

# Principles of AI Planning

## 12. Planning with State-Dependent Action Costs

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# Background

## Background

- State-Dependent  
Action Costs
- Edge-Valued  
Multi-Valued  
Decision Diagrams

## Compilation

## Relaxations

## Abstractions

## Summary

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- We now know the **basics of classical planning**.
- Where to go from here? **Possible routes:**
  - Algorithms: techniques orthogonal to heuristic search (**partial-order reduction**, symmetry reduction, decompositions, ...)  
    ↪ later
  - Algorithms: techniques other than heuristic search (SAT/SMT planning, BDD-based symbolic planning, ...)  
    ↪ beyond the scope of this course
  - Settings beyond classical planning (**nondeterminism**, partial observability, numeric planning, ...)  
    ↪ later
  - A slight extension to the expressiveness of classical planning tasks  
    ↪ **this chapter**

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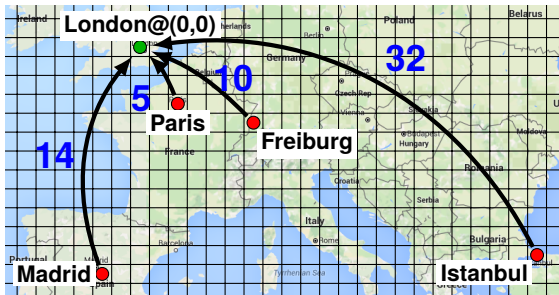
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# What are State-Dependent Action Costs?



Action costs:

unit

constant

state-dependent

$$\begin{aligned} \text{cost}(\text{fly}(\text{Madrid}, \text{London})) &= 1, & \text{cost}(\text{fly}(\text{Paris}, \text{London})) &= 1, \\ \text{cost}(\text{fly}(\text{Freiburg}, \text{London})) &= 1, & \text{cost}(\text{fly}(\text{Istanbul}, \text{London})) &= 1. \end{aligned}$$

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# Why Study State-Dependent Action Costs?



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- In classical planning: actions have **unit costs**.
  - Each action  $a$  costs 1.
- Simple extension: actions have **constant costs**.
  - Each action  $a$  costs some  $cost_a \in \mathbb{N}$ .
  - Example: Flying between two cities costs amount proportional to distance.
  - Still easy to handle algorithmically, e. g. when computing  $g$  and  $h$  values.
- Further extension: actions have **state-dependent costs**.
  - Each action  $a$  has **cost function**  $cost_a : S \rightarrow \mathbb{N}$ .
  - Example: Flying to a destination city costs amount proportional to distance, depending on the current city.

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# Why Study State-Dependent Action Costs?

- Human perspective:
  - “natural”, “elegant”, and “higher-level”
  - **modeler-friendly**  $\rightsquigarrow$  less error-prone?
- Machine perspective:
  - more **structured**  $\rightsquigarrow$  exploit structure in algorithms?
  - fewer redundancies, exponentially more **compact**
- Language support:
  - numeric **PDDL**, PDDL 3
  - **RDDL**, **MDPs** (state-dependent rewards!)
- Applications:
  - modeling **preferences** and **soft goals**
  - application domains such as **PSR**

(**Abbreviation:** SDAC = state-dependent action costs)

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## Good news:

- Computing ***g* values** in forward search still **easy**.  
(When expanding state  $s$  with action  $a$ , we know  $cost_a(s)$ .)

## Challenge:

- But what about **SDAC-aware *h* values** (relaxation heuristics, abstraction heuristics)?
- Or can we simply **compile SDAC away**?

## This chapter:

- Proposed **answers** to these challenges.

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## Roadmap:

- 1 Look at **compilations**.
- 2 This leads to **edge-valued multi-valued decision diagrams** (EVMDDs) as data structure to represent cost functions.
- 3 Based on EVMDDs, formalize and discuss:
  - compilations
  - relaxation heuristics
  - abstraction heuristics

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## Definition

A **SAS<sup>+</sup> planning task with state-dependent action costs** or **SDAC planning task** is a tuple  $\Pi = \langle V, I, O, \gamma, (cost_a)_{a \in O} \rangle$  where  $\langle V, I, O, \gamma \rangle$  is a (regular) SAS<sup>+</sup> planning task with state set  $S$  and  $cost_a : S \rightarrow \mathbb{N}$  is the **cost function** of  $a$  for all  $a \in O$ .

**Assumption:** For each  $a \in O$ , the set of variables occurring in the precondition of  $a$  is disjoint from the set of variables on which the cost function  $cost_a$  depends.

**(Question:** Why is this assumption unproblematic?)

Definitions of plans etc. stay as before. A plan is **optimal** if it minimizes the sum of action costs from start to goal.

For the rest of this chapter, we consider the following running example.

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## Example (Household domain)

### Actions:

$\text{vacuumFloor} = \langle \top, \text{floorClean} \rangle$

$\text{washDishes} = \langle \top, \text{dishesClean} \rangle$

$\text{doHousework} = \langle \top, \text{floorClean} \wedge \text{dishesClean} \rangle$

### Cost functions:

$\text{cost}_{\text{vacuumFloor}} = [\neg \text{floorClean}] \cdot 2$

$\text{cost}_{\text{washDishes}} = [\neg \text{dishesClean}] \cdot (1 + 2 \cdot [\neg \text{haveDishwasher}])$

$\text{cost}_{\text{doHousework}} = \text{cost}_{\text{vacuumFloor}} + \text{cost}_{\text{washDishes}}$

(**Question:** How much can applying action washDishes cost?)

