphs and only have proposition and operator nodes.

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Computing parallel forward distances from **RPGs**

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So far, relaxed planning graphs offer us a way to compute parallel forward distances:

Parallel forward distances from relaxed planning graphs

```
def parallel-forward-distance(\Pi^+):
```

Let A be the set of state variables of Π^+ .

for $k \in \{0, 1, 2, \dots\}$: $rpg := RPG_k(\Pi^+)$

Evaluate truth values for rpg.

if goal node of rpg has value 1:

return k

else if k = |A|:

return ∞

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Remarks on the algorithm



- The relaxed planning graph for depth k > 1 can be built incrementally from the one for depth k-1:
 - Add new layer k.
 - Move goal subgraph from layer k-1 to layer k.
- Similarly, all truth values up to layer k-1 can be reused.
- Thus, overall computation with maximal depth *m* requires time $O(\|RPG_m(\Pi^+)\|) = O((m+1) \cdot \|\Pi^+\|)$.
- This is not a very efficient way of computing parallel forward distances (and wouldn't be used in practice).
- However, it allows computing additional information for the relaxed planning graph nodes along the way, which can be used for heuristic estimates.

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Generic template

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Generic relaxed planning graph heuristics

Computing heuristics from relaxed planning graphs

```
def generic-rpg-heuristic(\langle A, I, O, \gamma \rangle, s):
     \Pi^+ := \langle A, s, O^+, \gamma \rangle
     for k \in \{0, 1, 2, \dots\}:
           rpg := RPG_k(\Pi^+)
           Evaluate truth values for rpg.
           if goal node of rpg has value 1:
                 Annotate true nodes of rpg.
                 if termination criterion is true:
```

return heuristic value from annotations

else if k = |A|: return ∞

generic template for heuristic functions

via to get concrete heuristic: fill in highlighted parts

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Forward cost heuristics

- The simplest relaxed planning graph heuristics are forward cost heuristics.
- Examples: h_{max}, h_{add}
- Here, node annotations are cost values (natural numbers).
- The cost of a node estimates how expensive (in terms of required operators) it is to make this node true.

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Concrete examples for the generic heuristic



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Many planning heuristics fit the generic template:

- additive heuristic *h*_{add} (Bonet, Loerincs & Geffner, 1997)
- max heuristic *h*_{max} (Bonet & Geffner, 1999)
- FF heuristic h_{FF} (Hoffmann & Nebel, 2001)
- cost-sharing heuristic h_{cs} (Mirkis & Domshlak, 2007)
 - not covered in this course
- set-additive heuristic h_{sa} (Keyder & Geffner, 2008)

Remarks:

- For all these heuristics, equivalent definitions that don't refer to relaxed planning graphs are possible.
- Historically, such equivalent definitions have mostly been used for h_{max} , h_{add} and h_{sa} .
- For those heuristics, the most efficient implementations do not use relaxed planning graphs explicitly.

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Forward cost heuristics: fitting the template

Forward cost heuristics

Computing annotations:

- Propagate cost values bottom-up using a combination rules for OR nodes and for AND nodes.
- At effect nodes, add 1 after applying combination rule.

Termination criterion:

stability: terminate if cost for proposition node a^k equals cost for a^{k-1} for all true propositions a in layer k (and true propositions in layers k and k-1 are the same)

Heuristic value:

- The heuristic value is the cost of the goal node.
- Different forward cost heuristics only differ in their choice of combination rules.

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The max heuristic h_{max} (again)

Forward cost heuristics: max heuristic h_{max} Combination rule for AND nodes:

 $oldsymbol{o}$ cost(u) = $oldsymbol{max}(\{cost(v_1), \dots, cost(v_k)\})$

(with $max(\emptyset) := 0$)

Combination rule for OR nodes:

 $cost(u) = min({cost(v_1), \dots, cost(v_k)})$

In both cases, $\{v_1, \dots, v_k\}$ is the set of true successors of u.

Intuition:

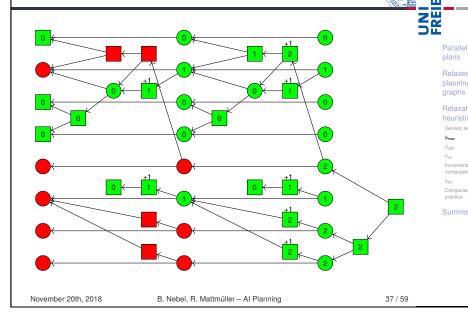
- AND rule: If we have to achieve several conditions, estimate this by the most expensive cost.
- OR rule: If we have a choice how to achieve a condition, pick the cheapest possibility.

