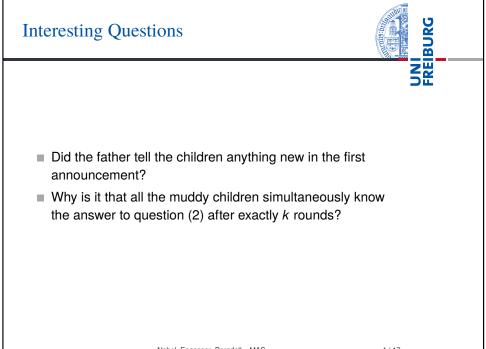


UNI FREIBURG Recap Last session: Axioms of epistemic/doxastic logic, group knowledge (common knowledge, distributed knowledge). Today: Modeling changes of knowledge due to public communication and observations (muddy children puzzle). Nebel, Engesser, Bergdoll - MAS 2/17



Base Case I

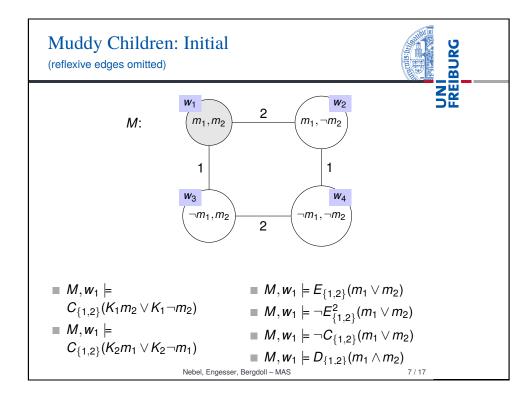


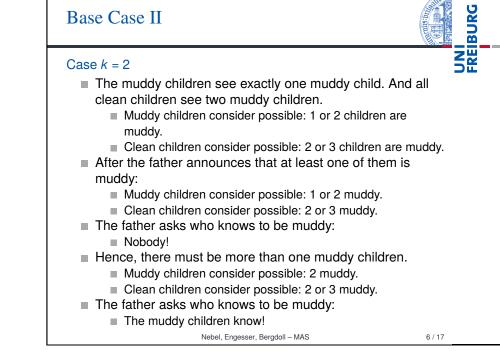
Case k = 1

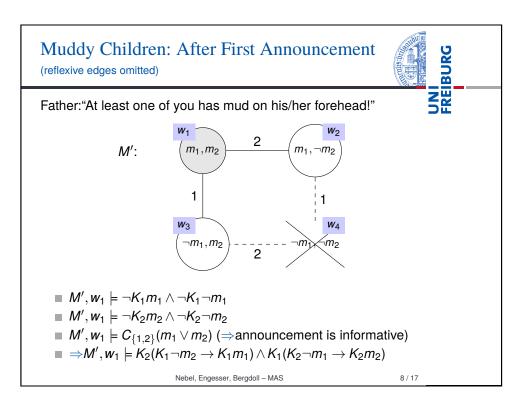
- The muddy child only sees clean children. And all clean children see one muddy child.
 - Muddy child considers possible: 0 or 1 children are muddy.
 - Clean children consider possible: 1 or 2 children are muddy.
- After the father announces that at least one of them is muddy:
 - Muddy child considers possible: 1 muddy.
 - Clean children consider possible: 1 or 2 muddy.
- The father asks who knows to be muddy:
 - Muddy child knows!

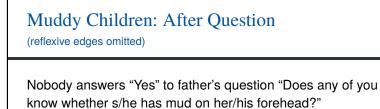
Nebel, Engesser, Bergdoll - MAS

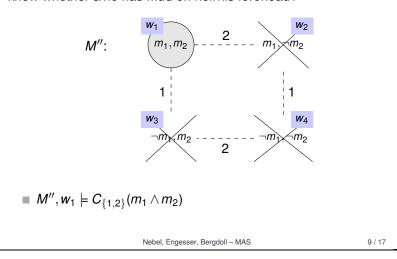
5/17



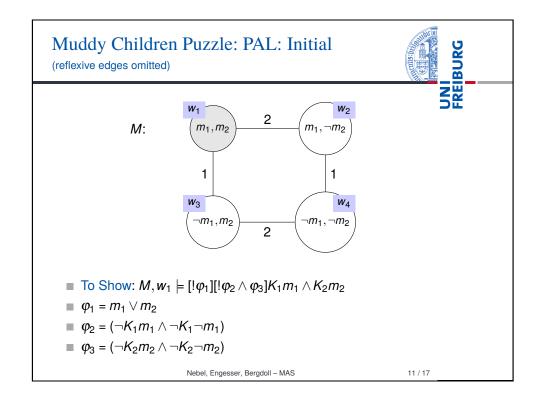




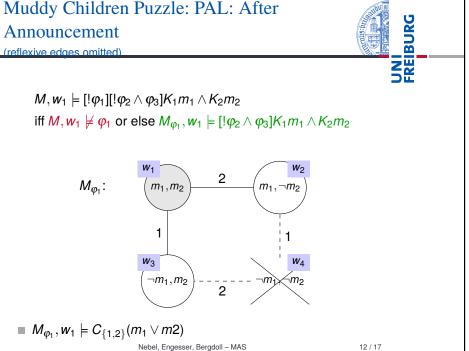




UNI FREIBURG



Public Announcement Operator	BURG
	LUN NO
$[! \varphi] \psi$: "After φ has been truthfully announced, ψ is the case."	
Semantics	
$M, w \models [! \varphi] \psi$ iff $M, w \not\models \varphi$, or else $M_{\varphi}, w \models \psi$	
■ M_{φ} is the relativation of M to the worlds where φ holds. The model $M_{\varphi} = (S', R', V')$ is given as follows:	
\mathcal{S}' = { $w \in \mathcal{S}$: $M, w \models \phi$ }	(1)
$R' = R _{S' imes S'}$	(2)
$V'(p)$ = $V(p) \cap S'$	(3)
Nebel, Engesser, Bergdoll – MAS	10 / 17
Muddy Children Puzzle: PAL: After	SUBVER .



Muddy Children Puzzle: PAL: After Question (reflexive edges omitted)