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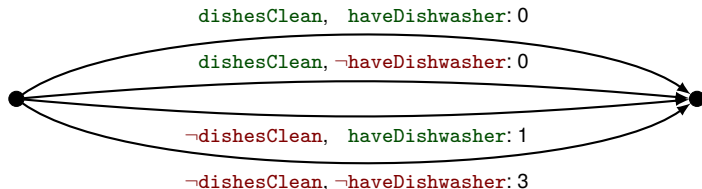
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Different ways of compiling SDAC away:

- **Compilation I:** “Parallel Action Decomposition”
- **Compilation II:** “Purely Sequential Action Decomposition”
- **Compilation III:** “EVMDD-Based Action Decomposition”  
(combination of Compilations I and II)

### Example



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$$\text{washDishes}(\text{dC}, \text{hD}) = \langle \text{dC} \wedge \text{hD}, \text{dC} \rangle, \quad \text{cost} = 0$$

$$\text{washDishes}(\text{dC}, \neg \text{hD}) = \langle \text{dC} \wedge \neg \text{hD}, \text{dC} \rangle, \quad \text{cost} = 0$$

$$\text{washDishes}(\neg \text{dC}, \text{hD}) = \langle \neg \text{dC} \wedge \text{hD}, \text{dC} \rangle, \quad \text{cost} = 1$$

$$\text{washDishes}(\neg \text{dC}, \neg \text{hD}) = \langle \neg \text{dC} \wedge \neg \text{hD}, \text{dC} \rangle, \quad \text{cost} = 3$$

### Compilation I

Transform each action into multiple actions:

- one for each partial state relevant to cost function
- add partial state to precondition
- use cost for partial state as constant cost

Properties:

- ✓ always possible
- ✗ exponential blow-up

Question: Exponential blow-up avoidable?  $\leadsto$  Compilation II

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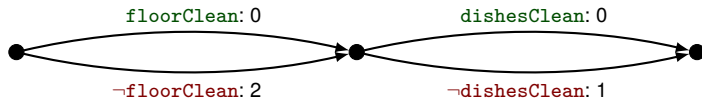
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### Example

Assume we own a dishwasher:

$$\text{cost}_{\text{doHousework}} = 2 \cdot [\neg \text{floorClean}] + [\neg \text{dishesClean}]$$



$$\text{doHousework}_1(\text{fC}) = \langle \text{fC}, \text{fC} \rangle, \quad \text{cost} = 0$$

$$\text{doHousework}_1(\neg \text{fC}) = \langle \neg \text{fC}, \text{fC} \rangle, \quad \text{cost} = 2$$

$$\text{doHousework}_2(\text{dC}) = \langle \text{dC}, \text{dC} \rangle, \quad \text{cost} = 0$$

$$\text{doHousework}_2(\neg \text{dC}) = \langle \neg \text{dC}, \text{dC} \rangle, \quad \text{cost} = 1$$

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## Compilation II

If costs are **additively decomposable/separable**:

- high-level actions  $\approx$  **macro actions**
- decompose into **sequential micro actions**

### Properties:

- ✓ only **linear** blow-up
- ✗ **not always possible**
- plan lengths not preserved

E. g., in a state where  $\neg fC$  and  $\neg dC$  hold, an application of

`doHousework`

in the SDAC setting is replaced by an application of the action **sequence**

$\text{doHousework}_1(\neg fC), \text{doHousework}_2(\neg dC)$

in the compiled setting.

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### Properties (ctd.):

- plan costs preserved
- blow-up in search space

E. g., in a state where  $\neg fC$  and  $\neg dC$  hold, should we apply  $\text{doHousework}_1(\neg fC)$  or  $\text{doHousework}_2(\neg dC)$  first?

$\rightsquigarrow$  impose action ordering!

- attention: we should apply all partial effects at end!  
Otherwise, an effect of an earlier action in the compilation might affect the cost of a later action in the compilation.

**Question:** Can this **always work** (kind of)?  $\rightsquigarrow$  Compilation III

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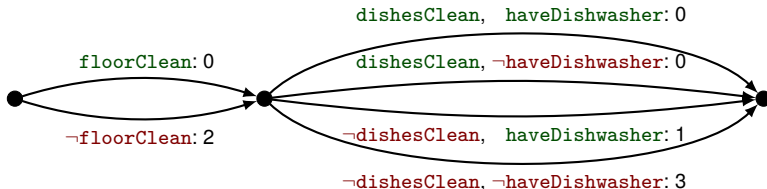
References

### Example

$$\text{cost}_{\text{doHousework}} = [\neg \text{floorClean}] \cdot 2 +$$

---

$$[\neg \text{dishesClean}] \cdot (1 + 2 \cdot [\neg \text{haveDishwasher}])$$



**Simplify** right-hand part of diagram:

- **Branch over single variable** at a time.
- Exploit: haveDishwasher **irrelevant** if dishesClean is true.

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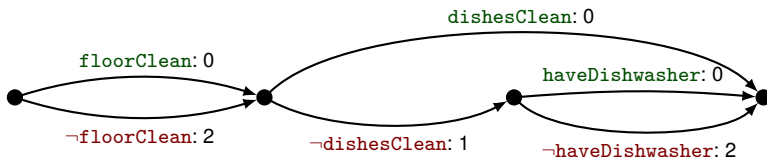
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### Example (ctd.)



### Later:

- Compiled actions
- Auxiliary variables to enforce action ordering

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### Compilation III

- exploit as much **additive separability** as possible
- **multiply out variable domains** where inevitable
- **Technicalities:**
  - fix **variable ordering**
  - perform **Shannon** and **isomorphism reduction**  
(cf. theory of BDDs)

### Properties:

- ✓ **always possible**
- **worst-case exponential** blow-up, but **as good as it gets**
- as with Compilation II: plan lengths not preserved, plan costs preserved
- as with Compilation II: action ordering, all effects at end!

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Compilation III provides **optimal** combination of sequential and parallel action decomposition, given fixed variable ordering.

**Question:** How to find such decompositions **automatically**?

**Answer:** Figure for Compilation III basically a **reduced ordered edge-valued multi-valued decision diagram (EVMDD)**!

[Lai et al., 1996; Ciardo and Siminiceanu, 2002]

### EVMDDs:

- Decision diagrams for arithmetic functions
- Decision nodes with associated decision variables
- Edge weights: partial costs contributed by facts
- Size of EVMDD **compact** in many “typical”, well-behaved cases (**Question**: For example?)

