## Principles of AI Planning

16. Strong nondeterministic planning



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### Strong planning



Concepts

Algorithms

Summary

In this chapter, we will consider the simplest case of nondeterministic planning by restricting attention to strong plans.



## 2Œ

### Concepts Strong plans

Images
Weak preimages
Strong preimages

Algorithms

Summary

## Concepts

### Strong plans



Recall the definition of strong plans:

### Definition (strong plan)

Let S be the set of states of a planning task  $\Pi$ . Then a strong plan for  $\Pi$  is a function  $\pi:S_\pi\to O$  for some subset  $S_\pi\subseteq S$ such that

- $\blacksquare$   $\pi(s)$  is applicable in s for all  $s \in S_{\pi}$ ,
- $\blacksquare S_{\pi}(s_0) \subseteq S_{\pi} \cup S_{\star}$  ( $\pi$  is closed),
- $\blacksquare$   $S_{\pi}(s') \cap S_{\star} \neq \emptyset$  for all  $s' \in S_{\pi}(s_0)$  ( $\pi$  is proper), and
- there is no state  $s' \in S_{\pi}(s_0)$  such that s' is reachable from s' following  $\pi$  in a strictly positive number of steps ( $\pi$  is acyclic).

#### Strong plans



#### Concepts

#### Strong plans

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#### Execution of a strong plan

- Determine the current state *s*.
- If s is a goal state then terminate.
- $\blacksquare$  Execute action  $\pi(s)$ .
- Repeat from first step.

### Strong plans



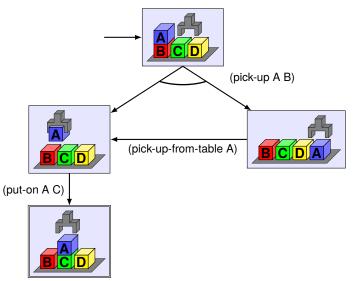




Images

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Algorithms



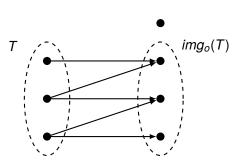
### **Images**



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#### **Image**

The image of a set T of states with respect to an operator o is the set of those states that can be reached by executing o in a state in T.



Concepts

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#### Concepts

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Definition (image of a state)

$$img_o(s) = \{s' \in S | s \xrightarrow{o} s'\} = app_o(s)$$

Definition (image of a set of states)

$$img_o(T) = \bigcup_{s \in T} img_o(s)$$

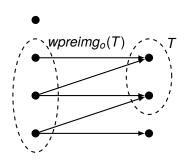
## Weak preimages



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#### Weak preimage

The weak preimage of a set T of states with respect to an operator o is the set of those states from which a state in T can be reached by executing o.



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## Weak preimages



Weak preimages

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Definition (weak preimage of a state)

wpreim
$$g_o(s') = \{s \in S | s \xrightarrow{o} s'\}$$

Definition (weak preimage of a set of states)

wpreim $g_o(T) = \bigcup_{s \in T} wpreimg_o(s)$ .

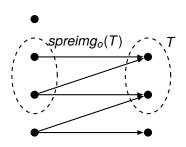
### Strong preimages



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### Strong preimage

The strong preimage of a set T of states with respect to an operator o is the set of those states from which a state in T is always reached when executing o.



#### Concepts

Strong plans Images Weak preimage

Strong preimages

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#### Concepts

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Definition (strong preimage of a set of states)

 $spreimg_o(T) = \{ s \in S \mid \exists s' \in T : s \xrightarrow{o} s' \land img_o(s) \subseteq T \}$ 



## **Algorithms**

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## Algorithms for strong planning



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Dynamic programming (backward)

Compute operator/distance/value for a state based on the operators/distances/values of its all successor states.

- Zero actions needed for goal states.
- If states with i actions to goals are known, states with  $\leq i + 1$  actions to goals can be easily identified.

Automatic reuse of plan suffixes already found.

2 Heuristic search (forward)

Strong planning can be viewed as AND/OR graph search.

