

Multi-Agent Systems

Agent-Based Modelling and Simulation

Albert-Ludwigs-Universität Freiburg



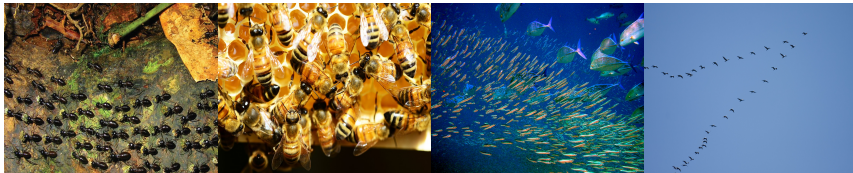
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- 1 So far, we studied small groups of agents, which were all rational/intelligent.
 - 2 We considered how to model communication and cooperation.
 - 3 What if we have **very large** groups of agents (> 100000)?
 - 4 What if we are interested in **emerging phenomena**?
- ~> Agent-based modelling and simulation

How much can a group of **simple reflex agents** can achieve?



- Swarm formation control: How to design programs that result into a particular swarm formation when executed on each simple reflex agent. [Video: EPFL Formation](#)



- Problem
 - Form an approximation of a simple geometric object (shape)
 - Problem not yet solved in general!
 - Algorithms exist that make simplifying assumptions about the agents' capabilities and the shape.
- Assumptions shared by the algorithms proposed by Sugihara & Suzuki (1996)
 - Each robot can see all the other robots
 - Shapes are connected
 - But ...
 - Total number of robots unknown
 - No common frame of reference (i.e., one cannot program the robots "to meet at point (X, Y) " or "to move north")
 - robots cannot communicate with each other
 - Local decision making



- **Problem:** Move a group of robots such that they will eventually approximate a circle of a given diameter D .

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- **Algorithm** [Sugihara & Suzuki, 1996]: The robot R continuously monitors the position of a farthest robot R_{far} and a nearest robot R_{near} , and the distance d between R (itself) and R_{far} .
 - 1 If $d > D$, then R moves towards R_{far}
 - 2 If $d < D - \delta$, then R moves away from R_{far}
 - 3 If $D - \delta \leq d \leq D$, then R moves away from R_{near}



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- **Algorithm** [Sugihara & Suzuki, 1996]:
 - 1 Run the CIRCLE algorithm until each robot R can recognize its immediate left neighbor $l(R)$ and right neighbor $r(R)$.
 - 2 Selection of n robots to be the vertices of the n -sided polygon.
 - 3 All robots R execute the CONTRACTION algorithm
 - 1 Continuously monitor the position of $l(R)$ and $r(R)$
 - 2 Move toward the midpoint of the segment $\overline{l(R)r(R)}$



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- **Algorithm** [Sugihara & Suzuki, 1996]: First n robots are picked as vertices of the polygon and moved to the desired position. All other robots R execute FILLPOLYGON:
 - 1 If, as seen from R , all other robots lie in a wedge whose apex angle is less than π , then R moves into the wedge along the bisector of the apex.
 - 2 Otherwise, R moves away from the nearest robot.



- Simple reflex agent's do not make use of memory. This can be a severe limitation:
 - Imagine you are at a crossing and you have to decide to either go left or right. You go left and find out it's a dead end. You return to the crossing. Again, you have the choice between going left and going right ...
 - Possible solutions:
 - Change the environment (pheromones, bread crumbs)
 - Put your previous actions and experiences into your memory

function REFLEX-AGENT-WITH-STATE(*percept*)

global rules, state

state ← UPDATE-STATE(*state, percept*)

rule ← RULE-MATCH(*state, rules*)

action ← RULE-ACTION(*rule*)

state ← UPDATE-STATE(*state, action*)

return *action*

end function

- Internal state is updated over time (takes both state and percept into account and thus can also update currently unobserved aspects).
- Practical reasoning is based on rules applied in this state and leads to another state update.

Definition (Wilensky & Rand, 2015)

Agent-based modeling is a form of computational modeling whereby a phenomenon is modeled in terms of agents and their interactions.

- Agents are entities that have state variables and values (e.g., position, velocity, age, wealth)
 - Gas molecule agent: mass, speed, heading
 - Sheep agent: speed, weight, fleece
- Agents also have rules of behavior
 - Gas molecule: Rule to collide with another molecule
 - Sheep: Rule to eat grass
- Universal clock: At each tick, all agents invoke their rules.