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Running example: h_{max}



Remarks on h_{max}

- The definition of h_{max} as a forward cost heuristic is equivalent to our earlier definition in this chapter.
- Unlike the earlier definition, it generalizes to an extension where every operator has an associated non-negative cost (rather than all operators having cost 1).
- In the case without costs (and only then), it is easy to prove that the goal node has the same cost in all graphs $RPG_k(\Pi^+)$ where it is true. (Namely, the cost is equal to the lowest value of k for which the goal node is true.)
- We can thus terminate the computation as soon as the goal becomes true, without waiting for stability.
- The same is not true for other forward-propagating heuristics (h_{add} , h_{cs} , h_{sa}).

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Relaxation heuristics

h_{max} h_{add} h_{sa}

h_{sa} Incremental computation

n_{FF} Comparison & practice

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The additive heuristic

Forward cost heuristics: additive heuristic h_{add} Combination rule for AND nodes:

 $cost(u) = cost(v_1) + ... + cost(v_k)$ (with $\sum(\emptyset) := 0$)

Combination rule for OR nodes:

■ $cost(u) = min(\{cost(v_1), ..., cost(v_k)\})$ In both cases, $\{v_1, ..., v_k\}$ is the set of true successors of u.

Intuition:

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- AND rule: If we have to achieve several conditions, estimate this by the cost of achieving each in isolation.
- OR rule: If we have a choice how to achieve a condition, pick the cheapest possibility.

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Running example: h_{add} graphs B. Nebel, R. Mattmüller - Al Planning November 20th, 2018 40 / 59

Remarks on h_{add}



It is important to test for stability in computing h_{add} ! (The reason for this is that, unlike h_{max} , cost values of true propositions can decrease from layer to layer.)

- Stability is achieved after layer |A| in the worst case.
- \blacksquare h_{add} is safe and goal-aware.
- Unlike h_{max} , h_{add} is a very informative heuristic in many planning domains.
- The price for this is that it is not admissible (and hence also not consistent), so not suitable for optimal planning.
- In fact, it almost always overestimates the h^+ value because it does not take positive interactions into account.

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The set-additive heuristic

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- We now discuss a refinement of the additive heuristic called the set-additive heuristic h_{sa} .
- \blacksquare The set-additive heuristic addresses the problem that h_{add} does not take positive interactions into account.
- Like h_{max} and h_{add} , h_{sa} is calculated through forward propagation of node annotations.
- However, the node annotations are not cost values, but sets of operators (kind of).
- The idea is that by taking set unions instead of adding costs, operators needed only once are counted only once.

Disclaimer: There are some quite subtle differences between the h_{sa} heuristic as we describe it here and the "real" heuristic of Keyder & Geffner. We do not want to discuss this in detail, but please note that such differences exist.

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Operators needed several times

- \blacksquare The original h_{sa} heuristic as described in the literature is defined for STRIPS tasks and propagates sets of operators.
- This is fine because in relaxed STRIPS tasks, each operator need only be applied once.
- The same is not true in general: in our running example, operator o_1 must be applied twice in the relaxed plan.
- In general, it only makes sense to apply an operator again in a relaxed planning task if a previously unsatisfied effect condition has been made true.
- For this reason, we keep track of operator/effect condition pairs rather than just plain operators.

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Set-additive heuristic: fitting the template

The set-additive heuristic h_{sa} Computing annotations:

Annotations are sets of operator/effect condition pairs. computed bottom-up.

Combination rule for AND nodes:

■ $ann(u) = ann(v_1) \cup \cdots \cup ann(v_k)$ (with $\bigcup (\emptyset) := \emptyset$)

Combination rule for OR nodes:

■ $ann(u) = ann(v_i)$ for some v_i minimizing $|ann(v_i)|$ In case of several minimizers, use any tie-breaking rule.

In both cases, $\{v_1, \dots, v_k\}$ is the set of true successors of u. At effect nodes, add the corresponding operator/effect condition pair to the set after applying combination rule.

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Summary

Set-additive heuristic: fitting the template (ctd.)



The set-additive heuristic h_{sa} (ctd.)

Computing annotations:

... (Effect nodes for unconditional effects are represented just by the operator, without a condition.)

Termination criterion:

stability: terminate if set for proposition node a^k has same cardinality as for a^{k-1} for all true propositions a in layer k(and true propositions in layers k and k-1 are the same)

Heuristic value:

■ The heuristic value is the set cardinality of the goal node annotation.