OR nodes: Choice between operators

AND nodes: Choice between effects

Heuristic AND/OR search algorithms:

AO\*, Proof Number Search, ...

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#### Planning by dynamic programming

If for all successors of state s with respect to operator o a plan exists, assign operator o to s.

- Base case i = 0: In goal states there is nothing to do.
- Inductive case  $i \ge 1$ : If  $\pi(s)$  is still undefined and there is  $o \in O$  such that for all  $s' \in img_o(s)$ , the state s' is a goal state or  $\pi(s')$  was assigned in an earlier iteration, then assign  $\pi(s) = o$ .

#### Backward distances

If s is assigned a value on iteration  $i \ge 1$ , then the backward distance of s is i. The dynamic programming algorithm essentially computes the backward distances of states.

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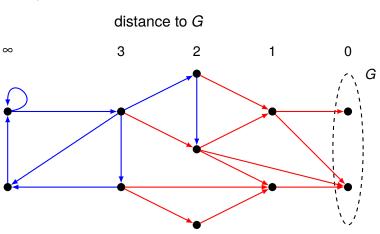
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#### Backward distances



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#### Example



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#### **Backward distances**



#### Definition (backward distance sets)

Let G be a set of states and O a set of operators.

The backward distance sets  $D_i^{bwd}$  for G and O consist of those states for which there is a guarantee of reaching a state in G with at most i operator applications using operators in O:

$$D_0^{bwd} := G$$

$$D_i^{bwd} := D_{i-1}^{bwd} \cup \bigcup_{o \in O} spreimg_o(D_{i-1}^{bwd}) \text{ for all } i \ge 1$$

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#### Backward distances



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## Definition (backward distance)

Let G be a set of states and O a set of operators, and let  $D_0^{bwd}, D_1^{bwd}, \dots$  be the backward distance sets for G and O. Then the backward distance of a state s for G and O is

$$\delta_G^{bwd}(s) = \min\{i \in \mathbb{N} \mid s \in D_i^{bwd}\}$$

(where  $\min \emptyset = \infty$ ).

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## Strong plans based on distances



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Let  $\Pi = \langle V, I, O, \gamma \rangle$  be a nondeterministic planning task with state set S and goal states  $S_+$ .

#### Extraction of a strong plan from distance sets

- Let  $S' \subseteq S$  be those states having a finite backward distance for  $G = S_*$  and O.
- Let  $s \in S'$  be a state with distance  $i = \delta_G^{bwd}(s) \ge 1$ .
- Assign to  $\pi(s)$  any operator  $o \in O$  such that  $img_o(s) \subseteq D_{i-1}^{bwd}$ . Hence o decreases the backward distance by at least one.

Then  $\pi$  is a strong plan for  $\mathscr{T}$  iff  $I \in S'$ .

Question: What is the worst-case runtime of the algorithm?

Question: What is the best-case runtime of the algorithm if most states have a finite backward distance?

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Summan

## Making the algorithm a logic-based algorithm



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- An algorithm that represents the states explicitly stops being feasible at about 10<sup>8</sup> or 10<sup>9</sup> states.
- For planning with bigger transition systems structural properties of the transition system have to be taken advantage of.
- As before, representing state sets as propositional formulae (or BDDs) often allows taking advantage of the structural properties: a formula (or BDD) that represents a set of states or a transition relation that has certain regularities may be very small in comparison to the set or relation.
- In the following, we will present an algorithm using a boolean-formula representation (without going into the details of how to implement it using BDDs).

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### Making the algorithm a logic-based algorithm



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Remark: The following algorithm assumes a propositional representation of the state space as opposed to a finite-domain representation. We have already seen how to translate an FDR encoding into a propositional encoding in Chapter 9 (cf. definition of the "induced propositional planning task").

Therefore, for the rest of the present section, we will assume without loss of generality that all  $v \in V$  are propositional variables with domain  $\mathcal{D}_v = \{0, 1\}$ .

