Principles of AI Planning

8. Planning as search: relaxation heuristics



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Parallel plans

Parallel plans

Plan steps Forward distances

Relaxed planning graphs

Relaxation heuristics

Towards better relaxed plans



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Why does the greedy algorithm compute low-quality plans?

It may apply many operators which are not goal-directed.

How can this problem be fixed?

- Reaching the goal of a relaxed planning task is most easily achieved with forward search.
- Analyzing relevance of an operator for achieving a goal (or subgoal) is most easily achieved with backward search.

Idea: Use a forward-backward algorithm that first finds a path to the goal greedily, then prunes it to a relevant subplan.

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Plan steps Forward distances

Relaxed planning graphs

Relaxation heuristics

Relaxed plan steps



How to decide which operators to apply in forward direction?

■ We avoid such a decision by applying all applicable operators simultaneously.

Definition (plan step)

A plan step is a set of operators $\omega = \{\langle \chi_1, e_1 \rangle, \dots, \langle \chi_n, e_n \rangle\}.$ In the special case of all operators of ω being relaxed, we further define:

- Plan step ω is applicable in state s iff $s \models \chi_i$ for all $i \in \{1, ..., n\}.$
- The result of applying ω to s, in symbols $app_{\omega}(s)$, is defined as the state s' with $on(s') = on(s) \cup \bigcup_{i=1}^{n} [e_i]_s$.

general semantics for plan steps \infty much later

Plan steps

Applying relaxed plan steps: examples



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In all cases, $s = \{a \mapsto 0, b \mapsto 0, c \mapsto 1, d \mapsto 0\}.$

$$\blacksquare \omega = \{\langle c, a \rangle, \langle \top, b \rangle\}$$

$$\blacksquare$$
 $\omega = \{\langle c, a \rangle, \langle c, a \rhd b \rangle\}$

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Relaxation heuristics

Serializations



Applying a relaxed plan step to a state is related to applying the operators in the step to a state in sequence.

Definition (serialization)

A serialization of plan step $\omega = \{o_1^+, \dots, o_n^+\}$ is a sequence $o_{\pi(1)}^+, \dots, o_{\pi(n)}^+$ where π is a permutation of $\{1, \dots, n\}$.

Lemma (conservativeness of plan step semantics)

If ω is a plan step applicable in a state s of a relaxed planning task, then each serialization o_1, \ldots, o_n of ω is applicable in s and $app_{o_1, \ldots, o_n}(s)$ dominates $app_{\omega}(s)$.

- Does equality hold for all/some serialization(s)?
- What if there are no conditional effects?
- What if we allowed general (unrelaxed) planning tasks?

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Plan steps

Forward distance

Relaxed planning graphs

Relaxation heuristics



Definition (parallel plan)

A parallel plan for a relaxed planning task $\langle A, I, O^+, \gamma \rangle$ is a sequence of plan steps $\omega_1, \dots, \omega_n$ of operators in O^+ with:

- \blacksquare $s_0 := I$
- For i = 1,...,n, step ω_i is applicable in s_{i-1} and $s_i := app_{\omega_i}(s_{i-1})$.
- $\blacksquare s_n \models \gamma$

Remark: By ordering the operators within each single step arbitrarily, we obtain a (regular, non-parallel) plan.

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Forward states, plan steps and sets



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Idea: In the forward phase of the heuristic computation,

- apply plan step with all operators applicable initially,
- apply plan step with all operators applicable then,
- and so on.

Definition (forward state/plan step/set)

Let $\Pi^+ = \langle A, I, O^+, \gamma \rangle$ be a relaxed planning task.

The *n*-th forward state, in symbols s_n^F ($n \in \mathbb{N}_0$), the *n*-th forward plan step, in symbols ω_n^F ($n \in \mathbb{N}_1$), and the *n*-th forward set, in symbols S_n^F ($n \in \mathbb{N}_0$), are defined as:

$$\mathbf{s}_0^\mathsf{F} := I$$

■
$$\omega_n^{\mathsf{F}} := \{ o \in O^+ \mid o \text{ applicable in } s_{n-1}^{\mathsf{F}} \}$$
 for all $n \in \mathbb{N}_1$

$$\blacksquare$$
 $s_n^{\mathsf{F}} := app_{\omega_n^{\mathsf{F}}}(s_{n-1}^{\mathsf{F}}) \text{ for all } n \in \mathbb{N}_1$

$$S_n^F := on(s_n^F)$$
 for all $n \in \mathbb{N}_0$

Parallel plans
Plan steps
Forward distances

Relaxed planning

Relaxation heuristics



Definition (parallel forward distance)

The parallel forward distance of a relaxed planning task $\langle A, I, O^+, \gamma \rangle$ is the lowest number $n \in \mathbb{N}_0$ such that $s_n^{\mathsf{F}} \models \gamma$, or ∞ if no forward state satisfies γ .

Remark: The parallel forward distance can be computed in polynomial time. (How?)