Parallel

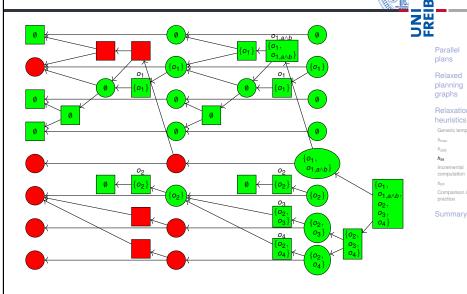
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Running example: $h_{\rm sa}$



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Remarks on $h_{\rm sa}$

- The same remarks for stability as for h_{add} apply.
- \blacksquare Like h_{add} , h_{sa} is safe and goal-aware, but neither admissible nor consistent.
- \blacksquare $h_{\rm sa}$ is generally better informed than $h_{\rm add}$, but significantly more expensive to compute.
- \blacksquare The h_{sa} value depends on the tie-breaking rule used, so h_{sa} is not well-defined without specifying the tie-breaking rule.
- The operators contained in the goal node annotation, suitably ordered, define a relaxed plan for the task.
 - Operators mentioned several times in the annotation must be added as many times in the relaxed plan.

Parallel

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Incremental computation of forward heuristics

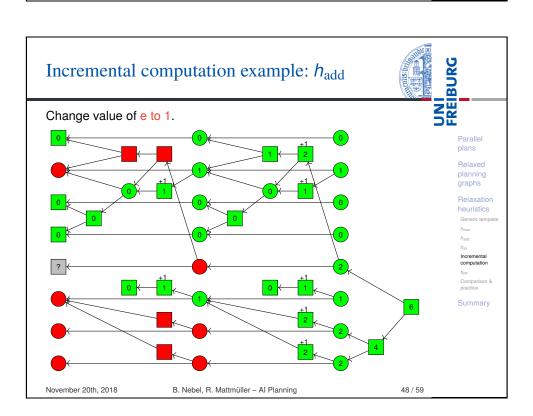
One nice property of forward-propagating heuristics is that they allow incremental computation:

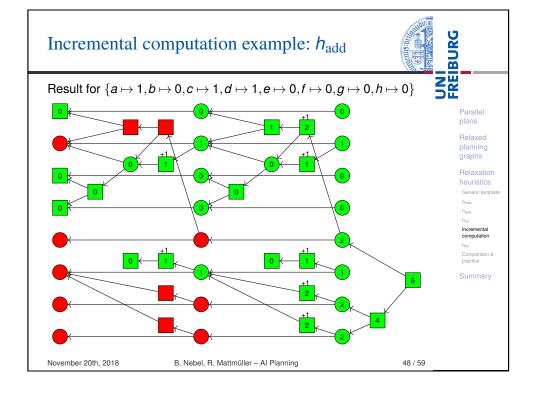
- when evaluating several states in sequence which only differ in a few state variables, can
 - start computation from previous results and
 - keep track only of what needs to be recomputed
- typical use case: depth-first style searches (e.g., IDA*)
- rarely exploited in practice

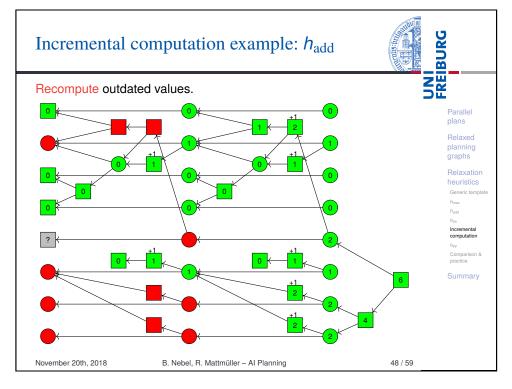
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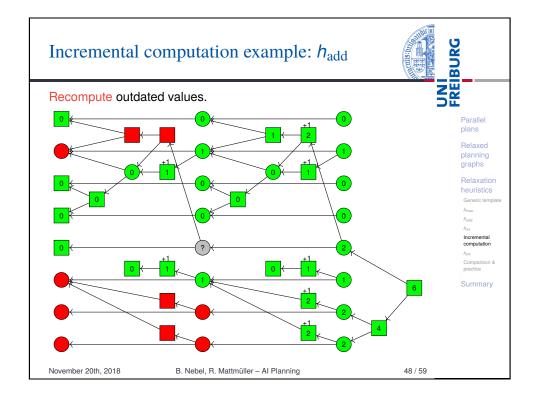
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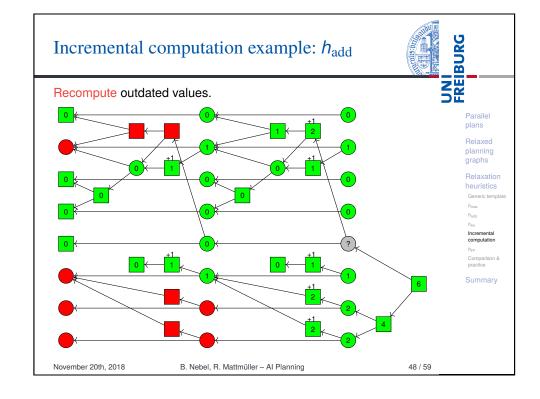
Parallel plans Relaxed planning graphs Relaxation heuristics Generic template hnase has incremental computation hpr Comparison & practice Summary