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## Breadth-first search with progression and state sets (deterministic case)



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```
Progression breadth-first search
```

```
def bfs-progression(V, I, O, \gamma):
    goal := formula-to-set(\gamma)
    reached := \{I\}

loop:
    if reached \cap goal \neq \emptyset:
    return solution found
    new-reached := reached \cup \bigcup_{o \in O} img_o(reached)
    if new-reached = reached:
    return no solution exists
    reached := new-reached
```

→ This can easily be transformed into a regression algorithm.

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## Breadth-first search with regression and state sets (deterministic case)





Efficient implementation of

earession

```
Regression breadth-first search
```

```
def bfs-regression(V, I, O, \gamma):
    init := I
    reached := formula-to-set(\gamma)
    loop:
        if init \in reached:
            return solution found
            new-reached := reached \cup \bigcup_{o \in O} wpreimg_o(reached)
        if new-reached = reached:
            return no solution exists
        reached := new-reached
```

This algorithm is very similar to the dynamic programming algorithm for the nondeterministic case!

## Breadth-first search with regression and state sets (strong nondeterministic case)



Efficient implementation of

earession

```
Regression breadth-first search
```

```
def bfs-regression(V, I, O, \gamma):
    init := I
    reached := formula-to-set(\gamma)
    loop:
    if init \in reached:
    return solution found
    new-reached := reached \cup \bigcup_{o \in O} spreimg_o(reached)
    if new-reached = reached:
```

return no solution exists

reached := new-reached

Remark: Do you recognize the assignments  $D_0^{bwd} := G$  and  $D_i^{bwd} := D_{i-1}^{bwd} \cup \bigcup_{o \in O} spreimg_o(D_{i-1}^{bwd})$  for  $i \ge 1$ ?

## Breadth-first search with regression and state sets (strong nondeterministic case, symbolic)



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Efficient implementation of

earession

