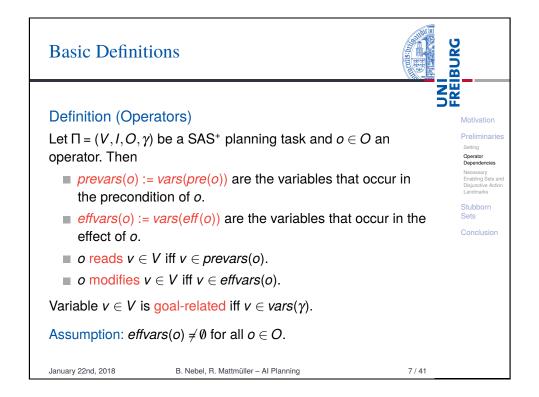


		LAND AND AND AND AND AND AND AND AND AND
		Preliminaries
		Operator Dependencies
Prelimi	narios	Necessary Enabling Sets and Disjunctive Action Landmarks
	nancs	Stubborn Sets
		Conclusion
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Setting		

Assumption: For the rest of the chapter, we assume that all planning tasks are SAS<sup>+</sup> planning tasks  $\Pi = (V, I, O, \gamma)$ .

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Motivation

Setting

Operator

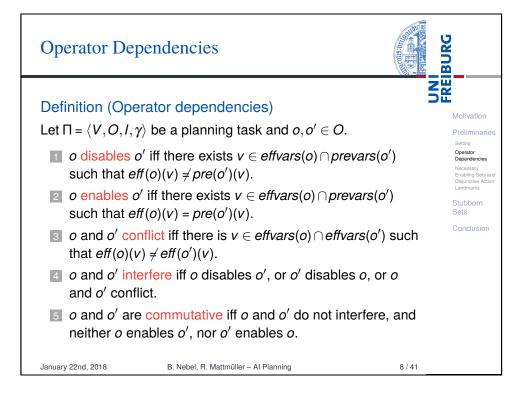
Necessary Enabling Sets a Disjunctive Act

Sets

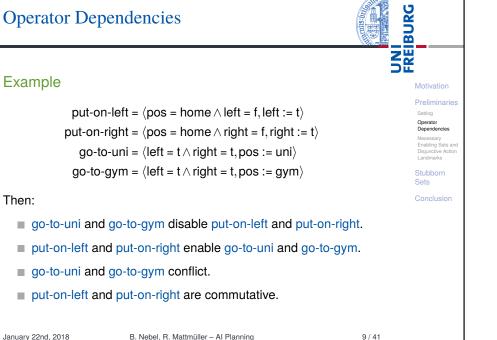
For convenience, we assume that operators have the form  $o = \langle pre(o), eff(o) \rangle$ , where pre(o) and eff(o) are both partial states over *V*, i.e., partial functions mapping variables *v* to values in  $\mathcal{D}_v$ . Similarly, we assume that  $\gamma$  is a partial state describing the goal.

### Example

Operator  $o = \langle pre(o), eff(o) \rangle$  with  $pre(o) = \{v_1 \mapsto d_1, v_5 \mapsto d_5\}$  and  $eff(o) = \{v_2 \mapsto d_2, v_3 \mapsto d_3\}$ corresponds to  $o = \langle \chi, e \rangle$  with  $\chi = (v_1 = d_1 \land v_5 = d_5)$  and  $e = (v_2 := d_2 \land v_3 := d_3)$ . January 22nd, 2018 B. Nebel, R. Mattmüller – Al Planning 6/41







# Necessary Enabling Sets and Disjunctive **Action Landmarks**

Definition (Disjunctive action landmark)

Let  $\Pi = \langle V, I, O, \gamma \rangle$  be a planning task and *s* a state. A disjunctive action landmark (DAL) L in s is a set of operators such that all operator sequences that lead from s to a goal state contain some operator in L.