### Properties:

- ✓ **satisfy all requirements** for Compilation III, even (almost) uniquely determined by them
- ✓ already have **well-established theory and tool support**
- ✓ **detect and exhibit additive structure** in arithmetic functions

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### Consequence:

- represent cost functions as **EVMDDs**
- **exploit** additive structure exhibited by them
- draw on theory and tool support for EVMDDs

### Two perspectives on EVMDDs:

- graphs specifying how to **decompose** action costs
- data structures **encoding** action costs  
(used **independently from compilations**)

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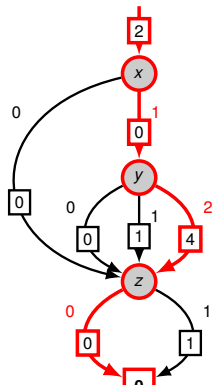
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### Example (EVMDD Evaluation)

$$cost_a = xy^2 + z + 2$$

$$\mathcal{D}_x = \mathcal{D}_z = \{0, 1\}, \quad \mathcal{D}_y = \{0, 1, 2\}$$



- Directed acyclic graph
- Dangling incoming edge
- Single **terminal node 0**
- **Decision nodes** with:
  - decision variables
  - edge label
  - edge weights
- We see:  $z$  independent from rest,  $y$  only matters if  $x \neq 0$ .
- $s = \{x \mapsto 1, y \mapsto 2, z \mapsto 0\}$

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### Properties of EVMDDs:

- ✓ Existence for finitely many finite-domain variables
- ✓ Uniqueness/canonicity if reduced and ordered
- ✓ Basic arithmetic operations supported

(Lai et al., 1996; Ciardo and Siminiceanu, 2002)

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Given arithmetic operator  $\otimes \in \{+, -, \cdot, \dots\}$ , EVMDDs  $\mathcal{E}_1, \mathcal{E}_2$ .  
Compute EVMDD  $\mathcal{E} = \mathcal{E}_1 \otimes \mathcal{E}_2$ .

**Implementation:** procedure **apply**( $\otimes, \mathcal{E}_1, \mathcal{E}_2$ ):

- **Base case:** single-node EVMDDs encoding constants
- **Inductive case:** apply  $\otimes$  recursively:
  - push down edge weights
  - recursively apply  $\otimes$  to corresponding children
  - pull up excess edge weights from children

**Time complexity [Lai et al., 1996]:**

- **additive operations:** product of input EVMDD sizes
- **in general:** exponential

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**Idea:** each edge in the EVMDD becomes a new micro action with constant cost corresponding to the edge constraint, precondition that we are currently at its start EVMDD node, and effect that we are currently at its target EVMDD node.

## Example (EVMDD-based action compilation)

Let  $a = \langle \chi, e \rangle$ ,  $cost_a = xy^2 + z + 2$ .

Auxiliary variables:

- One **semaphore variable**  $\sigma$  with  $\mathcal{D}_\sigma = \{0, 1\}$  for entire planning task.
- One **auxiliary variable**  $\alpha = \alpha_a$  with  $\mathcal{D}_{\alpha_a} = \{0, 1, 2, 3, 4\}$  for action  $a$ .

Replace  $a$  by new auxiliary actions (similarly for other actions).

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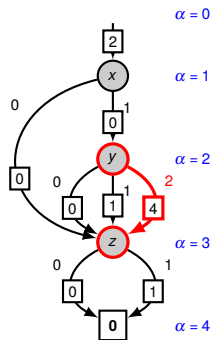
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## Example (EVMDD-based action compilation, ctd.)



$$a^{\chi} = \langle \chi \wedge \sigma = 0 \wedge \alpha = 0, \\ \sigma := 1 \wedge \alpha := 1 \rangle,$$

cost = 2

$$a^{1,x=0} = \langle \alpha = 1 \wedge x = 0, \alpha := 3 \rangle,$$

cost = 0

$$a^{1,x=1} = \langle \alpha = 1 \wedge x = 1, \alpha := 2 \rangle,$$

cost = 0

$$a^{2,y=0} = \langle \alpha = 2 \wedge y = 0, \alpha := 3 \rangle,$$

cost = 0

$$a^{2,y=1} = \langle \alpha = 2 \wedge y = 1, \alpha := 3 \rangle,$$

cost = 1

$$a^{2,y=2} = \langle \alpha = 2 \wedge y = 2, \alpha := 3 \rangle,$$

cost = 4

$$a^{3,z=0} = \langle \alpha = 3 \wedge z = 0, \alpha := 4 \rangle,$$

cost = 0

$$a^{3,z=1} = \langle \alpha = 3 \wedge z = 1, \alpha := 4 \rangle,$$

cost = 1

$$a^e = \langle \alpha = 4, e \wedge \sigma := 0 \wedge \alpha := 0 \rangle,$$

cost = 0

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## Definition (EVMDD-based action compilation)

Let  $\Pi = \langle V, I, O, \gamma, (cost_a)_{a \in O} \rangle$  be an SDAC planning task, and for each action  $a \in O$ , let  $\mathcal{E}_a$  be an EVMDD that encodes the cost function  $cost_a$ .

Let  $EAC(a)$  be the set of actions created from  $a$  using  $\mathcal{E}_a$  similar to the previous example. Then the **EVMDD-based action compilation** of  $\Pi$  using  $\mathcal{E}_a$ ,  $a \in O$ , is the task

$\Pi' = EAC(\Pi) = \langle V', I', O', \gamma' \rangle$ , where

- $V' = V \cup \{\sigma\} \cup \{\alpha_a \mid a \in O\}$ ,
- $I' = I \cup \{\sigma \mapsto 0\} \cup \{\alpha_a \mapsto 0 \mid a \in O\}$ ,
- $O' = \bigcup_{a \in O} EAC(a)$ , and
- $\gamma' = \gamma \wedge (\sigma = 0) \wedge \bigwedge_{a \in O} (\alpha_a = 0)$ .

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Let  $\Pi$  be an SDAC task and  $\Pi' = EAC(\Pi)$  its EVMDD-based action compilation (for appropriate EVMDDs  $\mathcal{E}_a$ ).

## Proposition

$\Pi'$  has only state-independent costs.

### Proof.

By construction. □

## Proposition

The size  $\|\Pi'\|$  is in the order  $O(\|\Pi\| \cdot \max_{a \in O} \|\mathcal{E}_a\|)$ , i. e. **polynomial** in the size of  $\Pi$  and the largest used EVMDD.