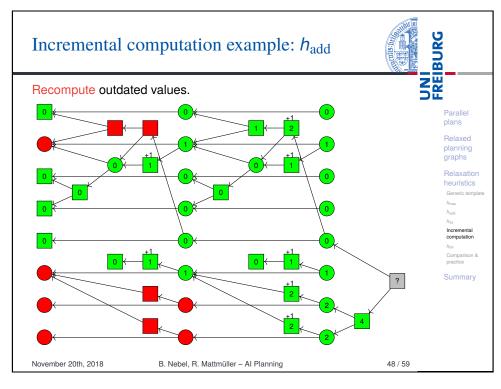


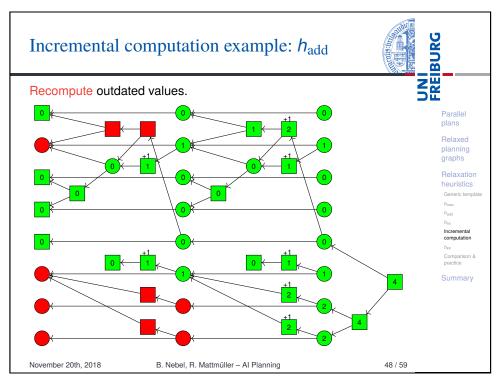












Heuristic estimate h_{FF}

- \blacksquare h_{sa} is more expensive to compute than the other forward propagating heuristics because we must propagate sets.
- It is possible to get the same advantage over h_{add} combined with efficient propagation.
- Key idea of *h*_{FF}: perform a backward propagation that selects a sufficient subset of nodes to make the goal true (called a solution graph in AND/OR dag literature).
- The resulting heuristic is almost as informative as h_{sa} , yet computable as quickly as h_{add} .

Note: Our presentation inverts the historical order. The set-additive heuristic was defined after the FF heuristic (sacrificing speed for even higher informativeness).

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FF heuristic: fitting the template



The FF heuristic h_{FF} Computing annotations:

Annotations are Boolean values, computed top-down.

A node is marked when its annotation is set to 1 and unmarked if it is set to 0. Initially, the goal node is marked, and all other nodes are unmarked.

We say that a true AND node is justified if all its true successors are marked, and that a true OR node is justified if at least one of its true successors is marked.

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FF heuristic: fitting the template (ctd.)

The FF heuristic h_{FF} (ctd.) Computing annotations:

. . . .

Apply these rules until all marked nodes are justified:

- Mark all true successors of a marked unjustified AND node.
- 2 Mark the true successor of a marked unjustified OR node with only one true successor.
- Mark a true successor of a marked unjustified OR node connected via an idle arc.
- 4 Mark any true successor of a marked unjustified OR node.

The rules are given in priority order: earlier rules are preferred if applicable.

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h_{add}
h_{sa}

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Summary

FF heuristic: fitting the template (ctd.)

The FF heuristic h_{FF} (ctd.)

Termination criterion:

Always terminate at first layer where goal node is true.

Heuristic value:

■ The heuristic value is the number of operator/effect condition pairs for which at least one effect node is marked.

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n_{sa}
Incremental
computation

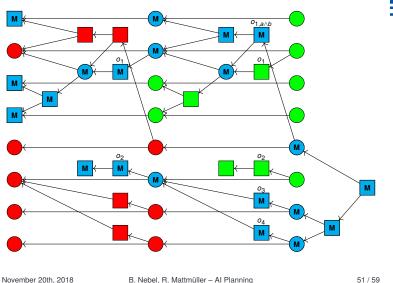
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Running example: *h*_{FF}



Remarks on *h*_{FF}



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- Like h_{add} and h_{sa} , h_{FF} is safe and goal-aware, but neither admissible nor consistent.
- Its informativeness can be expected to be slightly worse than for h_{sa} , but is usually not far off.
- Unlike h_{sa} , h_{FF} can be computed in linear time.
- Similar to h_{sa} , the operators corresponding to the marked operator/effect condition pairs define a relaxed plan.
- Similar to *h*_{sa}, the *h*_{FF} value depends on tie-breaking when the marking rules allow several possible choices, so *h*_{FF} is not well-defined without specifying the tie-breaking rule.
 - The implementation in FF uses additional rules of thumb to try to reduce the size of the generated relaxed plan.

