Principles of AI Planning

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Exercise Sheet 5 Due: Friday, November 23th, 2018

Send your solution to drexlerd@tf.uni-freiburg.de or submit a hardcopy before the lecture.

Exercise 5.1 (Delete relaxation, 2+2 points)

Consider the planning task $\Pi = \langle A, I, O, \gamma \rangle$ in positive normal form with

 $A = \{haveCake, eatenCake, haveNoCake\},$

 $I = \{have\text{-}cake \mapsto 0, eatenCake \mapsto 0, haveNoCake \mapsto 1\}$

 $O = \{eatCake, bakeCake\},\$

 $eatCake = \langle haveCake, \neg haveCake \wedge haveNoCake \wedge eatenCake \rangle,$

 $bakeCake = \langle haveNoCake, haveCake \wedge \neg haveNoCake \rangle$ und

 $\gamma = haveCake \wedge eatenCake$.

- (a) Give the relaxation Π^+ of Π .
- (b) Give a sequence π of operators (as short as possible) from O such that π is not a plan of Π , but π^+ is a plan of Π^+ .

Exercise 5.2 (h^+ heuristic, 3+3 points)

A 15-puzzle planning task $\Pi = \langle A, I, O, \gamma \rangle$ is given as

$$\begin{array}{lll} A & = & \{empty(p_{i,j}) \mid 0 \leq i, j \leq 3\} \cup \{at(t_k, p_{i,j}) \mid 0 \leq i, j \leq 3, 0 \leq k \leq 14\}, \\ O & = & \{move(t_m, p_{i,j}, p_{k,l}) \mid 0 \leq i, j, k, l \leq 3, 0 \leq m \leq 14, \\ & & (i = k \text{ and } |j - l| = 1) \text{ or } (j = l \text{ and } |i - k| = 1)\}, \\ \gamma & = & \bigwedge_{0 \leq m \leq 14} at(t_m, p_{\lfloor m/4 \rfloor, m\%4}) \end{array}$$

Action $move(t_m, p_{i,j}, p_{k,l})$ moves tile t_m from position $p_{i,j}$ to position $p_{k,l}$:

$$\begin{aligned} move(t_m, p_{i,j}, p_{k,l}) &= \langle at(t_m, p_{i,j}) \wedge empty(p_{k,l}), \\ & at(t_m, p_{k,l}) \wedge empty(p_{i,j}) \wedge \neg at(t_m, p_{i,j}) \wedge \neg empty(p_{k,l}) \rangle \end{aligned}$$

A syntactically possible state is legal if each tile t_m is at some position p_{ij} , if no two tiles are at the same position and if the remaining position is the only one that is empty. The initial state is an arbitrary state that is legal.

One possible heuristic for the 15-puzzle is the Manhattan-distance heuristic $h^{Manhattan}$: It sums the Manhattan distances of all tiles from their current positions to their target positions, where the Manhattan distance between position $p_{i,j}$ and $p_{k,l}$ is given as |i-k|+|j-l|.

The h^+ heuristic estimates the distance of state s to the closest goal state as the length of the optimal plan in the relaxed planning task (with initial state s).

- (a) Show that $h^+(s) \ge h^{Manhattan}(s)$ for each legal state s of a 15-puzzle planning task.
- (b) Show that $h^+(s) > h^{Manhattan}(s)$ for at least one state s of a 15-puzzle planning task.

You may and should solve the exercise sheets in groups of two. Please state both names on your solution.