### Proof.

By construction. □

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Let  $\Pi$  be an SDAC task and  $\Pi' = EAC(\Pi)$  its EVMDD-based action compilation (for appropriate EVMDDs  $\mathcal{E}_a$ ).

## Proposition

$\Pi$  and  $\Pi'$  admit the same plans (up to replacement of actions by action **sequences**). Optimal plan costs are preserved.

## Proof.

Let  $\pi = a_1, \dots, a_n$  be a plan for  $\Pi$ , and let  $s_0, \dots, s_n$  be the corresponding state sequence such that  $a_i$  is applicable in  $s_{i-1}$  and leads to  $s_i$  for all  $i = 1, \dots, n$ .

For each  $i = 1, \dots, n$ , let  $\mathcal{E}_{a_i}$  be the EVMDD used to compile  $a_i$ . State  $s_{i-1}$  determines a unique path through the EVMDD  $\mathcal{E}_{a_i}$ , which uniquely corresponds to an action sequence  $a_i^0, \dots, a_i^{k_i}$  (for some  $k_i \in \mathbb{N}$ ; including  $a_i^x$  and  $a_i^e$ ).

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## Proof (ctd.)

By construction,  $cost(a_i^0) + \dots + cost(a_i^{k_i}) = cost_{a_i}(s_{i-1})$ .

Moreover, the sequence  $a_i^0, \dots, a_i^{k_i}$  is applicable in  $s_{i-1} \cup \{\sigma \mapsto 0\} \cup \{\alpha_a \mapsto 0 \mid a \in O\}$  and leads to  $s_i \cup \{\sigma \mapsto 0\} \cup \{\alpha_a \mapsto 0 \mid a \in O\}$ .

Therefore, by induction,  $\pi' = a_1^0, \dots, a_1^{k_1}, \dots, a_n^0, \dots, a_n^{k_n}$  is applicable in  $s_0 \cup \{\sigma \mapsto 0\} \cup \{\alpha_a \mapsto 0 \mid a \in O\}$  (and leads to a goal state). Moreover,

$$cost(\pi') = cost(a_1^0) + \dots + cost(a_1^{k_1}) + \dots + cost(a_n^0) + \dots + cost(a_n^{k_n}) = cost_{a_1}(s_0) + \dots + cost_{a_n}(s_{n-1}) = cost(\pi).$$

Still to show:  $\Pi'$  admits no other plans. It suffices to see that the semaphore  $\sigma$  prohibits interleaving more than one EVMDD evaluation, and that each  $\alpha_a$  makes sure that the EVMDD for  $a$  is traversed in the unique correct order. □

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## Example

Let  $\Pi = \langle V, I, O, \gamma \rangle$  with  $V = \{x, y, z, u\}$ ,  $\mathcal{D}_x = \mathcal{D}_z = \{0, 1\}$ ,  
 $\mathcal{D}_y = \mathcal{D}_u = \{0, 1, 2\}$ ,  $I = \{x \mapsto 1, y \mapsto 2, z \mapsto 0, u \mapsto 0\}$ ,  
 $O = \{a, b\}$ , and  $\gamma = (u = 2)$  with

$$\begin{aligned} a &= \langle u = 0, u := 1 \rangle, & cost_a &= xy^2 + z + 2, \\ b &= \langle u = 1, u := 2 \rangle, & cost_b &= z + 1. \end{aligned}$$

Optimal plan for  $\Pi$ :

$$\pi = a, b \text{ with } cost(\pi) = 6 + 1 = 7.$$

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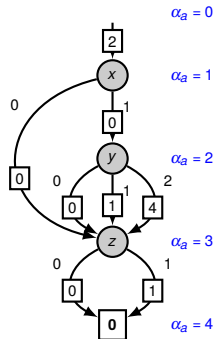
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## Example (Ctd.)

Compilation of  $a$ :



$$a^{\chi} = \langle u = 0 \wedge \sigma = 0 \wedge \alpha_a = 0, \\ \sigma := 1 \wedge \alpha_a := 1 \rangle,$$

$$a^{1,x=0} = \langle \alpha_a = 1 \wedge x = 0, \alpha_a := 3 \rangle,$$

$$a^{1,x=1} = \langle \alpha_a = 1 \wedge x = 1, \alpha_a := 2 \rangle,$$

$$a^{2,y=0} = \langle \alpha_a = 2 \wedge y = 0, \alpha_a := 3 \rangle,$$

$$a^{2,y=1} = \langle \alpha_a = 2 \wedge y = 1, \alpha_a := 3 \rangle,$$

$$a^{2,y=2} = \langle \alpha_a = 2 \wedge y = 2, \alpha_a := 3 \rangle,$$

$$a^{3,z=0} = \langle \alpha_a = 3 \wedge z = 0, \alpha_a := 4 \rangle,$$

$$a^{3,z=1} = \langle \alpha_a = 3 \wedge z = 1, \alpha_a := 4 \rangle,$$

$$a^e = \langle \alpha_a = 4, u := 1 \wedge \sigma := 0 \wedge \alpha_a := 0 \rangle, \quad cost = 0$$

$$cost = 2$$

$$cost = 0$$

$$cost = 0$$

$$cost = 0$$

$$cost = 1$$

$$cost = 4$$

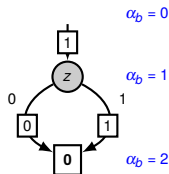
$$cost = 0$$

$$cost = 1$$

$$cost = 0$$

## Example (Ctd.)

Compilation of  $b$ :



$$b^x = \langle u = 1 \wedge \sigma = 0 \wedge \alpha_b = 0, \\ \sigma := 1 \wedge \alpha_b := 1 \rangle,$$

$$cost = 1$$

$$b^{1,z=0} = \langle \alpha_b = 1 \wedge z = 0, \alpha_b := 2 \rangle,$$

$$cost = 0$$

$$b^{1,z=1} = \langle \alpha_b = 1 \wedge z = 1, \alpha_b := 2 \rangle,$$

$$cost = 1$$

$$b^e = \langle \alpha_b = 2, u := 2 \wedge \sigma := 0 \wedge \alpha_b := 0 \rangle, \quad cost = 0$$

Optimal plan for  $\Pi'$  (with  $cost(\pi') = 6 + 1 = 7 = cost(\pi)$ ):

$$\pi' = \underbrace{a^x, a^{1,x=1}, a^{2,y=2}, a^{3,z=0}, a^e}_{cost=2+0+4+0+0=6}, \underbrace{b^x, b^{1,z=0}, b^e}_{cost=1+0+0=1}.$$



- Okay. We can compile SDAC away somewhat efficiently. Is this the end of the story?
- No! Why not?
  - Tighter integration of SDAC into planning process might be beneficial.
  - Analysis of heuristics for SDAC might improve our understanding.
- Consequence: Let's study heuristics for SDAC in uncompiled setting.



