

## Multiagent Systems

Prof. Dr. B. Nebel

Dr. C. Becker-Asano, Dr. S. Wölfl, A. Hertle  
Summer term 2014

University of Freiburg

Department of Computer Science

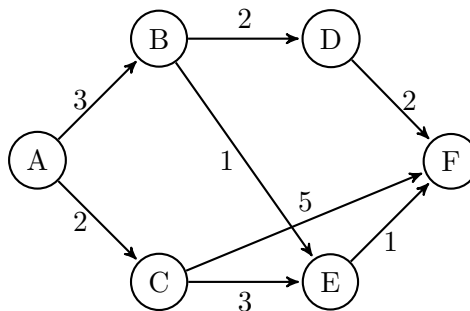
### Exercise Sheet 10

**Due: Friday, July 25, 2pm**

**Important:** Each exercise sheet is to be solved in groups of **two students**. Thus, please note your names on each solution sheet and, if applicable, in the source code (as a comment on top of each source file). The solutions are to be handed in as pdf or plain text files (UTF-8 encoded) using the SVN. We strongly suggest the use of L<sup>A</sup>T<sub>E</sub>X for typesetting your solutions. As always so far, you might solve the exercises in English or German.

#### Exercise 10.1 (VCG mechanism, 1+2+2 points)

Consider the problem of buying the shortest path in a transportation network (see Shoham and Leyton-Brown, p. 281). The transportation network is given by the following directed graph:



The numbers on the edges of this graph denote the agents' costs  $c$  for traversing the edge from one node to the other in the given direction. Thus, an agent's utility is  $-c$  if a route involving the edge with cost  $c$  is selected, and zero otherwise. In other words, the agent "sitting" on the edge would be paid the amount  $c$  for traversing its edge.

The cheapest route to get from  $A$  to  $F$  is clearly  $ABEF$  with a total cost of  $3 + 1 + 1 = 5$ . But how much would we have to pay each agent according to the VCG mechanism?

An example: The agent  $AC$  (owning the edge between the nodes  $A$  and  $C$ ) is not pivotal to the shortest/cheapest path  $ABEF$ . Taking his declaration  $c(AC) = 2$  into account leads to a cost of  $-5$  for the other agents, because the path does not involve him anyways. Likewise the shortest/cheapest path without  $AC$ 's declaration has cost  $-5$ . Thus, agent  $AC$  has not to pay (or gains) nothing, as  $(-5) - (-5) = 0$ .

- (a) Which of the agents are pivotal and how is each of them to be paid? Explain your calculations step by step for each agent.
- (b) The edges  $BE$  and  $EF$  both incur a cost of 1. However, the corresponding two agents do not receive the same amount of reward according to the VCG mechanism. Explain what that means.
- (c) How would the situation change, if the edge  $EF$  had a cost of 4 instead of 1? Calculate all payments of all agents again and discuss your result.

**Exercise 10.2** (Bargaining, 1+4 points)

Consider the following Task Oriented Domain:

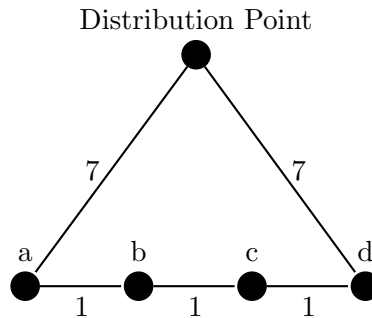
*Description:* Agents have to deliver sets of containers to warehouses, which are arranged on a weighted graph  $G = G(V, E)$ . There is no limit to the number of containers that can fit in a warehouse. The agents all start from a central distribution point. Agents can exchange containers at no cost while they are at the distribution point, prior to delivery.

*Task Set:* The set of all addresses in the graph, namely  $V$ . If address  $x$  is in an agent's task set, it means that it has least one container to deliver to  $x$ .

*Cost Function:* The cost of a subset of addresses  $X \subseteq V$ , i.e.,  $c(X)$ , is the length of the minimal path that starts at the distribution point and visits all members of  $X$ .

We now consider a concrete example:

The reachability between warehouses  $a, b, c, d$  together with their reachability costs are given by the following undirected graph:



Two agents  $A_1$  and  $A_2$  start at the delivery point and both have to deliver boxes to warehouses  $a, b, c$  and  $d$ .

- (a) Which value would  $A_1$ 's utility have, if  $A_2$  agreed to also take  $A_1$ 's boxes to the warehouses? Explain.
- (b) Apply the Zeuthen strategy for both agents as the negotiation strategy and explain the outcome as compared to the maximum overall utility.