Definition (max heuristic h_{max})

Let $\Pi = \langle A, I, O, \gamma \rangle$ be a planning task in positive normal form, and let s be a state of Π .

The max heuristic estimate for s, $h_{max}(s)$, is the parallel forward distance of the relaxed planning task $\langle A, s, O^+, \gamma \rangle$.

Remark: h_{max} is safe, goal-aware, admissible and consistent. (Whv?)

Forward distances

So far, so good...



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- We have seen how systematic computation of forward states leads to an admissible heuristic estimate
- However, this estimate is very coarse.
- To improve it, we need to include backward propagation of information

For this purpose, we use so-called relaxed planning graphs.

plans Plan steps

Forward distances

Relaxed planning

Relaxation heuristics



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Paralle plans

Relaxed planning graphs

Construction Truth values

Relaxation heuristics



Paralle

Relaxed planning graphs

Introduction Construction

Truth values

heuristics

Summary

Definition (AND/OR dag)

An AND/OR dag $\langle V, A, type \rangle$ is a directed acyclic graph $\langle V, A \rangle$ with a label function $type: V \to \{\land, \lor\}$ partitioning nodes into AND nodes $(type(v) = \land)$ and OR nodes $(type(v) = \lor)$.

Note: AND nodes drawn as squares, OR nodes as circles.

Definition (truth values in AND/OR dags)

Let $G = \langle V, A, type \rangle$ be an AND/OR dag, and let $u \in V$ be a node with successor set $\{v_1, \dots, v_k\} \subseteq V$.

The (truth) value of u, val(u), is inductively defined as:

- If $type(u) = \land$, then $val(u) = val(v_1) \land \cdots \land val(v_k)$.
- If $type(u) = \vee$, then $val(u) = val(v_1) \vee \cdots \vee val(v_k)$.

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Introduction Construction

Truth values

heuristics

Summary

Let Π^+ be a relaxed planning task, and let $k \in \mathbb{N}_0$.

The relaxed planning graph of Π^+ for depth k, in symbols $RPG_k(\Pi^+)$, is an AND/OR dag that encodes

- which propositions can be made true in *k* plan steps, and
- how they can be made true.

Its construction is a bit involved, so we present it in stages.

Running example



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As a running example, consider the relaxed planning task $\langle A, I, \{o_1, o_2, o_3, o_4\}, \gamma \rangle$ with

$$A = \{a,b,c,d,e,f,g,h\}$$

$$I = \{a \mapsto 1,b \mapsto 0,c \mapsto 1,d \mapsto 1,$$

$$e \mapsto 0,f \mapsto 0,g \mapsto 0,h \mapsto 0\}$$

$$o_1 = \langle b \lor (c \land d),b \land ((a \land b) \rhd e) \rangle$$

$$o_2 = \langle \top,f \rangle$$

$$o_3 = \langle f,g \rangle$$

$$o_4 = \langle f,h \rangle$$

$$\gamma = e \land (g \land h)$$

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Relaxed planning graphs

Construction

Truth values

heuristics Summary

Running example: forward sets and plan steps



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$$\begin{split} I &= \{a \mapsto 1, b \mapsto 0, c \mapsto 1, d \mapsto 1, e \mapsto 0, f \mapsto 0, g \mapsto 0, h \mapsto 0\} \\ o_1 &= \langle b \lor (c \land d), b \land ((a \land b) \rhd e) \rangle \\ o_2 &= \langle \top, f \rangle, \quad o_3 &= \langle f, g \rangle, \quad o_4 &= \langle f, h \rangle \\ \\ S_0^F &= \{a, c, d\} \\ \omega_1^F &= \{o_1, o_2\} \\ S_1^F &= \{a, b, c, d, f\} \\ \omega_2^F &= \{o_1, o_2, o_3, o_4\} \\ S_2^F &= \{a, b, c, d, e, f, g, h\} \\ \omega_3^F &= \omega_2^F \\ S_3^F &= S_2^F \text{ etc.} \end{split}$$

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Relaxation heuristics

Components of relaxed planning graphs



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A relaxed planning graph consists of four kinds of components:

- Proposition nodes represent the truth value of propositions after applying a certain number of plan steps.
- Idle arcs represent the fact that state variables, once true, remain true.
- Operator subgraphs represent the possibility and effect of applying a given operator in a given plan step.
- The goal subgraph represents the truth value of the goal condition after *k* plan steps.

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planning graphs Introduction

Construction Truth values

Relaxation

Relaxed planning graph: proposition layers



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Let $\Pi^+ = \langle A, I, O^+, \gamma \rangle$ be a relaxed planning task, let $k \in \mathbb{N}_0$.

For each $i \in \{0,...,k\}$, $RPG_k(\Pi^+)$ contains one proposition layer which consists of:

■ a proposition node a^i for each state variable $a \in A$.

Node a^i is an AND node if i = 0 and $I \models a$. Otherwise, it is an OR node.

