Constraint Satisfaction Problems

B. Nebel, S. Wölfl, J. Hué M. Westphal Sommersemester 2012 University of Freiburg Department of Computer Science

Exercise Sheet 8 Due: Monday 02.07.2012

Exercise 8.1 (6 Points)

Let $N = \langle (v_1, ..., v_8), (D_1, ..., D_8), C \rangle$ with

• $D_1 = D_8 = \{1\},$

• $D_2 = \{2, 3\},$

• $D_3 = \{0\},$

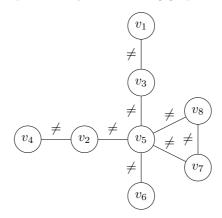
• $D_4 = \{3\},$

• $D_5 = \{1, 2\},$

• $D_6 = \{3, 4\},$

• $D_7 = \{0, 1\}.$

The constraints C are provided by the following graph:



In the following use lexicographic orderings, i.e., the variable ordering $v_1 \prec v_2 \prec \cdots \prec v_8$ and for value ordering $0 \prec 1 \prec \cdots \prec 4$. Do not use any look-ahead strategies.

It is sufficient to provide the *jumps* and the identified *internal* and *leave dead* ends in the order they appear during search.

- (a) Apply backtracking search with Gaschnig's Backjumping to N.
- (b) Apply backtracking search with Conflict-Directed Backjumping to N. Provide the jump-back sets where used.

Exercise 8.2 (2 Points)

Prove that Conflict-Directed Backjumping only performs safe jumps.

Exercise 8.3 (2 Points)

Show that jumping back further than the culprit variable for Gaschnig's Back-jumping is incorrect. To this end, let (a_1,\ldots,a_i) be a leaf dead-end, v_b its culprit variable, and construct an example where jumping back to (a_1,\ldots,a_j) , j < b skips solutions.