```
Regression breadth-first search
```

```
def bfs-regression(V, I, O, \gamma):
     init := I
     reached := \gamma
     loop:
           if init \models reached:
                return solution found
           new-reached := reached ∨
                                \bigvee_{o \in O} spreimgsymb<sub>o</sub>(reached)
           if new-reached \equiv reached:
                return no solution exists
           reached := new-reached
```

How do we define spreimgsymb with logic (or BDD) operations?

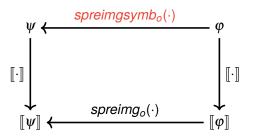
## Symbolic strong preimage computation



Let  $\varphi$  be a logic formula and  $\llbracket \varphi \rrbracket = \{ s \in S \mid s \models \varphi \}$ .

We want: a symbolic preimage operation *spreimgsymb* such that if  $\psi = spreimgsymb_o(\varphi)$ , then  $\llbracket \psi \rrbracket = \{ s \in S \mid s \models \psi \} = spreimg_o(\llbracket \varphi \rrbracket)$ .

In other words, we want the following diagram to commute:



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Let V be the set of state variables and  $V' := \{v' | v \in V\}$  a set of primed copies of the variables in V. Intuition:

- Variables in V describe the current state s.
- $\blacksquare$  Variables in V' describe the next state s'.

We would like to define a formula  $\tau_V(o)$  that describes the transitions labeled with o between states s (over V) and s' (over V') in terms of V and V'.

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Summary

The formula  $\tau_V(o)$  must express

- the conditions for applicability of o,
- how o changes state variables, and
- which state variables o does not change.

A significant difficulty lies in the third requirement because different variables may be affected depending on nondeterministic choices.



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 $\tau_V(o)$  for deterministic operators  $o = \langle \chi, e \rangle$ 

$$\tau_{V}(o) = \chi \land \bigwedge_{v \in V} ((EPC_{v}(e) \lor (v \land \neg EPC_{\neg v}(e))) \leftrightarrow v')$$
$$\land \bigwedge_{v \in V} \neg (EPC_{v}(e) \land EPC_{\neg v}(e))$$

Assume that  $e = \bigwedge_{a \in A} a \land \bigwedge_{d \in D} \neg d$  for  $A = \{a_1, \dots, a_k\}$  and  $D = \{d_1, \dots, d_l\}$  with  $A \cap D = \emptyset$ . Then this becomes simpler.

$$\tau_V(o)$$
 for STRIPS operators  $o = \langle \chi, \bigwedge_{a \in A} a \land \bigwedge_{d \in D} \neg d \rangle$ 

$$\tau_V(o) = \chi \land \bigwedge_{a \in A} a' \land \bigwedge_{d \in D} \neg d' \land \bigwedge_{v \in V \setminus (A \cup D)} (v \leftrightarrow v')$$

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For nondeterministic operators  $o = \langle \chi, \{e_1, \dots, e_n\} \rangle$  with corresponding add and delete lists  $A_i$  and  $D_i$  of  $e_i$  such that  $A_i \cap D_i = \emptyset$ ,  $i = 1, \dots, n$ , we get:

 $\tau_V(o)$  for nondeterministic operators  $o = \langle \chi, \{e_1, \dots, e_n\} \rangle$ 

$$\tau_{V}(o) = \chi \wedge \bigvee_{i=1}^{n} \left( \bigwedge_{a \in A_{i}} a' \wedge \bigwedge_{d \in D_{i}} \neg d' \wedge \bigwedge_{v \in V \setminus (A_{i} \cup D_{i})} (v \leftrightarrow v') \right)$$

#### Example

Let  $V = \{a,b\}$ ,  $V' = \{a',b'\}$ , and  $o = \langle \neg a, \{a,a \land \neg b\} \rangle$ . Then

$$\tau_V(o) = \neg a \wedge \Big( \Big( a' \wedge (b \leftrightarrow b') \Big) \vee (a' \wedge \neg b') \Big).$$

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Summar

#### Definition (substitution)

Let  $\varphi, t_1, \dots, t_n$  be propositional formulas and  $v_1, \dots, v_n$  atomic propositions.

We denote the formula obtained from  $\varphi$  by simultaneous replacement of all variables  $v_i$  by the corresponding formulas  $t_i$ , i = 1, ..., n, by  $\varphi[t_1, ..., t_n/v_1, ..., v_n]$ .

## Computing strong preimages



#### Definition (existential abstraction)

Let  $\varphi$  be a propositional formula and  $v_1, \ldots, v_n$  be atomic propositions. Then the existential abstraction of  $\varphi$  wrt.  $v_1, \ldots, v_n$  is recursively defined as follows:

$$\exists v. \varphi := \varphi[\top/v] \lor \varphi[\bot/v]$$

For a set of variables  $V = \{v_1, \dots, v_n\}$  we use the abbreviation

$$\exists V. \varphi := \exists v_1 \dots \exists v_n. \varphi.$$

Note: Even with intermediate formula simplifications this can lead to an exponential blowup. BDDs can be useful here.

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## Computing strong preimages



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#### Strong preimages

$$\begin{aligned} spreimg_o(T) &= \{s \in S \mid \exists s' \in T : s \xrightarrow{o} s' \land img_o(s) \subseteq T\} \\ &= \{s \in S \mid (\exists s' \in S : s \xrightarrow{o} s' \land s' \in T) \land \\ \{s' \in S \mid s \xrightarrow{o} s' \} \subseteq T\} \\ &= \{s \in S \mid (\exists s' \in S : s \xrightarrow{o} s' \land s' \in T) \land \\ (\forall s' \in S : s \xrightarrow{o} s' \Rightarrow s' \in T)\} \\ &= \{s \in S \mid (\exists s' \in S : s \xrightarrow{o} s' \land s' \in T) \land \\ (\neg \exists s' \in S : s \xrightarrow{o} s' \land \neg (s' \in T))\} \end{aligned}$$

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## Computing strong preimages with boolean function operations



$$spreimg_o(T) = \{ s \in S \mid (\exists s' \in S : s \xrightarrow{o} s' \land s' \in T) \land (\neg \exists s' \in S : s \xrightarrow{o} s' \land \neg (s' \in T)) \}$$

### Strong preimages with boolean functions

For formula  $\varphi$  characterizing set T of strongly backward-reached states:

$$spreimgsymb_o(\varphi) = \left( \exists V'. (\tau_V(o) \land \varphi[v'_1, \dots, v'_n/v_1, \dots, v_n]) \right) \land \left( \neg \exists V'. (\tau_V(o) \land \neg \varphi[v'_1, \dots, v'_n/v_1, \dots, v_n]) \right)$$

We can use this regression formula for efficient symbolic regression search. BDDs support all necessary operations (atomic propositions,  $\neg$ ,  $\wedge$ ,  $\vee$ , substitution,  $\exists$ , ...).

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## Computing strong preimages with boolean function operations



# EIBURG

### Example

Let 
$$V=\{a,b\},\ V'=\{a',b'\},$$
 and 
$$o=\langle \neg a,\{a,a\wedge \neg b\}\rangle, \quad \text{i.e.,}$$
 
$$\tau_V(o)=\neg a\wedge \Big(\big(a'\wedge (b\leftrightarrow b')\big)\vee (a'\wedge \neg b')\Big).$$

Moreover, let  $\varphi = a$ . Then

$$spreimgsymb_{o}(\varphi) = \exists a' \exists b'. \Big( \neg a \land \Big( \big( a' \land (b \leftrightarrow b') \big) \lor (a' \land \neg b') \Big) \land a' \Big) \land \\ \neg \exists a' \exists b'. \Big( \neg a \land \Big( \big( a' \land (b \leftrightarrow b') \big) \lor (a' \land \neg b') \Big) \land \neg a' \Big) \\ \equiv \neg a$$

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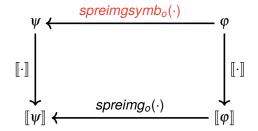
## Computing strong preimages with boolean function operations



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#### **Theorem**

The previous definition of the symbolic preimage operator makes the following diagram commute:



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Summary



Homework



# **Progression Search**



- We saw a generalization of regression search to strong planning.
- However, this search is uninformed (breadth-first search).
- Is there an analogue to A\* search for strong planning?
- Yes: AO\* search
  - Progression search (like A\*)
  - Guided by a heuristic (like A\*)
  - Guaranteed optimality (under certain conditions, like A\*)

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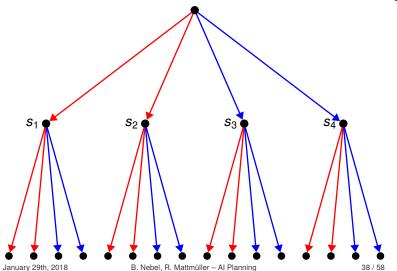
Regression

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# AND/OR search







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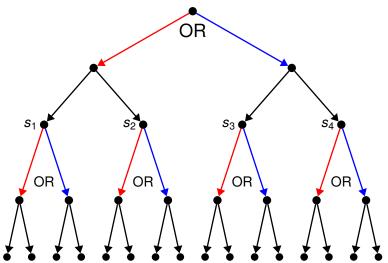
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# AND/OR search