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Truth values

heuristics

Relaxed planning graph: proposition layers





a ⁰



























































































Relaxed planning graph: idle arcs



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For each proposition node a^i with $i \in \{1, ..., k\}$, $RPG_k(\Pi^+)$ contains an arc from a^i to a^{i-1} (idle arcs).

Intuition: If a state variable is true in step *i*, one of the possible reasons is that it was already previously true.

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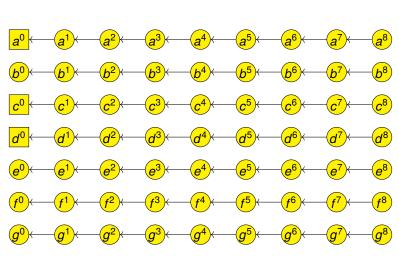
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Truth values

Relaxation

Relaxed planning graph: idle arcs







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Construction Truth values

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Relaxed planning graph: operator subgraphs



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For each $i \in \{1,...,k\}$ and each operator $o^+ = \langle \chi, e^+ \rangle \in O^+$, $RPG_k(\Pi^+)$ contains a subgraph called an operator subgraph with the following parts:

- one formula node n_{φ}^{i} for each formula φ which is a subformula of χ or of some effect condition in e^{+} :
 - If $\varphi = a$ for some atom a, n_{φ}^{i} is the proposition node a^{i-1} .
 - If $\varphi = \top$, n_{φ}^{i} is a new AND node without outgoing arcs.
 - If $\varphi = \bot$, n_{φ}^{i} is a new OR node without outgoing arcs.
 - If $\varphi = (\varphi' \wedge \varphi'')$, n_{φ}^i is a new AND node with outgoing arcs to $n_{\varphi'}^i$ and $n_{\varphi''}^i$.
 - If $\varphi = (\varphi' \vee \varphi'')$, n_{φ}^i is a new OR node with outgoing arcs to $n_{\varphi'}^i$ and $n_{\varphi''}^i$.

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planning graphs Introduction

Construction Truth values

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Relaxed planning graph: operator subgraphs



For each $i \in \{1, ..., k\}$ and each operator $o^+ = \langle \chi, e^+ \rangle \in O^+$, $RPG_k(\Pi^+)$ contains a subgraph called an operator subgraph with the following parts:

- for each conditional effect $(\chi' \triangleright a)$ in e^+ , an effect node $o^i_{\chi'}$ (an AND node) with outgoing arcs to the precondition formula node n^i_{χ} and effect condition formula node $n^i_{\chi'}$, and incoming arc from proposition node a^i
 - unconditional effects a (effects which are not part of a conditional effect) are treated the same, except that there is no arc to an effect condition formula node
 - effects with identical condition (including groups of unconditional effects) share the same effect node
 - \blacksquare the effect node for unconditional effects is denoted by o^i

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Relaxed planning graphs

Construction
Truth values

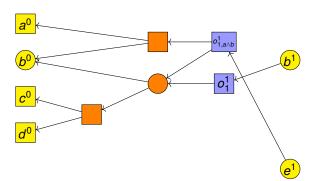
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Relaxed planning graph: operator subgraphs



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Operator subgraph for $o_1 = \langle b \lor (c \land d), b \land ((a \land b) \rhd e) \rangle$ for layer i = 1.



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Construction Truth values

heuristics

Relaxed planning graph: goal subgraph



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 $RPG_{\kappa}(\Pi^{+})$ contains a subgraph called a goal subgraph with the following parts:

- one formula node n_{φ}^k for each formula φ which is a subformula of γ :
 - If $\varphi = a$ for some atom a, n_{φ}^{k} is the proposition node a'.
 - If $\varphi = \top$, n_{φ}^{k} is a new AND node without outgoing arcs.
 - If $\varphi = \bot$, n_{φ}^{k} is a new OR node without outgoing arcs.
 - If $\varphi = (\varphi' \wedge \varphi'')$, n_{φ}^k is a new AND node with outgoing arcs to $n_{\varphi'}^k$ and $n_{\varphi''}^k$.
 - If $\varphi = (\varphi' \vee \varphi'')$, n_{φ}^k is a new OR node with outgoing arcs to $n_{\varphi'}^k$ and $n_{\varphi''}^k$.

The node n_{γ}^{k} is called the goal node.

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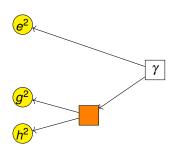
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Relaxed planning graph: goal subgraphs



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Goal subgraph for $\gamma = e \wedge (g \wedge h)$ and depth k = 2:



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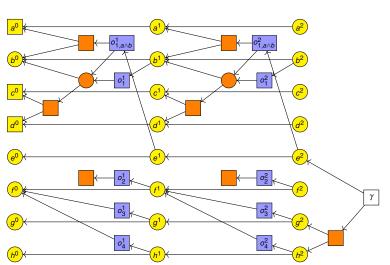
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Relaxed planning graph: complete (depth 2)



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Connection to forward sets and plan steps



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Theorem (relaxed planning graph truth values)

Let $\Pi^+ = \langle A, I, O^+, \gamma \rangle$ be a relaxed planning task. Then the truth values of the nodes of its depth-k relaxed planning graph $RPG_k(\Pi^+)$ relate to the forward sets and forward plan steps of Π^+ as follows:

- Proposition nodes: For all $a \in A$ and $i \in \{0,...,k\}$, $val(a^i) = 1$ iff $a \in S_i^F$.
- (Unconditional) effect nodes: For all $o \in O^+$ and $i \in \{1,...,k\}$, $val(o^i) = 1$ iff $o \in \omega_i^F$.
- Goal nodes: $val(n_{\gamma}^{k}) = 1$ iff the parallel forward distance of Π^{+} is at most k.