# Relaxations

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**We know:** Delete-relaxation heuristics informative in classical planning.

**Question:** Are they also informative in SDAC planning?

- Assume we want to compute the **additive heuristic**  $h^{add}$  in a task with state-dependent action costs.
- But what does an action  $a$  cost in a relaxed state  $s^+$ ?
- And how to compute that cost?

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Delete relaxation in SAS<sup>+</sup> tasks works as follows:

- Operators are already in effect normal form.
- We do not need to impose a positive normal form, because all conditions are conjunctions of facts, and facts are just variable-value pairs and hence always positive.
- Hence  $a^+ = a$  for any operator  $a$ , and  $\Pi^+ = \Pi$ .
- For simplicity, we identify relaxed states  $s^+$  with their on-sets  $on(s^+)$ .
- Then, a relaxed state  $s^+$  is a set of facts  $(v, d)$  with  $v \in V$  and  $d \in \mathcal{D}_v$  including at least one fact  $(v, d)$  for each  $v \in V$  (but possibly more than one, which is what makes it a **relaxed** state).

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- A relaxed operator  $a$  is applicable in a relaxed state  $s^+$  if all precondition facts of  $a$  are contained in  $s^+$ .
- Relaxed states **accumulate** facts reached so far.
- Applying a relaxed operator  $a$  to a relaxed state  $s^+$  adds to  $s^+$  those facts made true by  $a$ .

## Example

Relaxed operator  $a^+ = \langle x = 2, y := 1 \wedge z := 0 \rangle$  is applicable in relaxed state  $s^+ = \{(x, 0), (x, 2), (y, 0), (z, 1)\}$ , because precondition  $(x, 2) \in s^+$ , and leads to successor  $(s^+)' = s^+ \cup \{(y, 1), (z, 0)\}$ .

Relaxed plans, dominance, monotonicity etc. as before. The above definition generalizes the one for propositional tasks.

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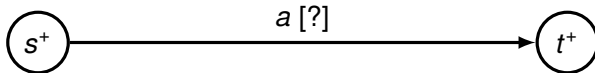
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## Example

Assume  $s^+$  is the relaxed state with

$$s^+ = \{(x, 0), (x, 1), (y, 1), (y, 2), (z, 0)\}.$$

What should action  $a$  with  $cost_a = xy^2 + z + 2$  cost in  $s^+$ ?



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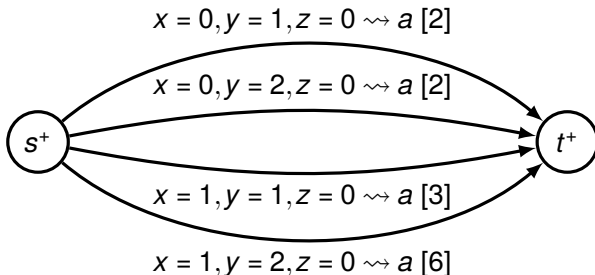
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**Idea:** We should assume the **cheapest** way of applying  $o^+$  in  $s^+$  to guarantee admissibility of  $h^+$ .

(Allow at least the behavior of the unrelaxed setting at no higher cost.)

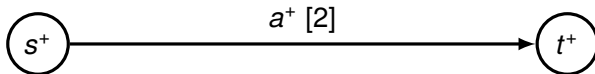
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**Idea:** We should assume the **cheapest** way of applying  $o^+$  in  $s^+$  to guarantee admissibility of  $h^+$ .

(Allow at least the behavior of the unrelaxed setting at no higher cost.)

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## Definition

Let  $V$  be a set of FDR variables,  $s : V \rightarrow \bigcup_{v \in V} \mathcal{D}_v$  an unrelaxed state over  $V$ , and  $s^+ \subseteq \{(v, d) \mid v \in V, d \in \mathcal{D}_v\}$  a relaxed state over  $V$ . We call  $s$  **consistent** with  $s^+$  if  $\{(v, s(v)) \mid v \in V\} \subseteq s^+$ .

## Definition

Let  $a \in O$  be an action with cost function  $cost_a$ , and  $s^+$  a relaxed state. Then the **relaxed cost** of  $a$  in  $s^+$  is defined as

$$cost_a(s^+) = \min_{s \in S \text{ consistent with } s^+} cost_a(s).$$

(**Question:** How many states  $s$  are consistent with  $s^+$ ?)

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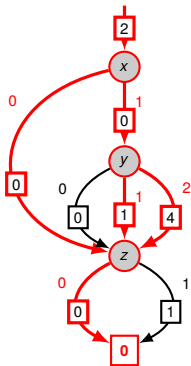
**Problem with this definition:** There are generally **exponentially** many states  $s$  consistent with  $s^+$  to minimize over.

**Central question:** Can we still do this minimization efficiently?

**Answer:** Yes, at least efficiently in the size of an EVMDD encoding  $cost_a$ .

## Example

Relaxed state  $s^+ = \{(x, 0), (x, 1), (y, 1), (y, 2), (z, 0)\}$ .



- Computing  $cost_a(s^+) =$  minimizing over  $cost_a(s)$  for all  $s$  consistent with  $s^+ =$  minimizing over all start-end-**paths** in EVMD following only edges consistent with  $s^+$ .
- **Observation:** Minimization over exponentially many paths can be replaced by **top-sort traversal of EVMD**, minimizing over incoming arcs consistent with  $s^+$  at all nodes!

