

Exercise 7

To be returned on Monday, June 28, 2004

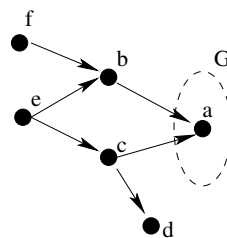
Assignment 7.1

Consider the procedure *prune* (from the lecture notes, with numbering for S and W corresponding to the iterations).

```

procedure prune( $O, W, G$ );
 $i := 0$ ;
 $W_0 := W$ ;
repeat
   $i := i + 1$ ;
   $k := 0$ ;
   $S_0 := G$ ;                                (* States from which  $G$  is reachable with 0 steps. *)
  repeat
     $k := k + 1$ ;                             (* States from which  $G$  is reachable with  $k$  steps. *)
     $S_k := S_{k-1} \cup \bigcup_{o \in O} (wpreimg_o(S_{k-1}) \cap spreimg_o(W_{i-1}))$ ;
  until  $S_k = S_{k-1}$ ;                       (* States that stay within  $W_{i-1}$  and eventually reach  $G$ . *)
   $W_i := W_{i-1} \cap S_k$ ;
until  $W_i = W_{i-1}$ ;                       (* States in  $W_i$  stay within  $W_i$  and eventually reach  $G$ . *)
return  $W_i$ ;
    
```

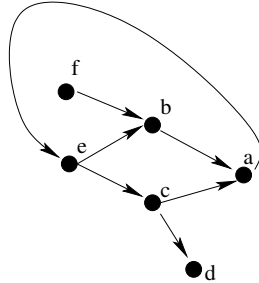
Consider the following transition graph (only one action o , which is nondeterministic in states e and c .)



Simulate the computation of *prune* when it is called with the following parameters: $\text{prune}(\{o\}, \{a, b, c, d, e, f\}, \{a\})$. List the values of S_k and W_i for different values of k and i .

Assignment 7.2

Simulate the computation of the algorithm for maintenance goals for the following graph (there is only one action) and $G = \{a, b, c, d, e, f\}$.



Assignment 7.3

1. Let there be 3 state variables A , B and C . Construct the transition matrix of the probabilistic operator

$$\langle B \rightarrow C, 0.5(A \triangleright B) | 0.5(0.5(B \triangleright C) | 0.5(A \triangleright C)) \rangle.$$

2. Outline an algorithm that constructs from any transition matrix a corresponding operator (assume that rows and columns correspond to valuations of state variables x_1, \dots, x_n for some n).

A brief outline of the idea of how the algorithm works suffices.

*You may work on these assignments and submit your results **in groups of two students**. Make sure to clearly indicate both names on your work. **You may write your answers in English or German.***