Principles of Knowledge Representation and Reasoning

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Exercise Sheet 14 Due: February 13th, 2013

Exercise 14.1 (POINT ALGEBRA, 1+1)

Let $B = \{<, =, >\}$ be the point algebra base relations. In the following we interpret them over the set of integers \mathbb{Z} . Prove:

- (a) The set B is not closed under composition.
- (b) Any superset of relations $A' \supseteq B$ that is closed under composition is infinite.

Exercise 14.2 (PATH CONSISTENCY, 3+1+1)

Consider the following constraint network over the point algebra:



The constraints are thus $x_1 \leq x_2$, $x_1 > x_4$, $x_1 < x_3$, and $x_3 \geq x_4$.

- (a) Apply the path consistency algorithm to the network using the composition/converse table.
- (b) Provide a solution for the network assuming domain \mathbb{Q} .
- (c) Is there a non-empty domain for which the network has no solution?

Exercise 14.3 (DIRECTION RELATIONS, 1+4)

Consider the following five *direction relations* for points in the Euclidean plane \mathbb{R}^2 :

- *a* I *b*, if *a* and *b* denote the same point.
- $a \ge b$, if a is north of b.
- $a \to b$, if a is east of b.
- $a \le b$, if a is south of b.
- $a \le b$, if a is west of b.

We interpret these relations as given in Figure 1; for any two points we assign the most appropriate relation, that is, a point x is considered to be north of point y if it is more to the north than to the east, west, or south. Points that are exactly located on a line in Figure 1 are considered to be N in the upper half-plane and S in the lower half-plane.

From these five relations $\mathcal{A}=\{I,N,E,S,W\}$ we obtain a JEPD relation system closed under converse.



Figure 1: Direction relations in the Euclidean plane.

- (a) Provide a formal definition for each of the five relations in \mathcal{A} .
- (b) Provide a composition table for the five relations of \mathcal{A} .