The populations of wolves and moose of Isle Royale have been observed for more than 50 years. Result: Dynamic variation rather than 'balance of nature'.

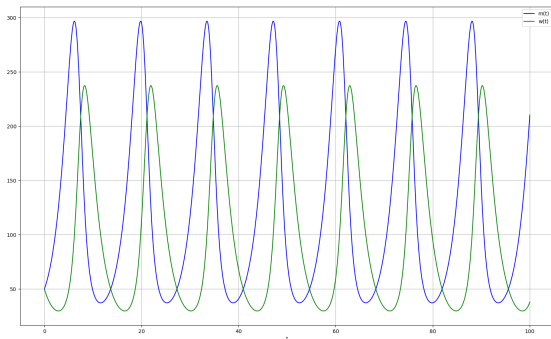
- More wolves
- ... leads to less moose
- ... leads to less wolves
- ... leads to more moose.

Wolves and Moose: Classical Model



Lotka-Volterra model for wolf (w) and moose (m) populations:

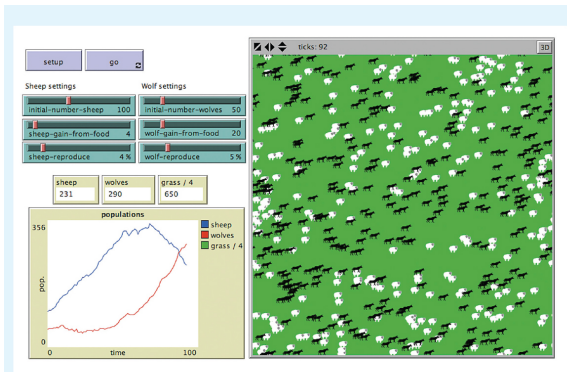
$$\frac{dm}{dt} = c_1 m - c_2 w m, \quad \frac{dw}{dt} = -c_3 w + c_4 w m$$



Wolves and Moose: Agent-Based Model



- Spawn m moose and w wolves and invoke each agent's behavior in each loop:
 - ask moose [move death reproduce-sheep]
 - ask wolves [move set energy energy - 1 catch-sheep death reproduce-wolves]





Differential Equations

Agent-Based Model

Differential Equations

- Pro: Mathematically well understood, analytical inference by using calculus, many tools available (e.g., Matlab)
- Con: Hard to explain, models phenomenon rather than behavior, harder to extend

Agent-Based Model

- Pro: Easy to understand and to explain to stakeholders, models individual behavior and observes emergent phenomenon, easy to extend
- Con: Tool support improves slowly, no analytical tools comparable to calculus

- Observation: Traffic on the motorway produces certain patterns.
- Question: Can similar patterns be algorithmically reproduced?
- Agent-Based Simulation approach:
 - Modeling traffic on the motorway as a multi-agent system
 - Cars (drivers) as agents
 - Percepts: Distance to next car in front
 - Internal State: Current Speed
 - Actions: Speeding, braking



- **Research Question:** How do traffic jams emerge?
- **Research Hypothesis:** Might be due to the local behaviour of individual agents.
- **Approach:** Model traffic as a MAS and study the resulting system's behavior. If the systems' behavior matches empirical phenomenon, then the model might be an acceptable explanation.

- A **cellular automaton** is a quad-tuple $A = \langle R, Q, N, \delta \rangle$
- A **cell space** R
- A set Q of **states** each cell can be in
- A **neighborhood** $N : R \rightarrow 2^R$
- A **transition function** $\delta : Q^{|N|} \rightarrow Q$
 - For a probabilistic cellular automaton, δ is a probability distribution $P(r = q | N(r))$
- The **configuration** of A can be written as $x_1 x_2 \dots x_n$ with x_i being the state of the cell r_i .