(We omit the straight-forward proof.)

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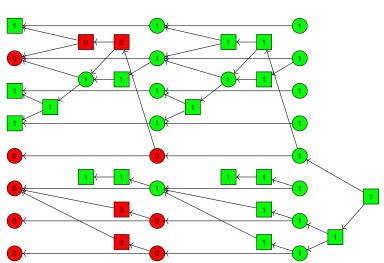
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Computing the node truth values







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Remark: Relaxed planning graphs have historically been defined for STRIPS tasks only. In this case, we can simplify:

- Only one effect node per operator: STRIPS does not have conditional effects.
 - Because each operator has only one effect node, effect nodes are called operator nodes in relaxed planning graphs for STRIPS.
- No goal nodes: The test whether all goals are reached is done by the algorithm that evaluates the AND/OR dag.
- No formula nodes: Operator nodes are directly connected to their preconditions.
- → Relaxed planning graphs for STRIPS are layered digraphs and only have proposition and operator nodes.

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planning graphs Introduction

Construction Truth values

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Relaxation heuristics

Generic template

h_{max} h_{add}

Incremental computation

h_{FF}

Computing parallel forward distances from RPGs



So far, relaxed planning graphs offer us a way to compute parallel forward distances:

Parallel forward distances from relaxed planning graphs

```
def parallel-forward-distance(\Pi^+):

Let A be the set of state variables of \Pi^+.

for k \in \{0,1,2,\dots\}:

rpg := RPG_k(\Pi^+)

Evaluate truth values for rpg.

if goal node of rpg has value 1:

return k

else if k = |A|:

return \infty
```

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n_{add}

Incremental

computation h_{FF}

Comparison & practice

Remarks on the algorithm



- The relaxed planning graph for depth $k \ge 1$ can be built incrementally from the one for depth k 1:
 - Add new layer k.
 - Move goal subgraph from layer k-1 to layer k.
- \blacksquare Similarly, all truth values up to layer k-1 can be reused.
- Thus, overall computation with maximal depth m requires time $O(\|RPG_m(\Pi^+)\|) = O((m+1) \cdot \|\Pi^+\|)$.
- This is not a very efficient way of computing parallel forward distances (and wouldn't be used in practice).
- However, it allows computing additional information for the relaxed planning graph nodes along the way, which can be used for heuristic estimates.

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max

sa

Incremental computation

Comparison practice

Generic relaxed planning graph heuristics



Computing heuristics from relaxed planning graphs

```
def generic-rpg-heuristic(\langle A, I, O, \gamma \rangle, s):
```

$$\Pi^+ := \langle A, s, O^+, \gamma \rangle$$
 for $k \in \{0, 1, 2, \dots\}$:

$$rpg := RPG_k(\Pi^+)$$

Evaluate truth values for rpg.

if goal node of rpg has value 1:

Annotate true nodes of rpg.

if termination criterion is true:

return heuristic value from annotations

else if
$$k = |A|$$
: return ∞

generic template for heuristic functions

→ to get concrete heuristic: fill in highlighted parts

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Concrete examples for the generic heuristic



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Many planning heuristics fit the generic template:

- additive heuristic h_{add} (Bonet, Loerincs & Geffner, 1997)
- max heuristic h_{max} (Bonet & Geffner, 1999)
- FF heuristic *h*_{FF} (Hoffmann & Nebel, 2001)
- cost-sharing heuristic h_{cs} (Mirkis & Domshlak, 2007)
 - not covered in this course
- set-additive heuristic *h*_{sa} (Keyder & Geffner, 2008)

Remarks:

- For all these heuristics, equivalent definitions that don't refer to relaxed planning graphs are possible.
- Historically, such equivalent definitions have mostly been used for h_{max} , h_{add} and h_{sa} .
- For those heuristics, the most efficient implementations do not use relaxed planning graphs explicitly.

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h_{sa}

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Forward cost heuristics



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- The simplest relaxed planning graph heuristics are forward cost heuristics.
- Examples: h_{max}, h_{add}
- Here, node annotations are cost values (natural numbers).
- The cost of a node estimates how expensive (in terms of required operators) it is to make this node true.

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Incremental computation

Comparison 8



Forward cost heuristics

Computing annotations:

- Propagate cost values bottom-up using a combination rules for OR nodes and for AND nodes.
- At effect nodes, add 1 after applying combination rule.