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- We describe AO\* on a graph representation without intermediate nodes, i.e., as in the first figure.
- There are different variants of AO\*, depending on whether the graph that is being searched is an AND/OR tree, an AND/OR DAG, or a general, possibly cyclic, AND/OR graph.
- The graphs we want to search,  $\mathscr{T}(\Pi)$ , are in general cyclic.
- However, AO\* becomes a bit more involved when dealing with cycles, so we only discuss AO\* under the assumption of acyclicity and leave the generalization to cyclic state spaces as an exercise.

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- The search is over  $\mathcal{T}(\Pi)$ .
- For ease of presentation, we do not distinguish between states of  $\mathcal{T}(\Pi)$  and search nodes.
- Also, for ease of presentation, we do not handle the case that no strong plan exists.



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# Definition (solution graph)

A solution graph for a nondeterministic transition system  $\mathscr{T} = \langle S, L, T, s_0, S_\star \rangle$  is an acyclic subgraph of  $\mathscr{T}$  (viewed as a graph),  $\mathscr{T}' = \langle S', L, T' \rangle$ , such that

- $\blacksquare$   $s_0 \in S'$ ,
- for each  $s' \in S' \setminus S_{\star}$ , there is exactly one label  $I \in L$  s.t.
  - $\blacksquare$  T' contains at least one outgoing transition from s' labeled with I,
  - T' contains all outgoing transitions from s' labeled with I
     (and S' contains the states reached via such transitions),
  - T' contains no outgoing transitions from s' labeled with any  $\tilde{l} \neq l$ , and
- $\blacksquare$  every directed path in  $\mathcal{T}'$  terminates at a goal state.



Conceptually, there are three graphs/transition systems:

- The induced transitions system  $\mathcal{T} = \mathcal{T}(\Pi)$ , which only exists as a mathematical object, but is in general not made explicit completely during AO\* search,
- The current portion of  $\mathcal{T}$  explicitly represented by the search algorithm,  $\mathcal{T}_{e}$ , and
- The current portion of  $\mathcal{T}_e$  considered by the algorithm as the cheapest/best current partial solution graph,  $\mathcal{T}_p$ .

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# Definition (partial solution graph)

A partial solution graph for a nondeterministic transition system  $\mathscr{T} = \langle S, L, T, s_0, S_{\star} \rangle$  is an acyclic subgraph of  $\mathscr{T}$  (viewed as a graph),  $\mathscr{T}_{\mathcal{D}} = \langle S_{\mathcal{D}}, L, T_{\mathcal{D}} \rangle$ , s.t.

- $\blacksquare$   $s_0 \in S_p$ ,
- for each  $s' \in S_p$  that is not an unexpanded leaf node in  $\mathscr{T}_p$  there is exactly one label  $I \in L$  such that
  - $T_p$  contains at least one outgoing transition from s' labeled with I.
  - T<sub>p</sub> contains all outgoing transitions from s' labeled with l (and  $S_p$  contains the states reached via such transitions),
  - $T_p$  contains no outgoing transitions from s' labeled with any  $\tilde{l} \neq l$ , and
- every directed path in  $\mathcal{T}_p$  terminates at a goal state or an unexpanded leaf node in  $\mathcal{T}_p$ .

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# Definition (cost of a partial solution graph)

Let  $h: S \to \mathbb{N} \cup \{\infty\}$  be a heuristic function for the state space S of  $\mathscr{T}$ , and let  $\mathscr{T}_p = \langle S_p, L, T_p \rangle$  be a partial solution graph. The cost labeling of  $\mathscr{T}_p$  is the solution to the following system of equations over the states  $S_p$  of  $\mathscr{T}_p$ :

$$f(s) = \begin{cases} 0 & \text{if } s \text{ is a goal state} \\ h(s) & \text{if } s \text{ is an unexpanded non-goal} \\ 1 + \max_{s \xrightarrow{o} s'} f(s') & \text{for the unique outgoing action} \\ o \text{ of } s \text{ in } \mathscr{T}_p, \text{ otherwise.} \end{cases}$$

The cost of  $\mathcal{T}_p$  is the cost labeling of its root.

