

# Principles of AI Planning

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## Exercise Sheet 10

**Due: Friday, January 16th, 2015**

### Exercise 10.1 (LM-cut heuristic, 5 points)

Consider the STRIPS planning task specified by  $\Pi = \langle A, I, O, \gamma \rangle$ , where

$$\begin{aligned}A &= \{s, b, c, d, e, t\} \\I &= \{s \mapsto 1, b \mapsto 0, c \mapsto 0, d \mapsto 0, e \mapsto 0, t \mapsto 0\} \\O &= \{o_i \mid 1 \leq i \leq 6\} \\o_1 &= \langle s, b \wedge c \rangle \\o_2 &= \langle b, d \rangle \\o_3 &= \langle c, e \rangle \\o_4 &= \langle d \wedge e, t \rangle \\o_5 &= \langle c \wedge e, t \rangle \\o_6 &= \langle e, s \rangle \\\gamma &= t\end{aligned}$$

Compute  $h_{\text{LM-cut}}(I)$ . In each iteration  $i$  of the algorithm (except for the last iteration where you identify  $h_{\text{max}}^c(t) = 0$ ), give the respective **pcf**  $D_i$ , the corresponding **justification graph**  $G_i$  of  $D_i$ , the **sets**  $V_i^*$ ,  $V_i^0$ ,  $V_i^b$  and  $L_i$  as well as the (intermediate) **heuristic value**.

For the sake of a unique solution, please break possible pcf ties in favor of proposition  $e$  in operators  $o_4$  and  $o_5$ .

*Hints:* When constructing an  $s$ - $t$ -cut, please keep the definition in mind (simply drawing a line through the graph may yield wrong results). Furthermore, a justification graph can contain multiple parallel edges as well as cycles, although the first example in the lecture did not.

### Exercise 10.2 (Active operators and projections, 2+3 points)

Let  $\Pi = \langle V, O, I, \gamma \rangle$  be a SAS+ planning task without trivially inapplicable operators and let  $s$  be a state of  $\Pi$ . Show that the set of active operators  $Act(s) \subseteq O$  in  $s$  can be identified efficiently by considering paths in the projection of  $\Pi$  onto  $v$ :

- Establish and prove a connection between the projection of  $\Pi$  onto  $v$  and the domain transition graph of  $v$ .
- Specify an efficient algorithm for the identification of  $Act(s)$ , prove its soundness and completeness, and reason about the runtime of the algorithm in terms of the input size.

You can and should solve the exercise sheets in groups of two. Please state both names on your solution.