Termination criterion:

■ stability: terminate if cost for proposition node a^k equals cost for a^{k-1} for all true propositions a in layer k

Heuristic value:

- The heuristic value is the cost of the goal node.
- Different forward cost heuristics only differ in their choice of combination rules.

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Relaxed planning graphs

Relaxation heuristics

Generic template

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h_{sa}

Incremental computation

Comparison practice

The max heuristic h_{max} (again)



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Forward cost heuristics: max heuristic h_{\max}

Combination rule for AND nodes:

 $cost(u) = \max(\{cost(v_1), \dots, cost(v_k)\})$ (with max(\emptyset) := 0)

Combination rule for OR nodes:

 $cost(u) = min(\{cost(v_1), \dots, cost(v_k)\})$

In both cases, $\{v_1, \dots, v_k\}$ is the set of true successors of u.

Intuition:

- AND rule: If we have to achieve several conditions, estimate this by the most expensive cost.
- OR rule: If we have a choice how to achieve a condition, pick the cheapest possibility.

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7_{max} 7_{add}

Incremental

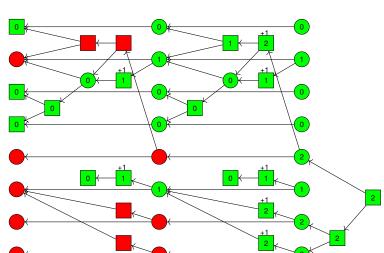
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Comparison a

Running example: h_{max}







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Relaxation heuristics

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 Unlike the earlier definition, it generalizes to an extension where every operator has an associated non-negative cost (rather than all operators having cost 1).

- In the case without costs (and only then), it is easy to prove that the goal node has the same cost in all graphs $RPG_k(\Pi^+)$ where it is true. (Namely, the cost is equal to the lowest value of k for which the goal node is true.)
- We can thus terminate the computation as soon as the goal becomes true, without waiting for stability.
- The same is not true for other forward-propagating heuristics (h_{add} , h_{cs} , h_{sa}).

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Relaxed planning graphs

heuristics
Generic template

h_{max}

h_{add}

Incremental

computation h_{FF}

Comparison 8 practice



Combination rule for AND nodes:

 $cost(u) = cost(v_1) + ... + cost(v_k)$ (with $\sum(\emptyset) := 0$)

Combination rule for OR nodes:

 $cost(u) = min(\{cost(v_1), \dots, cost(v_k)\})$

In both cases, $\{v_1, \dots, v_k\}$ is the set of true successors of u.

Intuition:

- AND rule: If we have to achieve several conditions, estimate this by the cost of achieving each in isolation.
- OR rule: If we have a choice how to achieve a condition, pick the cheapest possibility.

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Relaxed planning graphs

heuristics

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h_{sa}

Incremental computation

Comparison

Running example: h_{add}



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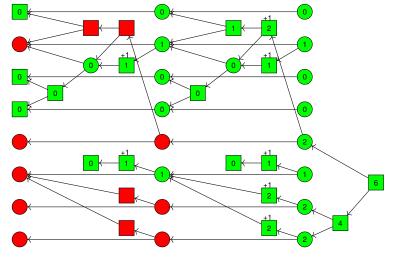
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h_{sa}

Incremental

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- Stability is achieved after layer |A| in the worst case.
- \blacksquare h_{add} is safe and goal-aware.
- Unlike h_{max} , h_{add} is a very informative heuristic in many planning domains.
- The price for this is that it is not admissible (and hence also not consistent), so not suitable for optimal planning.
- In fact, it almost always overestimates the h⁺ value because it does not take positive interactions into account.

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- We now discuss a refinement of the additive heuristic called the set-additive heuristic h_{sa}.
- The set-additive heuristic addresses the problem that h_{add} does not take positive interactions into account.
- Like h_{max} and h_{add} , h_{sa} is calculated through forward propagation of node annotations.
- However, the node annotations are not cost values, but sets of operators (kind of).
- The idea is that by taking set unions instead of adding costs, operators needed only once are counted only once.

Disclaimer: There are some quite subtle differences between the $h_{\rm sa}$ heuristic as we describe it here and the "real" heuristic of Keyder & Geffner. We do not want to discuss this in detail, but please note that such differences exist.

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Generic template

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sa

Incrementa

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Comparison & practice



- The original h_{sa} heuristic as described in the literature is defined for STRIPS tasks and propagates sets of operators.
- This is fine because in relaxed STRIPS tasks, each operator need only be applied once.
- The same is not true in general: in our running example, operator o_1 must be applied twice in the relaxed plan.
- In general, it only makes sense to apply an operator again in a relaxed planning task if a previously unsatisfied effect condition has been made true.
- For this reason, we keep track of operator/effect condition pairs rather than just plain operators.

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h_{FF} Comparison 8

Set-additive heuristic: fitting the template



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The set-additive heuristic h_{sa}

Computing annotations:

Annotations are sets of operator/effect condition pairs, computed bottom-up.