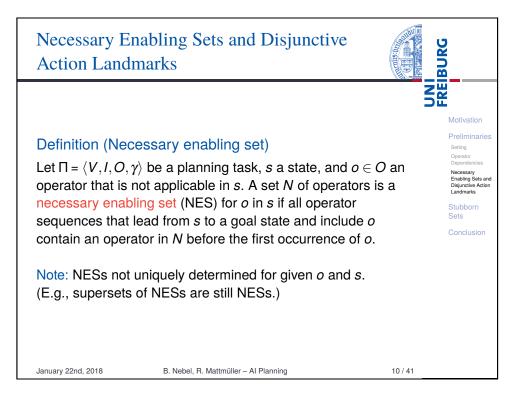
Setting
Operator Dependencies
Necessary Enabling Sets and Disjunctive Action Landmarks
Stubborn Sets

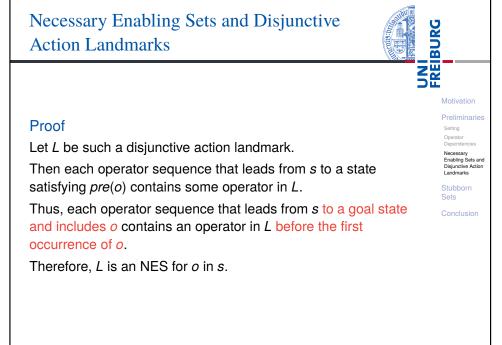
Motivation

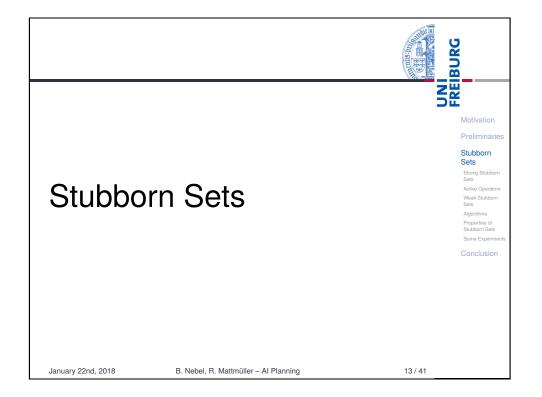
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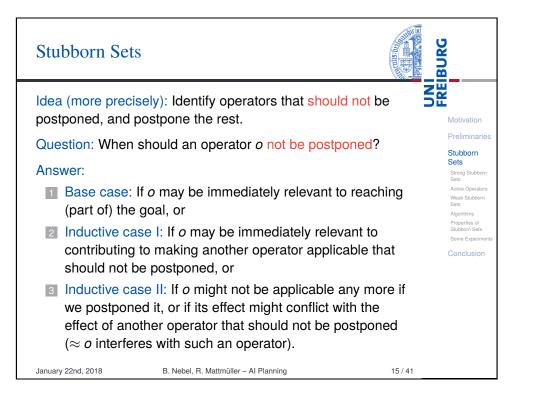
#### Observation

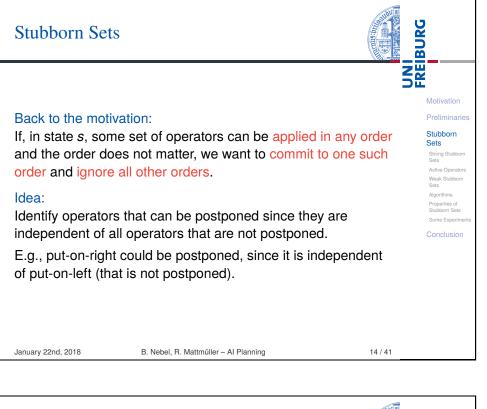
For state *s* and operator *o* that is not applicable in *s*, disjunctive action landmarks for task  $\langle V, I, O, pre(o) \rangle$  are necessary enabling sets for o in s.

