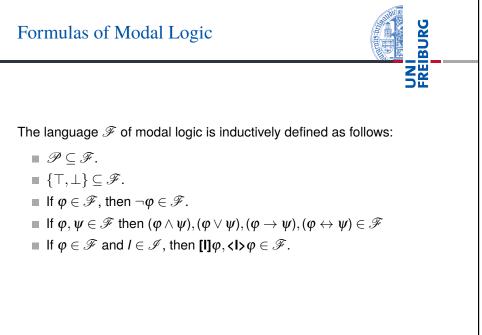




Overview		
5		
Belief, Desire, Obligation graphical models. Kripke models formalize By constraining the access	omains (Programs, Knowled ) can nicely be modeled usin graphical models. ssibility relations of Kripke fr prrespond to above concepts	ames
	ages to talk about Kripke mo Knowledge, Belief, Desire,	odels
Μ	lodal Logics	
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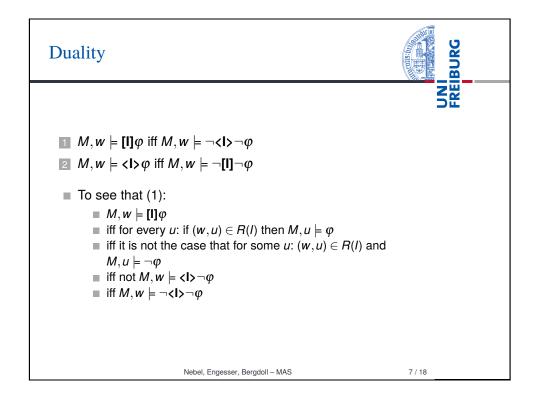
## Different Variants of Languages

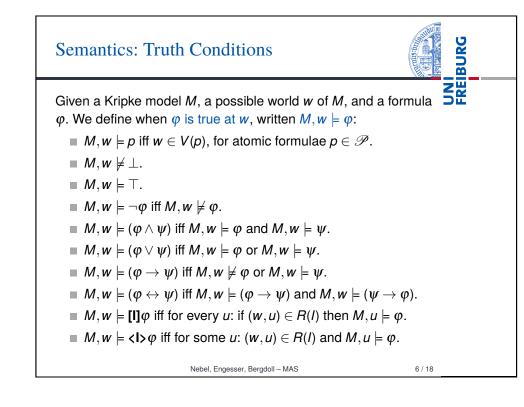


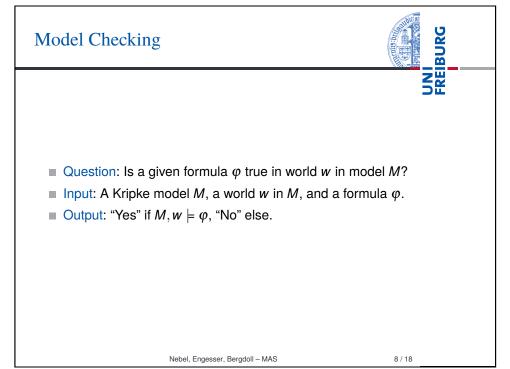
- Alethic logic (Necessity): □, ◇
- Epistemic logic (Knowledge): K, K
- Doxastic logic (Belief): B, B
- Deontic logic (Obligation): O, P
- Multi-Agent Epistemic logic: Agent name as subscript, e.g., K<sub>mary</sub> K̂<sub>john</sub>sun\_shining
- Notation: Sometimes, we will decide that [I] shall be read in context of epistemic logic, sometimes we will decide to read it in context of deontic logic. We then may also sometimes write K<sub>I</sub> (i.e., Agent I knows), and O<sub>I</sub> (i.e., Agent I ought to) instead of [I].

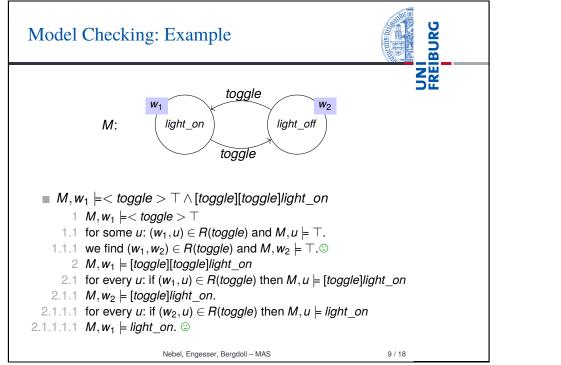
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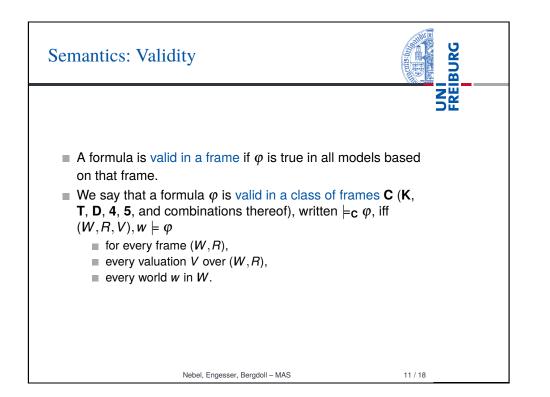
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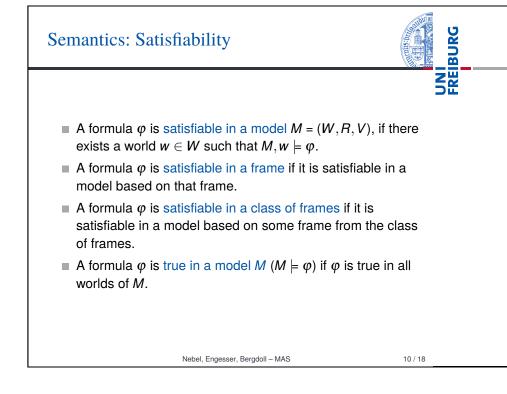