Combination rule for AND nodes:

■ $ann(u) = ann(v_1) \cup \cdots \cup ann(v_k)$ (with $\bigcup (\emptyset) := \emptyset$)

Combination rule for OR nodes:

■ $ann(u) = ann(v_i)$ for some v_i minimizing $|ann(v_i)|$ In case of several minimizers, use any tie-breaking rule.

In both cases, $\{v_1, \ldots, v_k\}$ is the set of true successors of u. At effect nodes, add the corresponding operator/effect condition pair to the set after applying combination rule.

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Incremental computation

Comparison &



The set-additive heuristic h_{sa} (ctd.)

Computing annotations:

...(Effect nodes for unconditional effects are represented just by the operator, without a condition.)

Termination criterion:

■ stability: terminate if set for proposition node a^k has same cardinality as for a^{k-1} for all true propositions a in layer k

Heuristic value:

■ The heuristic value is the set cardinality of the goal node annotation.

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Running example: $h_{\rm sa}$







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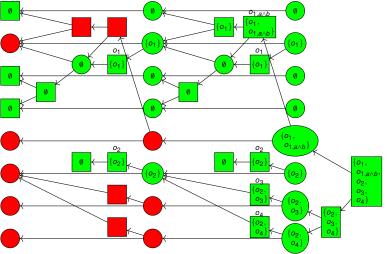
Generic template

h_{max}

h_{sa}

computation

Comparison & practice





- Like *h*_{add}, *h*_{sa} is safe and goal-aware, but neither admissible nor consistent.
- h_{sa} is generally better informed than h_{add} , but significantly more expensive to compute.
- The *h*_{sa} value depends on the tie-breaking rule used, so *h*_{sa} is not well-defined without specifying the tie-breaking rule.
- The operators contained in the goal node annotation, suitably ordered, define a relaxed plan for the task.
 - Operators mentioned several times in the annotation must be added as many times in the relaxed plan.

Paralle plans

Relaxed planning graphs

heuristics

Generic template

h_{add}

Incremental

n_{FF}
Comparison 8
practice

Incremental computation of forward heuristics



FREIBL

One nice property of forward-propagating heuristics is that they allow incremental computation:

- when evaluating several states in sequence which only differ in a few state variables, can
 - start computation from previous results and
 - keep track only of what needs to be recomputed
- typical use case: depth-first style searches (e.g., IDA*)
- rarely exploited in practice

Parallel plans

Relaxed planning graphs

neuristics

Generic template

h_{max}

Incremental

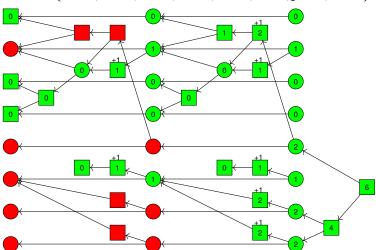
computation h_{FF}

Comparison 8 practice



UNI FREIBURG

Result for $\{a \mapsto 1, b \mapsto 0, c \mapsto 1, d \mapsto 1, e \mapsto 0, f \mapsto 0, g \mapsto 0, h \mapsto 0\}$



Parallel plans

Relaxed planning graphs

Relaxation heuristics

Generic template

n_{max} h_{add}

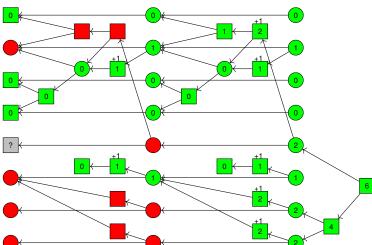
Incremental computation

h_{FF}
Comparison 8
practice



EIBURG

Change value of e to 1.



Parallel plans

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Relaxation heuristics

Generic template

h_{max} h_{add}

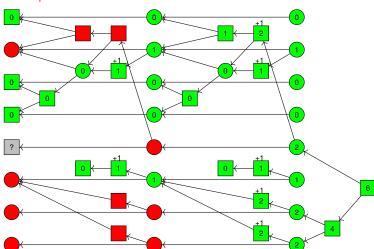
Incremental computation

h_{FF}
Comparison &



EIBURG

Recompute outdated values.



Parallel

Relaxed planning graphs

Relaxation heuristics

Generic template

h_{max} h_{add}

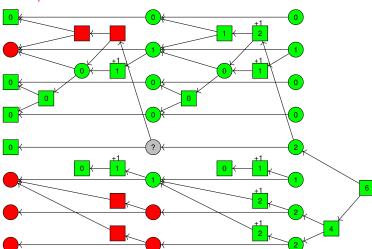
Incremental computation

h_{FF} Comparison &



EIBURG

Recompute outdated values.