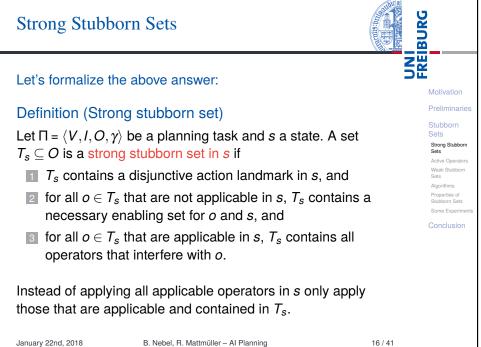












### Strong Stubborn Sets

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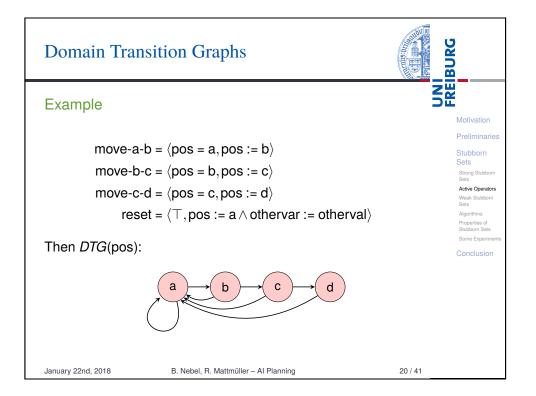
#### BURG Example Motivation $I = \{ pos \mapsto home, left \mapsto f, right \mapsto f \}, \gamma = \{ pos \mapsto uni \}$ put-on-left = $\langle pos = home \land left = f, left := t \rangle$ Sets put-on-right = $\langle pos = home \land right = f, right := t \rangle$ Strong Stubborn go-to-uni = $\langle \text{left} = t \land \text{right} = t, \text{pos} := \text{uni} \rangle$ Active Operator Weak Stubborn Sets Algorithms Step 1: DAL in *I* is {go-to-uni} $\rightarrow T_s := \{go-to-uni\}$ . Properties of Some Experime Step 2: go-to-uni not applicable in *I*. One possible NES for go-to-uni in *I* is {put-on-left} $\rightsquigarrow T_s := T_s \cup \{\text{put-on-left}\}.$ Step 3: put-on-left is applicable in *I*. The only operator that interferes with it, go-to-uni, is already in $T_s$ . Hence, $T_s = \{$ go-to-uni, put-on-left $\}$ , and $T_s$ restricted to the applicable operators is {put-on-left}. During search, only apply put-on-left (not put-on-right).

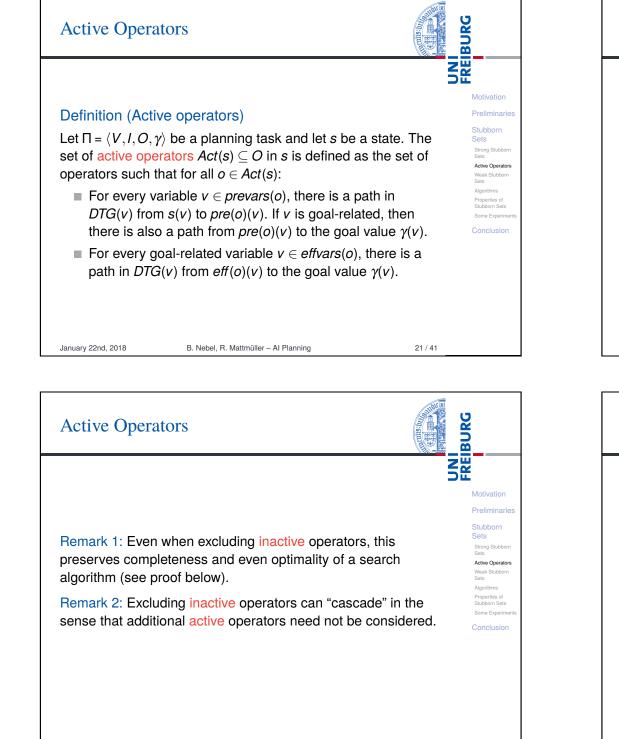
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UNI FREIBURG **Domain Transition Graphs** Motivation Definition (Domain transition graph) Sets Let  $\Pi = (V, I, O, \gamma)$  be a SAS<sup>+</sup> planning task and  $v \in V$ . The Strong Stubborr Sets Active Operators domain transition graph for v is the directed graph Weak Stubborn Sets  $DTG(v) = \langle \mathscr{D}_v, E \rangle$  where  $(d, d') \in E$  iff there is an operator Algorithms Properties of  $o \in O$  with Some Experime  $\blacksquare$  eff(o)(v) = d', and •  $v \notin prevars(o)$  or pre(o)(v) = d. January 22nd, 2018 B. Nebel, R. Mattmüller - Al Planning 19/41