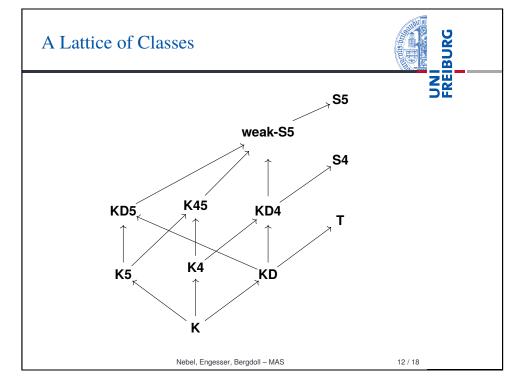












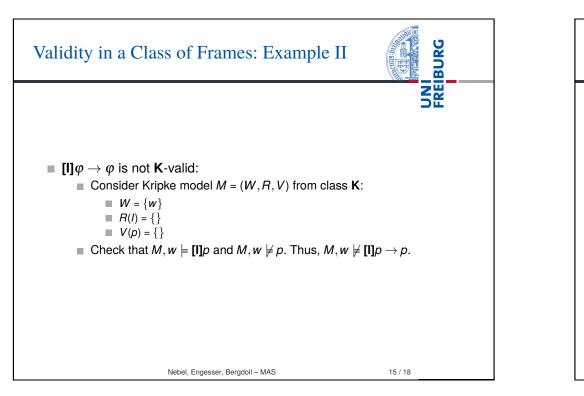
## Validity in a Class of Frames

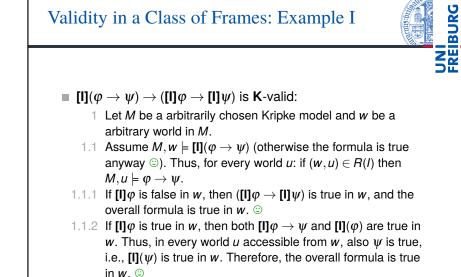


- Valid formulas give us an idea of how the classes differ, and thus what is and is not specific to the general behavior of our modalities (Knowledge, Belief, Obligation etc.).
- Correspondences between classes of frames and formulas
  - **[I]** $(\phi \rightarrow \psi) \rightarrow ([I]\phi \rightarrow [I]\psi)$  (for every formulae  $\phi, \psi$ ) is **K**-valid (valid in the class of all frames)
  - **[I]** $\phi \rightarrow \phi$  (for every formulae  $\phi$ ) is **T**-valid (exactly valid in the class of reflexive frames)
  - **[I]** $\phi \rightarrow \langle I \rangle \phi$  (for every formulae  $\phi$ ) is **D**-valid (exactly valid in the class of serial frames)
  - **[I]** $\phi \rightarrow$ **[I][I]** $\phi$  (for every formulae  $\phi$ ) is **4**-valid (exactly valid in the class of transitive frames)
  - $\langle I \rangle \phi \rightarrow [I] \langle I \rangle \phi$  (for every formulae  $\phi$ ) is 5-valid (exactly valid in the class of Euclidean frames)

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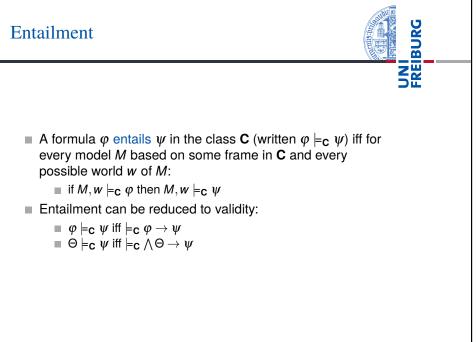
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## Reducing Validity to Satisfiability



- The validity problem can be reduced to the satisfiability problem:
  - Instead of asking whether φ is true in all worlds in all Kripke models in a class, we can ask if ¬φ is true in some world in some Kripke model in the class.
- Problem formulation:
  - Input: A formula  $\varphi$ .
  - Output: "Yes" if there is a Kripke model *M* and a world *w* of *M* such that  $M, w \models \varphi$ , "No" otherwise.
- It turns out that we can systematically search for Kripke models that satisfy some formula. With this tool at hand, we can algorithmically decide validity.

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