







rather than 'balance of nature'.

- More wolves
- ... leads to less moose
- ... leads to less wolves
- … leads to more moose.

Wolves and Moose: Classical Model

Lotka-Volterra model for wolf (w) and moose (m) populations:

$$\frac{\delta m}{\delta t} = k_1 m - k_2 wm, \frac{\delta w}{\delta t} = -k_3 w + k_4 k_2 wm$$



Discussion: Pros and Cons

Differential Equations

- Pro: Mathematically well understood, analytical inference by using calculus, many tools available (e.g., Matlab)
- Con: Hard to explain, models phenomenon rather than behavior, harder to extend

Agent-Based Model

- Pro: Easy to understand and to explain to stakeholders, models individual beahvior and observes emergent phenomenon, easy to extend
- Con: Tool support improves slowly, no analytical tools comparable to calculus



Nebel, Lindner, Engesser - MAS

6 / 20



BURG

UNI REI

UNI FREIBURG

Nagel-Schreckenberg Model: Motivation



9 / 20

- Research Question: How do traffic jams emerge?
- Research Hypothesis: Might be due to the local behaviour of individual agents.
- Approach: Model traffic as a MAS and study the resulting system's behavior. If the systems' behavior matches empirical phenomenon, then the model might be an acceptable explanation.

Nebel, Lindner, Engesser - MAS





- Overreaction when braking
- Car motion: Move forward v cells.

Nebel, Lindner, Engesser - MAS









Nagel-Schreckenberg: Density and Flow



- Assume constant system density: $\rho = \frac{|Ag|}{|B|}$
- For a fixed cell *c_i*, time-averaged density over time interval *T*:

$$\bar{\rho}^{T} = \frac{1}{T} \sum_{t=t_{0}+1}^{t_{0}+T} n_{i}(t)$$

- ... with $n_i(t) = 1$ if *i* is occupied, else $n_i(t) = 0$
- Time-averaged flow \bar{q} between *i* and *i* + 1:

$$\bar{q}^{T} = \frac{1}{T} \sum_{t=t_{0}+1}^{t_{0}+T} n_{i,i+1}(t)$$

- ... with $n_{i,i+1}(t) = 1$ if some car moved between *i* and *i* + 1 at *t*, else $n_{i,i+1}(t) = 0$
 - Nebel, Lindner, Engesser MAS

17 / 20