Strong Stubbor	rn Sets		
Example			
Let $V = \{u_1, u_2, v, v\}$	$v$ , $I = \{u_1 \mapsto 0, u_2 \mapsto 0, v \mapsto 0, w \mapsto 0$	→ 0}.	Motivation
<b>(</b> · / <b>-</b> / /	$, u_2 \mapsto 1$ , and $O = \{o_1, o_2, o_3\}$ , wh	, ·	Preliminaries
$o_1 = \langle u_1 = 0, u \rangle$	$_1 := 1 \wedge w := 2 \rangle$ ,		Stubborn Sets
$ O_2 = \langle u_2 = 0, u \rangle $			Strong Stubborn Sets Active Operators
= ( = / /	$u_2 = 0, v := 1 \land w := 1 \rangle.$		Weak Stubborn Sets
Strong stubborn se	_ /		Algorithms Properties of Stubborn Sets Some Experiment
U U	e $o_1$ (or $o_2$ ) in $T_s$ as DAL.		Conclusion
Step 2: Includ	e $o_3$ in $T_s$ since it interferes with $o_3$	<sub>1</sub> (or <i>o</i> <sub>2</sub> ).	
Step 3: Includ	e $o_2$ (or $o_1$ ) in $T_s$ since it interferes	with $o_3$ .	
→ all applicable or	perators included in $T_s$ , no pruning	•	
Question: Can we	do better than that in this example	?	
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Active Oper	ators		BURG
		2	FRE
Proposition			Motivation
	be identified efficiently for a given s g paths in the projection of $\Pi$ onto v	•	Preliminaries Stubborn Sets
when reas	not in $Act(s)$ can be treated as non oning about <i>s</i> because they are no s reachable from <i>s</i> , or they lead to a	t applicable	Strong Stubborn Sets Active Operators Weak Stubborn Sets Algorithms Properties of Stubborn Sets Some Experiments
Proof			Conclusion
1 Homework <i>Act(s</i> ).	: Specify efficient algorithm for ider	ntification of	
2 Obvious.			
January 22nd, 2018	B. Nebel, R. Mattmüller – Al Planning	22 / 41	
Γ			

Strong Stubborn Se	ets		
Definition (Strong stub pruning)	born set with active operator		Motivation Preliminaries
	planning task and <i>s</i> a state. A set orn set in <i>s</i> if		Stubborn Sets Strong Stubborn Sets
<b>1</b> $T_s$ contains a disjur	nctive action landmark in <i>s</i> , and		Active Operators Weak Stubborn Sets
	e not applicable in $s$ , $T_s$ contains set for $o$ and $s$ , and	а	Algorithms Properties of Stubborn Sets Some Experiments
	e applicable in $s$ , $T_s$ contains all active in $s$ and interfere with $o$ .		Conclusion
Instead of applying all a those that are applicable	oplicable operators in $s$ only apply and contained in $T_s$ .	/	
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### Strong Stubborn Sets

Why operator activity matters

BURG **NNI** Recall the previous example where strong stubborn sets without active operator pruning were useless. Motivation Sets  $\blacksquare I = \{u_1 \mapsto 0, u_2 \mapsto 0, v \mapsto 0, w \mapsto 0\},\$  $\gamma = \{ v \mapsto 0, u_1 \mapsto 1, u_2 \mapsto 1 \}$ Active Operators Weak Stubborn  $o_1 = \langle u_1 = 0, u_1 := 1 \land w := 2 \rangle$ Properties of  $o_2 = \langle u_2 = 0, u_2 := 1 \land w := 2 \rangle$  $o_3 = \langle u_1 = 0 \land u_2 = 0, v := 1 \land w := 1 \rangle$ Now, with active operator pruning: Step 1: Include  $o_1$  (or  $o_2$ ) in  $T_s$  as DAL. Step 2: Operator  $o_3$  is not active in any reachable state.  $\rightsquigarrow o_3$  not in  $T_s$ , although it interferes with  $o_1$  (or  $o_2$ ).

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Example

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## Weak Stubborn Sets

With weak stubborn sets, some operators that disable an operator in  $T_s$  need not be included in  $T_s$ .