- Traffic is modeled as $A = \langle R, Q, N, \delta \rangle$
- Entities of $R = \{c_1, c_2, \dots\}$ stand for parts of the lane
 - Each cell corresponds to a discrete part of the lane (roughly the space needed by a car)
- $Q = \{0, \dots, v_{max}, free\}$: Each cell is either occupied by one car with velocity $v \leq v_{max}$, or it is empty.
- $N(c_i) = \{c_{i-v_{max}}, \dots, c_{i+1}\}$
- δ is realized by a set of four rules executed by each driver

- Each car at cell c_i with velocity v performs four consecutive steps:
 - **Acceleration:** If $v < v_{max}$ and gap to next car is larger than $v + 1$, then increment speed by 1.
 - **Slowing down:** If the next car is at cell $i + j$ with $j \leq v$, then reduce speed to $j - 1$.
 - **Randomization:** If $v > 0$, then decrement v by 1 with probability p .
 - Car does not accelerate although it could (takes back **Acceleration**)
 - Car reached maximal velocity but slows down again
 - Overreaction when braking
 - **Car motion:** Move forward v cells.

Nagel-Schreckenberg: Example



2 _ _ 2 _ _ 2 _ _
_ _ _ _ _ _ _ _
_ _ _ _ _ _ _ _
_ _ _ _ _ _ _ _
_ _ _ _ _ _ _ _

Nagel-Schreckenberg: Example



2 _ _ 2 _ _ 2 _ _
_ _ 2 _ _ 2 _ _ 2
_ 2 _ _ 2 1 _ _

Nagel-Schreckenberg: Example



2	_	_	2	_	_	2	_	_
_	_	2	_	_	2	_	_	2
_	2	_	_	2	1	_	_	_
_	_	_	2	0	_	_	_	2

Nagel-Schreckenberg: Example



2	_	_	2	_	_	2	_	_
_	_	2	_	_	2	_	_	2
_	2	_	_	2	1	_	_	_
_	_	_	2	0	_	_	_	2
_	2	_	0	_	1	_	_	_

- Assume constant **system density**: $\rho = \frac{|Ag|}{|R|}$
- For a fixed cell c_i , **time-averaged density** over time interval T :

$$\bar{\rho}^T = \frac{1}{T} \sum_{t=t_0+1}^{t_0+T} n_i(t)$$

- ...with $n_i(t) = 1$ if i is occupied, else $n_i(t) = 0$
- **Time-averaged flow** \bar{q} between i and $i + 1$:

$$\bar{q}^T = \frac{1}{T} \sum_{t=t_0+1}^{t_0+T} n_{i,j+1}(t)$$

- ...with $n_{i,j+1}(t) = 1$ if some car moved between i and $i + 1$ at t , else $n_{i,j+1}(t) = 0$

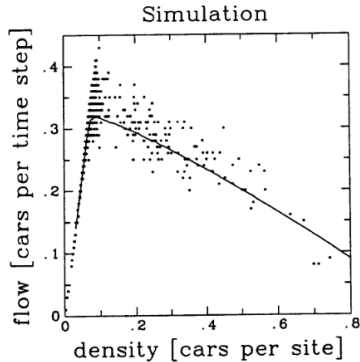


Fig.: Source: [2]

Netlogo simulation

- 1 Can you do more than giving nice visualizations?
- 2 Vary parameters, do sensitivity analysis!
- 3 Make detailed models and try to answer **what-if** questions, e.g. what happens if we introduce different airport signage
- 4 What happens if we introduce new economic tools such as basic income?

1 NetLogo

- Simple, easy to learn and to use
- Implemented in Java
- Scalability issues

2 Repast Symphony

- More complex, more difficult to learn
- Java-based (comes with Eclipse IDE)
- Includes 3D GIS model
- Scalable for complex models
- HPC version

3 FLAME

- Automata-based, using XML and C, difficult to learn
- Scalable for very large models, HPC support
- Used for some elaborate economic models

4 ...

- 1 Agent-based modelling and simulation helps to model large systems of agents (comparatively stupid ones, though)
- 2 Can be used
 - to explore emergent phenomena
 - to predict behaviour based on parameter changes (sensitivity analysis!)
 - can answer what-if question when environment should be changed
- 3 There exists a number of different ABS frameworks
- 4 Interesting question: Can the incorporation of more intelligence lead to qualitatively different system behaviour?



U. Wilensky, W. Rand, *An Introduction to Agent-Based Modeling*, MIT Press, ISBN: 9780262731898, 2015.



K. Nagel, M. Schreckenberg (1992), A cellular automaton model for freeway traffic, *J. Phys. I France* 2, pp. 2221–2229.