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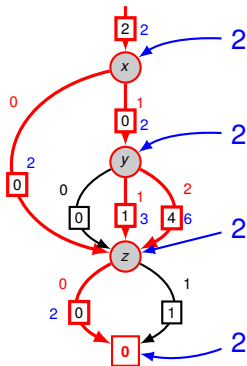
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## Example

Relaxed state  $s^+ = \{(x, 0), (x, 1), (y, 1), (y, 2), (z, 0)\}$ .



■  $cost_a(s^+) = 2$

■ Cost-minimizing  $s$  consistent with  $s^+$ :  $s(x) = s(z) = 0$ ,  $s(y) \in \{1, 2\}$ .

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## Theorem

*A top-sort traversal of the EVMDD for  $\text{cost}_a$ , adding edge weights and minimizing over incoming arcs consistent with  $s^+$  at all nodes, computes  $\text{cost}_a(s^+)$  and takes time in the order of the size of the EVMDD.*

## Proof.

Homework?



The following definition is equivalent to the RPG-based one.

Definition (Classical additive heuristic  $h^{add}$ )

$$\begin{aligned}h^{add}(s) &= h_s^{add}(GoalFacts) \\h_s^{add}(Facts) &= \sum_{fact \in Facts} h_s^{add}(fact) \\h_s^{add}(fact) &= \begin{cases} 0 & \text{if } fact \in s \\ \min_{\text{achiever } a \text{ of } fact} [h_s^{add}(pre(a)) + \text{cost}_a] & \text{otherwise} \end{cases}\end{aligned}$$

Question: How to generalize  $h^{add}$  to SDAC?

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## Example

$$a = \langle \top, x = 1 \rangle$$

$$cost_a = 2 - 2y$$

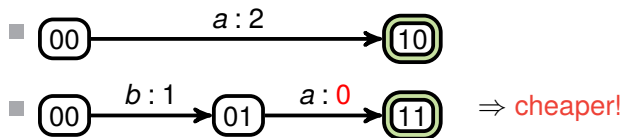
$$b = \langle \top, y = 1 \rangle$$

$$cost_b = 1$$

$$s = \{x \mapsto 0, y \mapsto 0\}$$

$$h_s^{add}(y = 1) = 1$$

$$h_s^{add}(x = 1) = ?$$



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(Here, we need the assumption that no variable occurs both in the cost function and the precondition of the same action):

Definition (Additive heuristic  $h^{add}$  for SDAC)

$$h_s^{add}(fact) = \begin{cases} 0 & \text{if } fact \in s \\ \min_{\text{achiever } a \text{ of } fact} [h_s^{add}(pre(a)) + \text{cost}_a] & \text{otherwise} \end{cases}$$

$$h_s^{add}(fact)$$

$$= \begin{cases} 0 \\ \min_{\text{achiever } a \text{ of } fact} \end{cases}$$

$$Cost_a^s = \min_{\hat{s} \in S_a} [cost_a(\hat{s}) + h_s^{add}(\hat{s})]$$

$S_a$ : set of partial states over variables in cost function

$|S_a|$  **exponential** in number of variables in cost function

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## Theorem

*Let  $\Pi$  be an SDAC planning task, let  $\Pi'$  be an EVMDD-based action compilation of  $\Pi$ , and let  $s$  be a state of  $\Pi$ . Then the classical  $h^{add}$  heuristic in  $\Pi'$  gives the same value for  $s \cup \{\sigma \mapsto 0\} \cup \{\alpha_a \mapsto 0 \mid a \in O\}$  as the generalization of  $h^{add}$  to SDAC tasks defined above gives for  $s$  in  $\Pi$ .  $\square$*

## Computing $h^{add}$ for SDAC:

- **Option 1:** Compute classical  $h^{add}$  on compiled task.
- **Option 2:** Compute  $Cost_a^s$  directly. How?
  - Plug EVMDDs as subgraphs into RPG
  - $\rightsquigarrow$  efficient computation of  $h^{add}$

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**Remark:** We can use EVMDDs to compute  $C_s^a$  and hence the generalized additive heuristic directly, by embedding them into the relaxed planning task.

We just briefly show the example, without going into too much detail.

**Idea:** Augment EVMDD with input nodes representing  $h^{add}$  values from the previous RPG layer.

- Use augmented diagrams as RPG subgraphs.
- Allows efficient computation of  $h^{add}$ .

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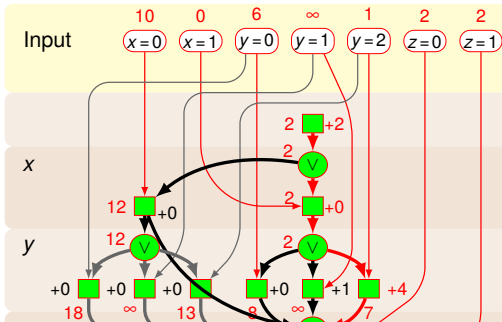
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# Option 2: RPG Compilation Option 2: Computing $Cost_a^s$



Evaluate nodes:

- $cost_a = xy^2 + z + 2$
- variable nodes become V-nodes
- weights become  $\wedge$ -nodes
- Augment with input nodes
- Ensure complete evaluation
- Insert  $h^{add}$  values
- $\wedge$ :  $\sum(\text{parents}) + \text{weight}$
- $\vee$ :  $\min(\text{parents})$
- $Cost_a^s =$

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- Use above construction as subgraph of RPG in each layer, for each action (as operator subgraphs).
- Add AND nodes conjoining these subgraphs with operator precondition graphs.
- Link EVMDD outputs to next proposition layer.

## Theorem

*Let  $\Pi$  be an SDAC planning task. Then the classical additive RPG evaluation of the RPG constructed using EVMDDs as above computes the generalized additive heuristic  $h^{add}$  defined before.*

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# Abstractions

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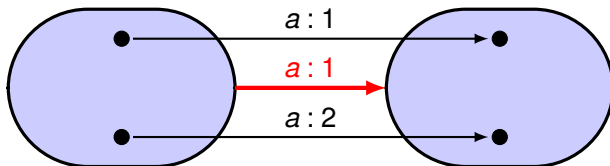
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**Question:** Why consider **abstraction heuristics**?