Therefore, weak stubborn sets potentially allow more pruning than strong stubborn sets.

### Definition (Weak stubborn set)

Let  $\Pi = \langle V, I, O, \gamma \rangle$  be a planning task and *s* a state. A set  $T_s \subset O$  is a weak stubborn set in s if

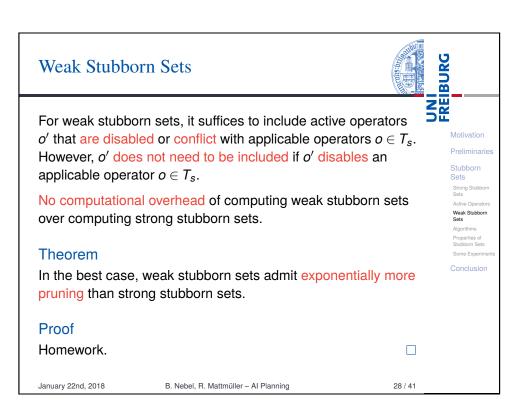
- **T**<sub>s</sub> contains a disjunctive action landmark in s, and
- 2 for all  $o \in T_s$  that are not applicable in s,  $T_s$  contains a necessary enabling set for o and s, and
- **3** for all  $o \in T_s$  that are applicable in *s*,  $T_s$  contains the active operators in s that have conflicting effects with o or that are disabled by o.

Strong Stubborn Sets  
Why operator activity matters  
**Example (Example, ctd.)**  
Now, with active operator pruning:  
Step 1: Include 
$$o_1$$
 (or  $o_2$ ) in  $T_s$  as DAL.  
Step 2: Operator  $o_3$  is not active in any reachable state.  
 $\Rightarrow o_3$  not in  $T_s$ , although it interferes with  $o_1$  (or  $o_2$ ).  
Hence, e.g.,  $T_s = \{o_1\}$  strong stubborn set (with active  
operator pruning) in *I*.  
Even active operator  $o_2$  is not included in  $T_s = \{o_1\}$ .  
 $\Rightarrow$  some pruning occurs.  
Motivation  
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UNI FREIBURG