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Comparison of relaxation heuristics

Theorem (relationship between relaxation heuristics)

Let s be a state of planning task $\langle A, I, O, \gamma \rangle$. Then:

- $h_{max}(s) \le h^+(s) \le h^*(s)$
- $\blacksquare h_{max}(s) \leq h^+(s) \leq h_{sa}(s) \leq h_{add}(s)$
- $\blacksquare h_{max}(s) \leq h^+(s) \leq h_{FF}(s) \leq h_{add}(s)$
- \blacksquare h^* , h_{FF} and h_{sa} are pairwise incomparable
- \blacksquare h^* and h_{add} are incomparable

Moreover, h^+ , h_{max} , h_{add} , h_{sa} and h_{FF} assign ∞ to the same set of states.

Note: For inadmissible heuristics, dominance is in general neither desirable nor undesirable. For relaxation heuristics, the objective is usually to get as close to h^+ as possible.

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Relaxation

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h_{add} h_{sa}

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Comparison & practice

Summar

Literature: Bonet, Loerincs & Geffner (1997), Bonet & Geffner (2001)

Relaxation heuristics in practice: HSP



Example (HSP)

HSP (Bonet & Geffner) was one of the four top performers at the 1st International Planning Competition (IPC-1998).

Key ideas:

- \blacksquare hill climbing search using h_{add}
- on plateaus, keep going for a number of iterations, then restart
- use a closed list during exploration of plateaus

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Relaxation heuristics in practice: FF



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Example (FF)

FF (Hoffmann & Nebel) won the 2nd International Planning Competition (IPC-2000).

Key ideas:

- enforced hill-climbing search using her
- helpful action pruning: in each search node, only consider successors from operators that add one of the atoms marked in proposition layer 1
- goal ordering: in certain cases, FF recognizes and exploits that certain subgoals should be solved one after the other

If main search fails, FF performs greedy best-first search using $h_{\rm FF}$ without helpful action pruning or goal ordering.

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Relaxation heuristics in practice: Fast Downward



Example (Fast Downward)

Fast Downward (Helmert & Richter) won the satisficing track of the 4th International Planning Competition (IPC-2004).

Key ideas:

- \blacksquare greedy best-first search using h_{FF} and causal graph heuristic (not relaxation-based)
- search enhancements:
 - multi-heuristic best-first search
 - deferred evaluation of heuristic estimates
 - preferred operators (similar to FF's helpful actions)

Literature: Helmert (2006)

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Relaxation heuristics in practice: SGPlan



Example (SGPlan)

SGPlan (Wah, Hsu, Chen & Huang) won the satisficing track of the 5th International Planning Competition (IPC-2006).

Key ideas:

- problem decomposition techniques
- domain-specific techniques

Literature: Chen, Wah & Hsu (2006)

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Relaxation heuristics in practice: LAMA



Example (LAMA)

LAMA (Richter & Westphal) won the satisficing track of the 6th International Planning Competition (IPC-2008).

Kev ideas:

- Fast Downward
- landmark pseudo-heuristic instead of causal graph heuristic ("somewhat" relaxation-based)
- anytime variant of Weighted A* instead of greedy best-first search

Literature: Richter, Helmert & Westphal (2008), Richter & Westphal (2010)

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Summary

- UNI FREIBURG
- Relaxed planning graphs are AND/OR dags. They encode which propositions can be made true in Π^+ and how.
 - Closely related to forward sets and forward plan steps, based on the notion of parallel relaxed plans.
 - They can be constructed and evaluated efficiently, in time $O((m+1)||\Pi^+||)$ for planning task Π and depth m.
- By annotating RPG nodes with appropriate information, we can compute many useful heuristics.
- Examples: max heuristic h_{max} , additive heuristic h_{add} , set-additive heuristic h_{sa} and FF heuristic h_{FF}
 - Of these, only h_{max} admissible (but not very accurate).
 - The others are much more informative. The set-additive heuristic is the most sophisticated one.
 - The FF heuristic is often similarly informative. It offers a good trade-off between accuracy and computation time.

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