AO\* search keeps track of a cheapest partial solution graph by marking for each expanded state s an outgoing action o minimizing  $1 + \max_{s \xrightarrow{o} c'} f(s')$ .

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### Procedure ao-star

**def** ao-star( $\mathcal{T}$ ):

let  $\mathcal{T}_e$  and  $\mathcal{T}_p$  initially consist of the initial state  $s_0$ .

**while**  $\mathcal{T}_p$  has unexpanded non-goal node:

expand an unexpanded non-goal node s of  $\mathscr{T}_p$ 

add new successor states to  $\mathscr{T}_{\mathbf{e}}$ 

for all new states s' added to  $\mathcal{T}_e$ :

$$f(s') \leftarrow h(s')$$

 $Z \leftarrow s$  and its ancestors in  $\mathscr{T}_e$  along marked actions.

**while** *Z* is not empty:

remove from Z a state s w/o descendant in Z.

$$f(s) \leftarrow \min_{o \text{ applicable in } s} (1 + \max_{s \stackrel{o}{\longrightarrow} s'} f(s')).$$
 mark the best outgoing action for  $s$ 

(this may implicitly change  $\mathcal{T}_{p}$ ).

return an optimal solution graph.

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# Correctness (proof sketch)

- Solution graphs directly correspond to strong plans.
- Algorithm eventually terminates (finite number of possible node expansions).
- Acyclicity guarantees that extraction of  $\mathcal{T}_p$  and dynamic programming back-propagation of f values always terminates.
- Marking makes sure that existing solutions are eventually marked.

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implementation regression

Progression



#### **Details**

- Pseudocode omits bookkeeping of solved states (can improve performance).
- Choice of unexpanded non-goal node of best partial solution graph is unspecified.
  - Correctness/optimality not affected.
  - One possibility: choose node with lowest cost estimate.
  - Alternative: expand several nodes simultaneously.
- Algorithm can be extended to deal with cycles in the AND/OR graph.

#### Concepts

Regression

implementation regression

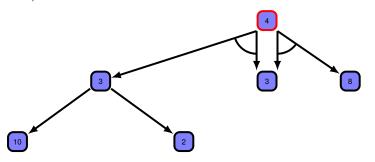
Progression

Summarv



# UNI FREIBUR

# Example



#### Concepts

#### Algorithms

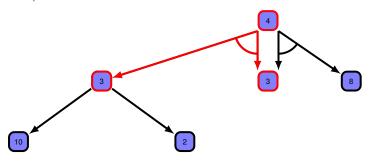
Regression

regression Progression



# UNI FREIBUR

# Example



#### Concepts

#### Algorithms

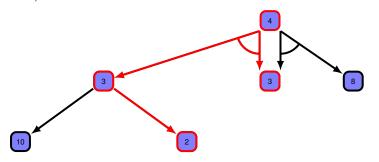
Regression

regression Progression



# UNI FREIBUR

# Example



#### Concepts

#### Algorithms

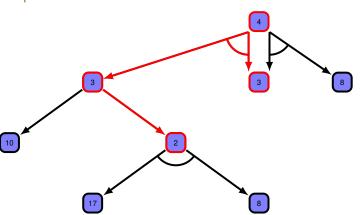
Regression

regression Progression



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# Example



#### Concepts

#### Algorithms

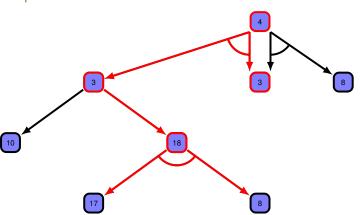
Regression

regression Progression



# UNI

# Example



#### Concepts

#### Algorithms

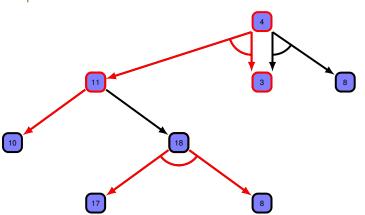
Regression

regression Progression



UNI FREIBUR

# Example



#### Concepts

#### Algorithms

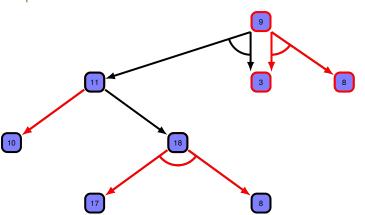
Regression

regression Progression



# UNI

# Example



#### Concepts

#### Algorithms

Regression

regression Progression



# UNI FREIBU

#### Heuristic Evaluation Function

- Desirable: informative, domain-independent heuristic to initialize cost estimates.
- Heuristic should estimate (strong) goal distances.
- Heuristic does not necessarily have to be admissible (unless we seek optimal solutions).
- We can adapt many heurstics we already know from classical planning (details omitted).

Concepts

Algorithms

Regression

regression

Progression

Cummon



Concepts

Algorithms

Summary

# **Summary**



- We have considered the special case of nondeterministic planning where
  - planning tasks are fully observable and
  - we are interested in strong plans.
- We have introduced important concepts also relevant to other variants of nondeterministic planning such as
  - images and
  - weak and strong preimages.
- We have discussed some basic classes of algorithms:
  - backward induction by dynamic programming, and
  - forward search in AND/OR graphs.

Concepts

Algorithms