Motivation

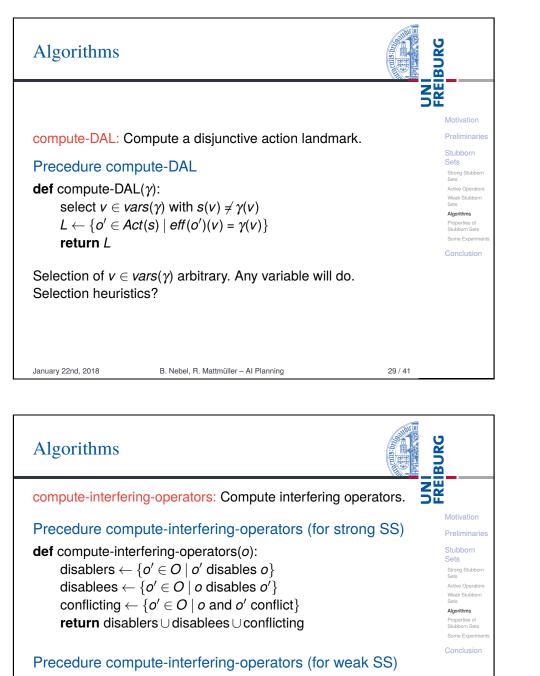
Sets

Strong Stubborn

Weak Stubborn

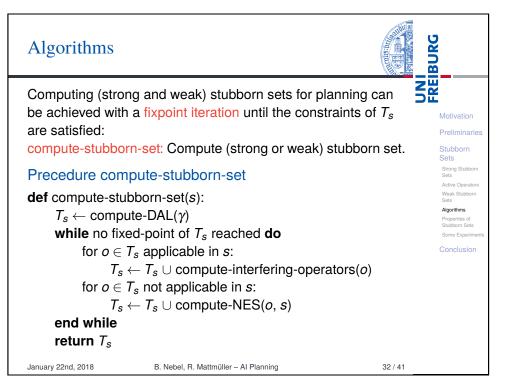
Algorithms

Properties of



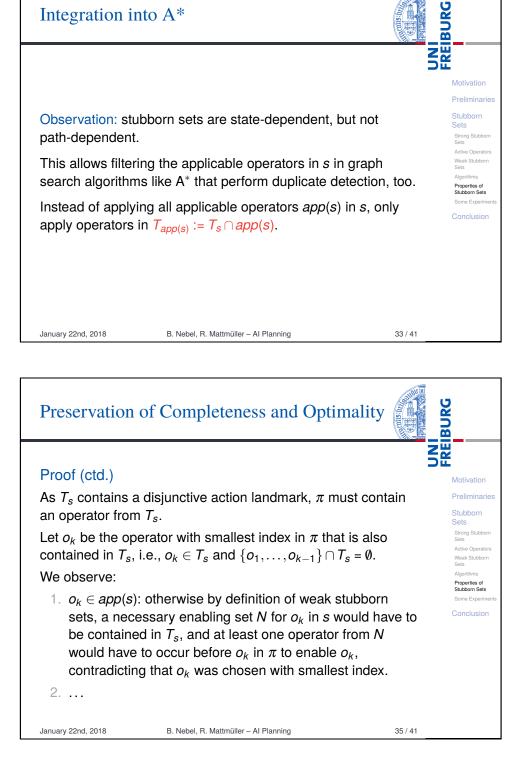
 $\begin{array}{l} \textbf{def compute-interfering-operators}(o):\\ \text{disablees} \leftarrow \{o' \in O \mid o \text{ disables } o'\}\\ \text{conflicting} \leftarrow \{o' \in O \mid o \text{ and } o' \text{ conflict}\}\\ \textbf{return } \text{disablees} \cup \text{conflicting} \end{array}$ 

UNI FREIBURG Algorithms Motivation compute-NES: Compute a necessary enabling set. Precedure compute-NES Sets **def** compute-NES(*o*,*s*): Active Operato Weak Stubbor select  $v \in prevars(o)$  with  $s(v) \neq pre(o)(v)$ Algorithms  $N \leftarrow \{o' \in Act(s) \mid eff(o')(v) = pre(o)(v)\}$ return N Selection of  $v \in prevars(o)$  arbitrary. Any variable will do. Selection heuristics? 30/41 January 22nd, 2018 B. Nebel, R. Mattmüller - Al Planning



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### Integration into A\*



## Preservation of Completeness and Optimality



#### Theorem

Weak stubborn sets are completeness and optimality preserving.

### Proof

Let  $T_{app(s)} := T_s \cap app(s)$  for a weak stubborn set  $T_s$ .

We show that for all states s from which an optimal plan consisting of n > 0 operators exists,  $T_{app(s)}$  contains an operator that starts such a plan.

We show by induction that A\* restricting successor generation to  $T_{app(s)}$  is optimal.

Let  $T_s$  be a weak stubborn set and  $\pi = o_1, \ldots, o_n$  be an optimal plan that starts in s.

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# Preservation of Completeness and Optimality

UNI FREIBURG

Motivation

Sets

Sets Algorithms

Strong Stubb

Weak Stubbon

Properties of

Stubborn Set

### Proof (ctd.)

#### 1. . . .

2.  $o_k$  is does not disable any of the operators  $o_1, \ldots, o_{k-1}$ , and all these operators have non-conflicting effects with  $o_k$ : otherwise, as  $o_k \in app(s)$ , and by definition of weak stubborn sets, at least one of  $o_1, \ldots, o_{k-1}$  would have to be contained in  $T_s$ , again contradicting the assumption.

Hence, we can move  $o_k$  to the front:

 $o_k, o_1, \ldots, o_{k-1}, o_{k+1}, \ldots, o_n$  is also a plan for  $\Pi$ .

It has the same cost as  $\pi$  and is hence optimal.

Thus, we have found an optimal plan of length *n* started by an operator  $o_k \in T_{app(s)}$ , completing the proof. 