Parallel plans

Relaxed planning graphs

Relaxation heuristics

Generic template

h_{max} h_{add}

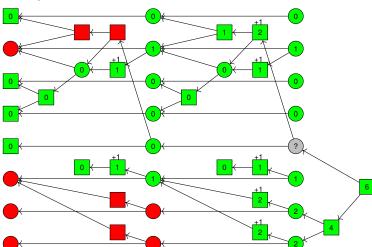
Incremental computation

h_{FF}
Comparison & practice



EIBURG

Recompute outdated values.



Parallel plans

Relaxed planning graphs

Relaxation heuristics

Generic template

h_{max} h_{add}

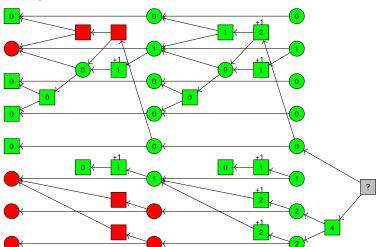
Incremental computation

h_{FF}
Comparison &



EIBURG

Recompute outdated values.



Parallel plans

Relaxed planning graphs

Relaxation heuristics

Generic template

h_{max}

Incremental

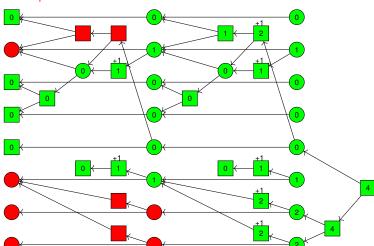
computation $h_{\rm FF}$

Comparison & practice



EIBURG

Recompute outdated values.



Parallel

Relaxed planning graphs

Relaxation heuristics

Generic template

h_{max} h_{add}

Incremental

h_{FF} Comparison &



- h_{sa} is more expensive to compute than the other forward propagating heuristics because we must propagate sets.
- It is possible to get the same advantage over h_{add} combined with efficient propagation.
- Key idea of h_{FF}: perform a backward propagation that selects a sufficient subset of nodes to make the goal true (called a solution graph in AND/OR dag literature).
- The resulting heuristic is almost as informative as h_{sa} , yet computable as quickly as h_{add} .

Note: Our presentation inverts the historical order.
The set-additive heuristic was defined after the FF heuristic (sacrificing speed for even higher informativeness).

Parallel plans

Relaxed planning graphs

heuristics
Generic template

h_{max}

h_{add}

Incremental computation

h_{FF} Comparison 8

FF heuristic: fitting the template



The FF heuristic h_{FF} Computing annotations:

■ Annotations are Boolean values, computed top-down.

A node is marked when its annotation is set to 1 and unmarked if it is set to 0. Initially, the goal node is marked, and all other nodes are unmarked.

We say that a true AND node is justified if all its true successors are marked, and that a true OR node is justified if at least one of its true successors is marked.

. . .

Paralle plans

Relaxed planning graphs

heuristics

Generic template

h_{add}

Incremental

computation her

Comparison & practice

FF heuristic: fitting the template (ctd.)



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The FF heuristic h_{FF} (ctd.) Computing annotations:

...

Apply these rules until all marked nodes are justified:

- Mark all true successors of a marked unjustified AND node
- Mark the true successor of a marked unjustified OR node with only one true successor.
- Mark a true successor of a marked unjustified OR node connected via an idle arc.
- 4 Mark any true successor of a marked unjustified OR node.

The rules are given in priority order: earlier rules are preferred if applicable.

Parallel plans

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Relaxation heuristics

Generic template

h_{add}

Incremental computation

Omparison 8 practice

FF heuristic: fitting the template (ctd.)



JNI

The FF heuristic h_{FF} (ctd.)

Termination criterion:

Always terminate at first layer where goal node is true.

Heuristic value:

The heuristic value is the number of operator/effect condition pairs for which at least one effect node is marked. Paralle plans

Relaxed planning graphs

Relaxation heuristics

Generic template

hade

 $h_{\rm sa}$

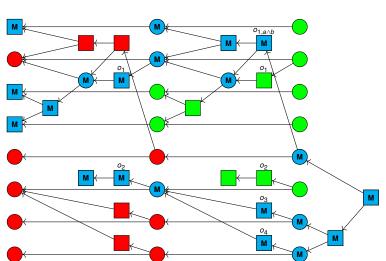
Incremental

h_{FF}

Running example: h_{FF}







Parallel plans

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Relaxation heuristics

Generic template

h_{max} h_{add}

Incrementa

computation

Comparison & practice



- FREIBU
- Like h_{add} and h_{sa} , h_{FF} is safe and goal-aware, but neither admissible nor consistent.
- Its informativeness can be expected to be slightly worse than for h_{sa} , but is usually not far off.
- Unlike h_{sa} , h_{FF} can be computed in linear time.
- Similar to h_{sa} , the operators corresponding to the marked operator/effect condition pairs define a relaxed plan.
- Similar to h_{sa}, the h_{FF} value depends on tie-breaking when the marking rules allow several possible choices, so h_{FF} is not well-defined without specifying the tie-breaking rule.
 - The implementation in FF uses additional rules of thumb to try to reduce the size of the generated relaxed plan.