**Answer:**

- admissibility
- $\rightsquigarrow$  **optimality**



**Question:** What are the **abstract action costs**?

**Answer:** For **admissibility**, abstract cost of  $a$  should be

$$cost_a(s^{abs}) = \min_{\substack{\text{concrete state } s \\ \text{abstracted to } s^{abs}}} cost_a(s).$$

**Problem:** exponentially many states in minimization

**Aim:** Compute  $cost_a(s^{abs})$  efficiently  
(given EVMDD for  $cost_a(s)$ ).

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We will see: possible if the abstraction is **Cartesian** or coarser.

(Includes projections and domain abstractions.)

## Definition (Cartesian abstraction)

A set of states  $s^{\text{abs}}$  is **Cartesian** if it is of the form

$$D_1 \times \cdots \times D_n,$$

where  $D_i \subseteq \mathcal{D}_i$  for all  $i = 1, \dots, n$ .

An abstraction is Cartesian if all abstract states are Cartesian sets.

[Seipp and Helmert, 2013]

**Intuition:** Variables are abstracted **independently**.

$\rightsquigarrow$  **exploit independence** when computing abstract costs!

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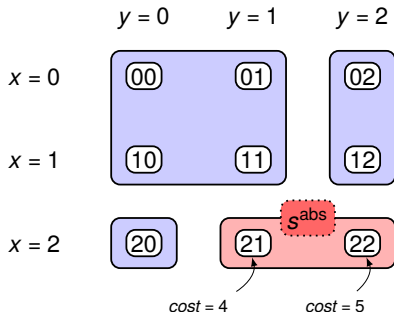
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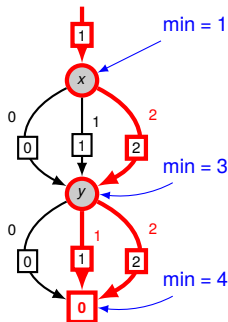
## Example (Cartesian abstraction)

Cartesian abstraction over  $x, y$



Cost  $x + y + 1$

(edges consistent with  $s^{abs}$ )



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Why does the topsort EVMDD traversal (cheapest path computation) correctly compute  $cost_a(s^{abs})$ ?

**Short answer:** The exact same thing as with relaxed states, because **relaxed states are Cartesian sets!**

**Longer answer:**

- 1 For each Cartesian state  $s^{abs}$  and each variable  $v$ , each value  $d \in \mathcal{D}_v$  is either **consistent** with  $s^{abs}$  or not.
- 2 This implies: at all decision nodes associated with variable  $v$ , some outgoing edges are **enabled**, others are **disabled**. This is **independent** from all other decision nodes.
- 3 This allows **local minimizations** over linearly many **edges** instead of **global minimization** over exponentially many **paths** in the EVMDD when computing minimum costs.

$\rightsquigarrow$  **polynomial** in EVMDD size!

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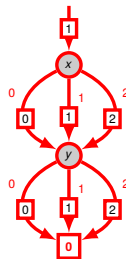
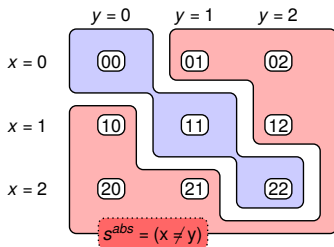
If abstraction **not Cartesian**: two variables can be

- **independent** in cost function ( $\rightsquigarrow$  compact EVMDD), but
- **dependent** in abstraction.

$\rightsquigarrow$  cannot consider independent parts of EVMDD separately.

## Example (Non-Cartesian abstraction)

$cost : x + y + 1$ ,  $cost(s^{abs}) = 2$ , local minim.:  $1 \rightsquigarrow$  underestimate!



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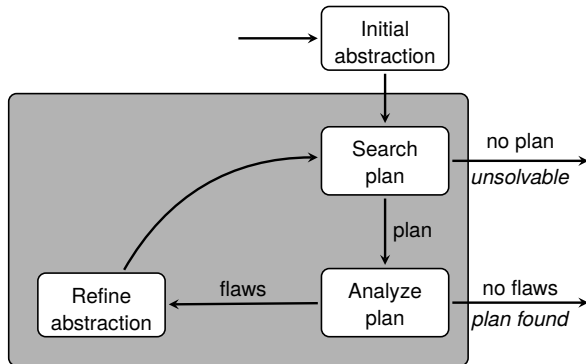
# Counterexample-Guided Abstraction Refinement