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### Motivation

Sets

Weak Stubbo

Properties of

Stubborn Set

### Preservation of Completeness and Optimality



Motivation

Stubborn Sets

Strong Stubborn Sets

Active Operators Weak Stubborn Sets

Algorithms Properties of

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Stubborn Sets Some Experime

Preliminaries

**Remark**: The argument to move  $o_k$  to the front also holds for strong stubborn sets: in this case,  $o_k$  is not even disabled by any of  $o_1, \ldots, o_{k-1}$  (and hence,  $o_k$  is independent of  $o_1, \ldots, o_{k-1}$ ), which is a stronger property than needed in the proof.

### Corollary

Strong stubborn sets are completeness and optimality preserving.

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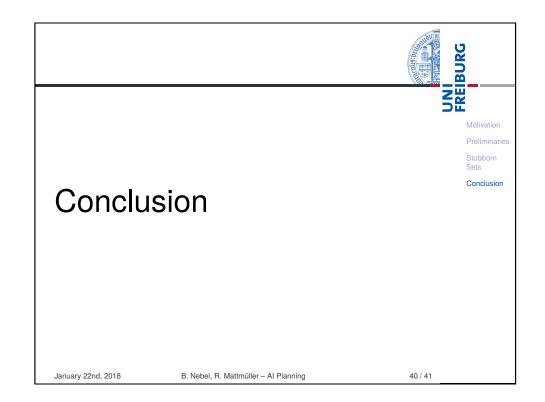
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						Motivatio Prelimina
Domain (problems)	Cove SSS	erage WSS	Nodes ge SSS	nerated WSS	# problems w. diff. gen.	Stubborn Sets
OPENSTACKS-OPT08 (30)	21	±0	152711917	99.936%	18	Strong Stub Sets
OPENSTACKS-OPT11 (20)	16	$\pm 0$	152642101	99.936%	16	Active Open Weak Stubb
PATHWAYS-NONEG (30)	5	$\pm 0$	162347	99.702%	2	Sets Algorithms
PSR-SMALL (50)	49	$\pm 0$	18119489	99.998%	6	Properties of Stubborn Se
SATELLITE (36)	12	$\pm 0$	70299721	92.804%	12	Stubborn Se Some Exper
In practice (or, at least, ifference between weak a				lems) there i	is no significant	Conclu

Some Experiments: Overview Optimal Planning, A\* with LM-cut Heuristic, Selected Domains

	Cov	erage	Nodes gen	erated	58
Domain (problems)	A*	+SSS	<b>A</b> *	+SSS	Motivation
PARCPRINTER-08 (30)	18	+12	2455181	<1%	
PARCPRINTER-OPT11 (20)	13	+7	2454533	<1%	Preliminarie
WOODWORKING-OPTO8 (30)	17	+10	26796212	<1%	Stubborn
WOODWORKING-OPT11 (20)	12	+7	26795517	<1%	Sets Strong Stubborn
SATELLITE (36)	7	+5	5116312	2%	Sets
ROVERS (40)	7	+2	1900691	22%	Active Operators Weak Stubborn
AIRPORT (50)	28	$\pm 0$	545072	93%	Sets
OPENSTACKS-OPT08 (30)	19	+2	56584063	51%	Algorithms Properties of
OPENSTACKS-OPT11 (20)	14	+2	56456969	51%	Stubborn Sets
DRIVERLOG (20)	13	+1	3679376	82%	Some Experime
SCANALYZER-08 (30)	15	-3	14203012	100%	Conclusion
SCANALYZER-OPT11 (20)	12	-3	14202884	100%	
PARKING-OPT11 (20)	3	-1	560914	100%	
SOKOBAN-OPTO8 (30)	30	-1	20519270	100%	
VISITALL-OPT11 (20)	11	-1	1991169	100%	
Remaining domains (980)	544	$\pm 0$	436017004	93%	
SUM (1396)	763	+39	670278179	77%	

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## Cond

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nclusion	BURG				
	FRE				
Need for techniques orthogonal to heuristic search,	Motivation Preliminaries				
complementing heuristics.	Stubborn Sets				
One idea: Commit to one order of operators if they are independent. Prune other orders.					
Class of such techniques: partial-order reduction (POR	R)				
One such technique: strong/weak stubborn sets					
Can lead to substantial pruning compared to plain A*.					
Many other POR techniques exist.					
Other pruning techniques exist as well, e.g., symmetry reduction.					
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