Parallel plans

> Relaxed planning graphs

heuristics

Generic template

max

Incremental

Incremental computation

h_{FF} Comparison 8

Comparison of relaxation heuristics



UNI

Theorem (relationship between relaxation heuristics)

Let s be a state of planning task $\langle A, I, O, \gamma \rangle$. Then:

- $h_{max}(s) \le h^{+}(s) \le h^{*}(s)$
- $\blacksquare h_{max}(s) \leq h^+(s) \leq h_{sa}(s) \leq h_{add}(s)$
- $\blacksquare h_{max}(s) \leq h^+(s) \leq h_{FF}(s) \leq h_{add}(s)$
- \blacksquare h^* , h_{FF} and h_{sa} are pairwise incomparable
- \blacksquare h^* and h_{add} are incomparable

Moreover, h^+ , h_{max} , h_{add} , h_{sa} and h_{FF} assign ∞ to the same set of states.

Note: For inadmissible heuristics, dominance is in general neither desirable nor undesirable. For relaxation heuristics, the objective is usually to get as close to h^+ as possible.

Parallel plans

planning graphs

heuristics

Generic template

hadd

n_{add}

Incremental

h_{FF}
Comparison 8

Relaxation heuristics in practice: HSP



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Example (HSP)

HSP (Bonet & Geffner) was one of the four top performers at the 1st International Planning Competition (IPC-1998).

Key ideas:

- hill climbing search using hadd
- on plateaus, keep going for a number of iterations, then restart
- use a closed list during exploration of plateaus

Literature: Bonet, Loerincs & Geffner (1997), Bonet & Geffner (2001)

Paralle plans

Relaxed planning graphs

Relaxation heuristics

Generic template

max add

 $h_{\rm sa}$

Incremental computation

Comparison 8 practice

Relaxation heuristics in practice: FF



NI REIBURG

Example (FF)

FF (Hoffmann & Nebel) won the 2nd International Planning Competition (IPC-2000).

Key ideas:

- enforced hill-climbing search using h_{FF}
- helpful action pruning: in each search node, only consider successors from operators that add one of the atoms marked in proposition layer 1
- goal ordering: in certain cases, FF recognizes and exploits that certain subgoals should be solved one after the other

If main search fails, FF performs greedy best-first search using h_{FF} without helpful action pruning or goal ordering.

Parallel plans

Relaxed planning graphs

heuristics

Generic template

max

add

Incremental computation

Comparison & practice

Relaxation heuristics in practice: Fast Downward



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Example (Fast Downward)

Fast Downward (Helmert & Richter) won the satisficing track of the 4th International Planning Competition (IPC-2004).

Key ideas:

- greedy best-first search using h_{FF} and causal graph heuristic (not relaxation-based)
- search enhancements:
 - multi-heuristic best-first search
 - deferred evaluation of heuristic estimates
 - preferred operators (similar to FF's helpful actions)

Literature: Helmert (2006)

Parallel plans

Relaxed planning graphs

Relaxation heuristics

Generic template

n_{max} h_{arid}

h_{sa}

Incremental

Comparison 8

Relaxation heuristics in practice: SGPlan



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Example (SGPlan)

SGPlan (Wah, Hsu, Chen & Huang) won the satisficing track of the 5th International Planning Competition (IPC-2006). Key ideas:

- FF
- problem decomposition techniques
- domain-specific techniques

Literature: Chen, Wah & Hsu (2006)

Parallel plans

Relaxed planning graphs

heuristics
Generic template

h

h_{add}

h_{sa}

Incremental computation

Comparison & practice

Relaxation heuristics in practice: LAMA



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Example (LAMA)

LAMA (Richter & Westphal) won the satisficing track of the 6th International Planning Competition (IPC-2008).

Key ideas:

- Fast Downward
- landmark pseudo-heuristic instead of causal graph heuristic ("somewhat" relaxation-based)
- anytime variant of Weighted A* instead of greedy best-first search

Literature: Richter, Helmert & Westphal (2008), Richter & Westphal (2010)

Parallel plans

Relaxed planning graphs

Relaxation heuristics

Generic template

h_{add}

h_{sa}

Incremental computation

Comparison 8 practice



- Relaxed planning graphs are AND/OR dags. They encode which propositions can be made true in Π^+ and how.
 - Closely related to forward sets and forward plan steps, based on the notion of parallel relaxed plans.
 - They can be constructed and evaluated efficiently, in time $O((m+1)\|\Pi^+\|)$ for planning task Π and depth m.
- By annotating RPG nodes with appropriate information, we can compute many useful heuristics.
- Examples: max heuristic h_{max}, additive heuristic h_{add}, set-additive heuristic h_{sa} and FF heuristic h_{FF}
 - \blacksquare Of these, only h_{max} admissible (but not very accurate).
 - The others are much more informative. The set-additive heuristic is the most sophisticated one.
 - The FF heuristic is often similarly informative. It offers a good trade-off between accuracy and computation time.

Parallel plans

Relaxed planning graphs

Relaxation heuristics