**Wanted:** principled way of **computing Cartesian abstractions**.

~~~> **Counterexample-Guided Abstraction Refinement (CEGAR)**

[Clarke et al., 2000] [Seipp and Helmert, 2013]



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Assume the following:

- **Initial abstraction** is one-state abstraction with single abstract state  $\mathcal{D}_1 \times \dots \times \mathcal{D}_n$ .  
 $\rightsquigarrow$  **Cartesian abstraction**
- Each **refinement step** takes one abstract state  $s^{\text{abs}} = D_1 \times \dots \times D_n$ , one variable  $v_i$ , and splits  $s^{\text{abs}}$  into
  - $D_1 \times \dots \times D_{i-1} \times D'_i \times D_{i+1} \times \dots \times D_n$
  - $D_1 \times \dots \times D_{i-1} \times D''_i \times D_{i+1} \times \dots \times D_n$such that  $D'_i \cap D''_i = \emptyset$  and  $D'_i \cup D''_i = D_i$ .  
 $\rightsquigarrow$  still a **Cartesian abstraction**

So, inductively:

- Initial abstraction is Cartesian.
- Each refinement step preserves being Cartesian.
- $\rightsquigarrow$  **All generated abstractions are Cartesian.**

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## Some questions:

- Q: **When** to split abstract states?  
A: When first **flaw** is identified. (Details below.)
- Q: **How** to split abstract states?  
A: So as to **resolve that flaw**. (Details below.)

## Some questions:

- Q: **How long** to stay in refinement loop?
- A: Until one of the following **termination criteria** is met:
  - **No abstract plan** exists.
    - ↪ Terminate with result “unsolvable”.
  - Abstract plan  $\pi$  is **concretizable** (= has no flaw).
    - ↪ Return  $\pi$  as concrete plan.
  - Available **resources** (time, memory, abstraction size bound, ...) exhausted.
    - ↪ Use current abstraction as basis for **abstraction heuristic** for concrete planning task (i. e., compute abstract goal distances, store in lookup table, ...).

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## Example (one package, one truck)

Consider the following FDR planning task  $\langle V, I, O, \gamma \rangle$ :

- $V = \{t, p\}$  with
  - $\mathcal{D}_t = \{L, R\}$
  - $\mathcal{D}_p = \{L, T, R\}$
- $I = \{t \mapsto L, p \mapsto L\}$
- $O = \{pick\text{-}in_i \mid i \in \{L, R\}\} \cup \{drop\text{-}in_i \mid i \in \{L, R\}\} \cup \{move_{i,j} \mid i, j \in \{L, R\}, i \neq j\}$ , where
  - $pick\text{-}in_i = \langle t = i \wedge p = i, p := T \rangle$
  - $drop\text{-}in_i = \langle t = i \wedge p = T, p := i \rangle$
  - $move_{i,j} = \langle t = i, t := j \rangle$
- $\gamma = (p = R)$ .

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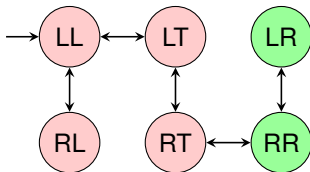
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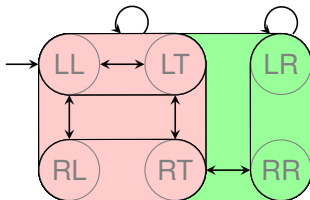
## Example (Ctd.)

Before we look at CEGAR applied to this task, here is the concrete transition system (just for reference):

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## Example (Ctd.)

Refinement step 0 (initial abstraction):    Refinement step 1:  
Refinement step 2:    Refinement step 3:    Refinement step 4:



**Abstract plan:**

$$\pi_0 = \langle \rangle \pi_1 = \langle \text{drop-in}_R \rangle \pi_2 = \langle \text{move}_{L,R}, \text{drop-in}_R \rangle \pi_3 = \langle \text{move}_{L,R}, \text{drop-in}_R \rangle \pi_4 = \langle \text{pick-in}_L, \text{move}_{L,R}, \text{drop-in}_R \rangle$$

**Flaw:**  $s_0 = LL$  is not a goal state.

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## CEGAR for unit-cost tasks. Three kinds of flaws:

- Abstract plan works in concrete transition system, but ends in **non-goal state**.  
(Step 0 in example.)
- Some step of abstract plan fails in concrete transition system, because **operator precondition is violated**.  
(Steps 1 and 2 in example.)
- Concrete and abstract **paths diverge** at some point, because abstract transition system is nondeterministic.  
(Step 3 in example.)

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**Flaw 1:** Abstract plan terminates in concrete non-goal state.

**Resolution:** Split abstraction of last state  $s_n$  of concrete trace into (a) part containing  $s_n$ , but containing no concrete goal state, and (b) rest.

**Flaw 2:** Abstract plan fails because some operator precondition is violated.

**Resolution:** Split abstraction of state  $s_{i-1}$  of concrete trace, where operator precondition  $\chi$  is violated, into (a) part containing  $s_{i-1}$ , but no concrete state in which precondition  $\chi$  is satisfied, and (b) rest.

**Flaw 3:** Concrete and abstract paths diverge.

**Resolution:** Split abstraction of state  $s_{i-1}$  of concrete trace, after which paths diverge when applying operator  $o$ , into (a) part containing  $s_{i-1}$  where applying  $o$  always leads to the “wrong” abstract successor state, and (b), rest.

**Remark:** In tasks with state-dependent action costs, there is a fourth type of flaws, so-called **cost-mismatch** flaws.

**Flaw 4:** Action is **more costly** in concrete state than in abstract state.

**Resolution:** Split abstraction of violating concrete state into two parts that differ on the value of a variable that is relevant to the cost function of the operator in question, such that we have different cost values in the two parts.

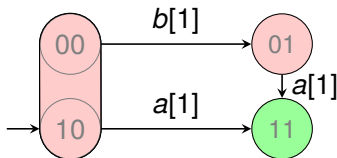
## Example (Cost-mismatch flaw)

$$a = \langle \top, x \wedge y \rangle, \text{cost}_a = 2x + 1$$

$$s_0 = 10$$

$$b = \langle \top, \neg x \wedge y \rangle, \text{cost}_b = 1$$

$$s_\star = x \wedge y$$



- Optimal abstract plan:  $\langle a \rangle$  (abstract cost 1)
- This is also a **concrete plan** (concrete cost  $3 \neq 1$ )  
 $\rightsquigarrow$  split  $\{0, 1\} \times \{0\}$
- Cf. optimal concrete plan:  $\langle b, a \rangle$  (concr. and abstr. cost 2)

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### Summary:

- State-dependent actions costs practically relevant.
- EVMDDs exhibit and exploit structure in cost functions.
- Graph-based representations of arithmetic functions.
- Edge values express partial cost contributed by facts.
- Size of EVMDD is **compact** in many “typical” cases.
- Can be used to compile tasks with state-dependent costs to tasks with state-independent costs.
- Alternatively, can be embedded into the RPG to compute forward-cost heuristics directly.
- For  $h^{add}$ , both approaches give the same heuristic values.
- Abstraction heuristics can also be generalized to state-dependent action costs.

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### Future Work and Work in Progress:

- Investigation of other delete-relaxation heuristics for tasks with state-dependent action costs.
- Investigation of static and dynamic EVMDD variable orders.
- Application to cost partitioning, to planning with preferences, ...
- Better integration of SDAC in PDDL.
- Tool support.
- Benchmarks.

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